### Two new explicit depth migration schemes that honour local velocity gradients

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Two new migration schemes - p.1/20





Two new migration schemes - p.2/20



A typical CREWES Marmousi seismic image



## Can we improve?



- Can we improve?
- Better images....



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- Better: horizontal velocity gradient (The Stolk operator in GPSPI migration).



- Can we improve?
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- Faster calculation....
- Better: horizontal velocity gradient (The Stolk operator in GPSPI migration).
- Faster: vertical velocity gradient (Stabilizing explicit  $\omega x$  migration using local WKBJ operators).



#### GPSPI

 $\Psi(x,z,\omega)$  is the (frequency) data that would be recorded by a geophone at point (x,z)

$$\Psi(x, z = \Delta z, \omega) = \mathbf{T}_{\alpha} \Psi(x, z = 0, \omega)$$

 $T_{\alpha}$  is a wavefield extrapolation operator.



#### **GPSPI**

$$\Psi(x, z = \Delta z, \omega) = \mathcal{F}^{-1}\left[\alpha\left(v(x), k_x, \omega\right) \mathcal{F}\left[\Psi(x, z = 0, \omega)\right]\right]$$

where

$$\alpha \left( v\left( x \right), k_x, \omega \right) = \begin{cases} e^{i\Delta z k_z(x)}, \ |k_x| \le \frac{\omega}{v(x_0)} \\ e^{-|\Delta z k_z(x)|}, \ |k_x| > \frac{\omega}{v(x_0)} \end{cases}$$

$$k_z(x) = \sqrt{\frac{\omega^2}{v(x_0)^2} - k_x^2}$$



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$$k_{z}(x) = \left(\sqrt{\frac{\omega^{2}}{v(x_{0})^{2}} - k_{x}^{2}}\right)$$



### **Making better images**





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We use the local output velocity. What about a horizontal derivative?



#### **The Stolk correction**

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$$+ \frac{ik_x\omega^2}{2v(x_0)} \left(\frac{\partial}{\partial x}s(x_0)\right) \left(\frac{\omega^2}{v(x_0)^2} - k_x^2\right)^{-3/2}$$



#### **The Stolk correction**

$$k_z(x) = \sqrt{\frac{\omega^2}{v(x_0)^2} - k_x^2} + \frac{ik_x\omega^2}{2v(x_0)} \left(\frac{\partial}{\partial x}s(x_0)\right) \left(\frac{\omega^2}{v(x_0)^2} - k_x^2\right)^{(-3/2)}$$



### **GPSPI and Stolk**



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### **GPSPI and Stolk**



# **GPSPI** migration



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# **Stolk migration**



# **Stolk migration**

- Not much of an improvement (if any).
- Unfortunately, it takes at least twice as long to run.
- High-frequency correction maybe makes Marmousi less than the ideal candidate.













## **V(z)**

$$\alpha = \exp\left(i\Delta z \sqrt{\frac{\omega^2}{v(x_0)^2} - k_x^2}\right)$$



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$$\alpha = \exp\left(i\Delta z \sqrt{\frac{\omega^2}{v(x_0)^2} - k_x^2}\right)$$
$$\alpha = \exp\left(i\int_0^{\Delta z} \sqrt{\frac{\omega^2}{v(z')^2} - k_x^2}dz'\right)$$
$$v(z) = v_0 + Az$$



#### **FOCI** in $\omega - x$





V(z) in  $\omega - x$ 



# **31 point FOCI image**



# 31 point V(z) image, 40m aperture



Marmousi migration, V(z) 31pt 40m ap



GPSPI makes nice images already



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- The Stolk correction only adds computational time
- ....but maybe Marmousi is a lousy test?
- V(z) does a nice job of truncating the operator naturally
- ....this means we can try it in 3D

# Acknowledgements

- Thanks to all CREWES sponsors
- Kevin Hall, Henry Bland, and Rolf Maier
- Hugh Geiger and Saleh Al-Saleh

