



The accuracy of dipole sonic logs and implications

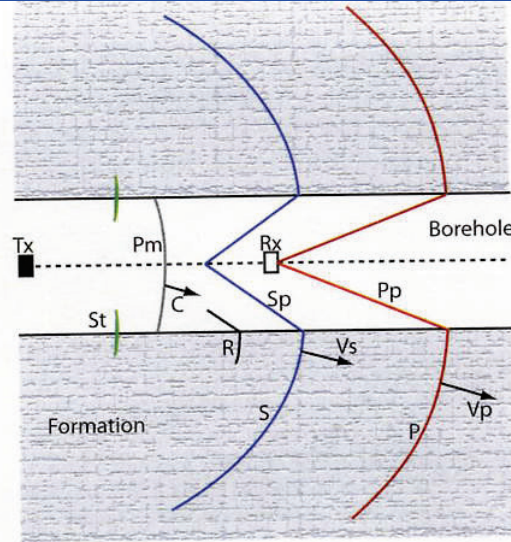
Larry Lines

P.F. Daley

Latif Ibna-Hamid

Sonic waveform propagation

- Sonic waveform component propagation (Close et al., CSEG Recorder, May 2009)

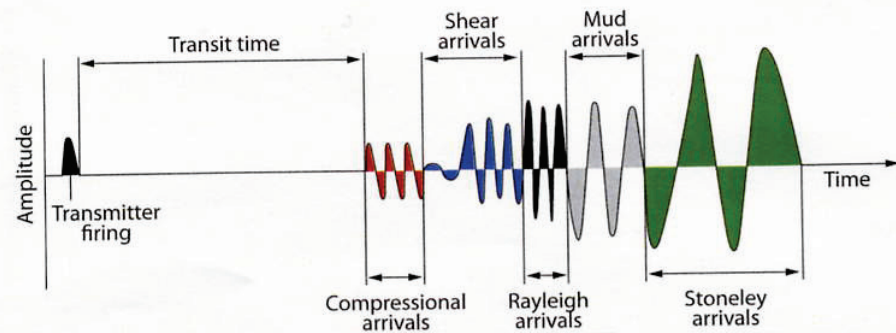


Tx = Transmitter
Rx = Receiver

P = Compressional body wave (refracted)
Pp = Compressional head wave
S = Shear body wave (refracted)
Sp = Shear head wave
R = Pseudo Rayleigh wave (surface wave)
Pm = Direct mud wave
St = Stoneley wave (tube wave)

Vp = Formation compressional velocity
Vs = Formation shear velocity
C = Mud velocity

a)



b)

Why do we make repeat runs of dipole sonic logs?
Photo courtesy of Robert Stewart



Reasons for Repeating Dipole Sonic Measurements

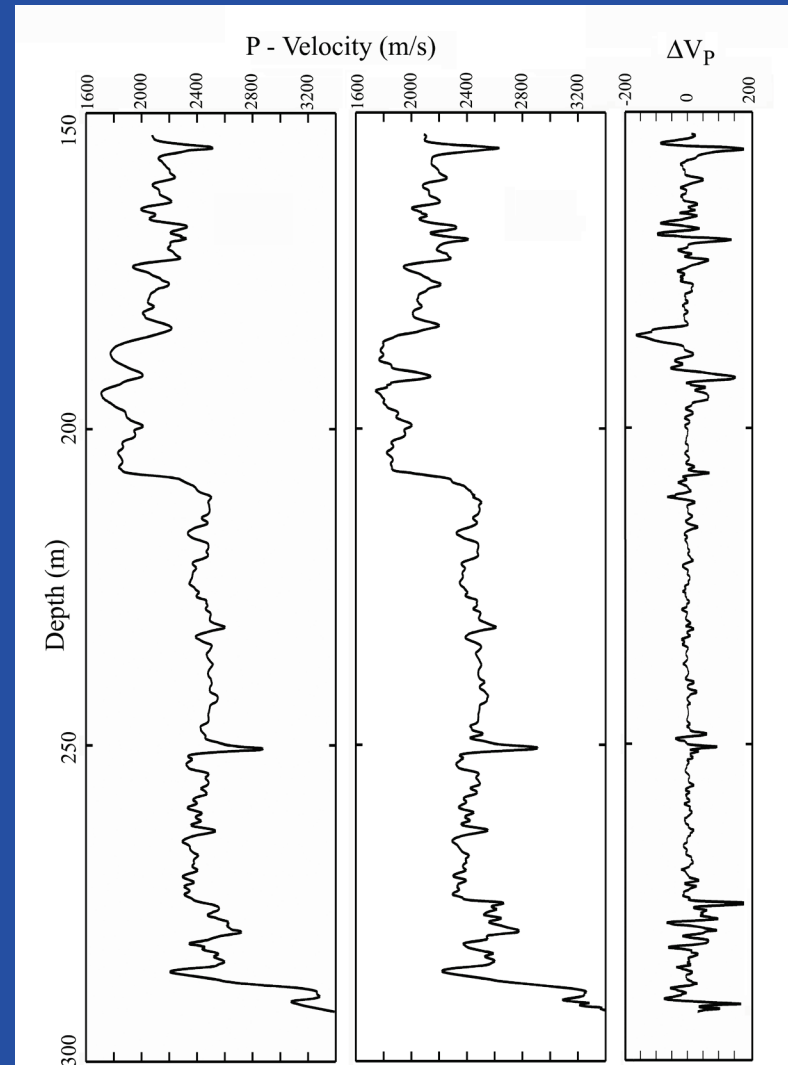
- Once logging equipment has been set up, the incremental cost of repeated measurements is small relative to total costs.
- Repeat runs are often “free of charge” to the customer.
- Provides validation of measurements and data for error analysis.

Analysis of Discrepancies in Repeated Dipole Sonic Logs

- Differences in reflectivity functions
- Differences in synthetic seismograms
- Differences in log-based wavelet (LBW) estimates
- Comparisons of LBW with statistically-based wavelets
- Comparisons of P-wave and shear-wave logs
- Comparisons of VP/VS maps for formations

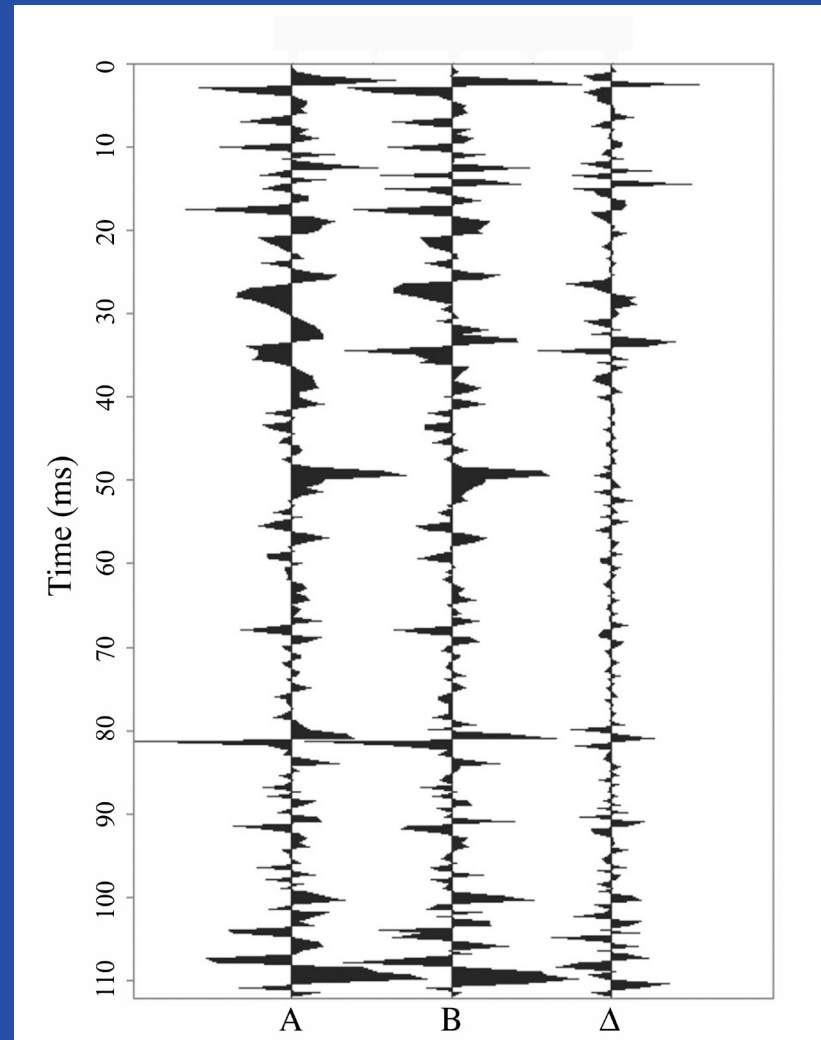
Repeated P-wave sonic logs and discrepancy log

- Two P-wave logs for Long Lake well between depths of 153.5-292m. And the discrepancy log between them (at expanded scale).



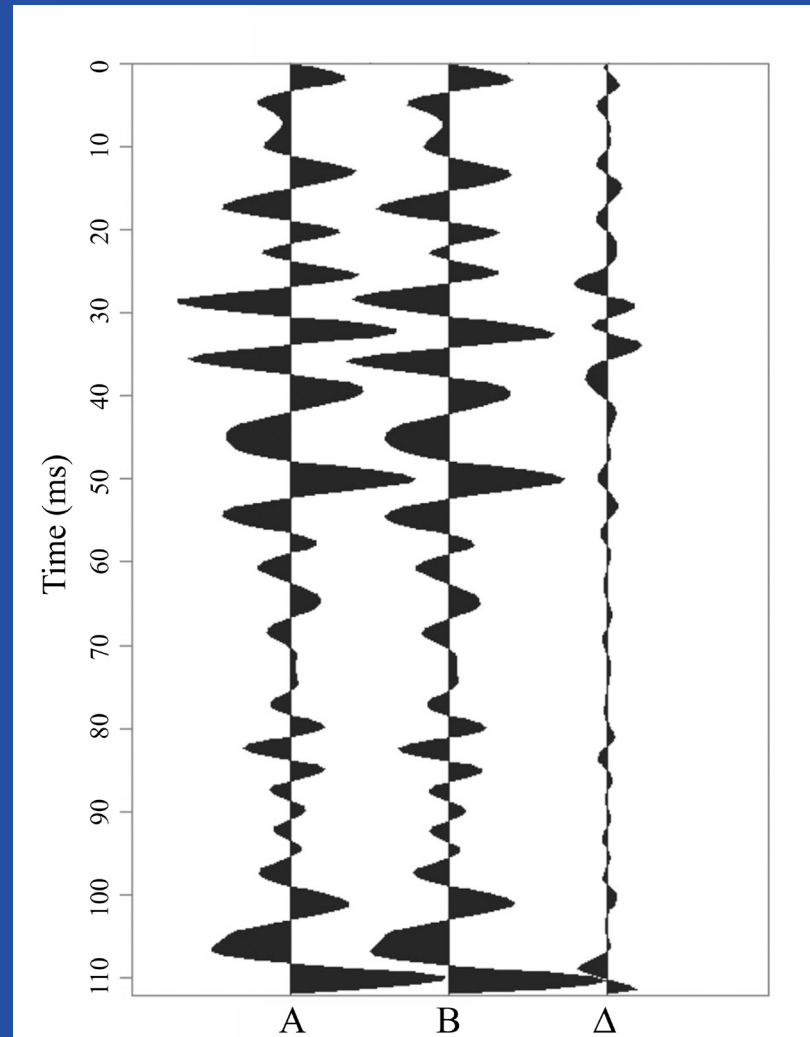
Reflectivity for P-wave sonic logs for Long Lake well

- Reflectivity functions for wells A and B and the difference of reflectivities for B-A.
- The semblance for the two reflectivities = 0.93.
- Sample interval=0.5ms



Synthetic Seismograms for P-wave sonic logs

- Synthetic seismogram using minimum phase equivalent of 150 Hz Ricker wavelet.
- The semblance for the two traces is 0.98
- Sample interval=0.5ms



Log-based Wavelet Estimation

- Two basic assumptions:
 - The wavelet estimated at the well is consistent for the entire seismic line.
 - The reflectivity can be reliably estimated from the well log.

$$W(f) = \frac{Y(f)}{R(f)} \quad \left[W(\omega) = \frac{Y(\omega)}{R(\omega)} \right]$$

Log-based Wavelet Estimation

- Effect of logging errors on the wavelet estimate.

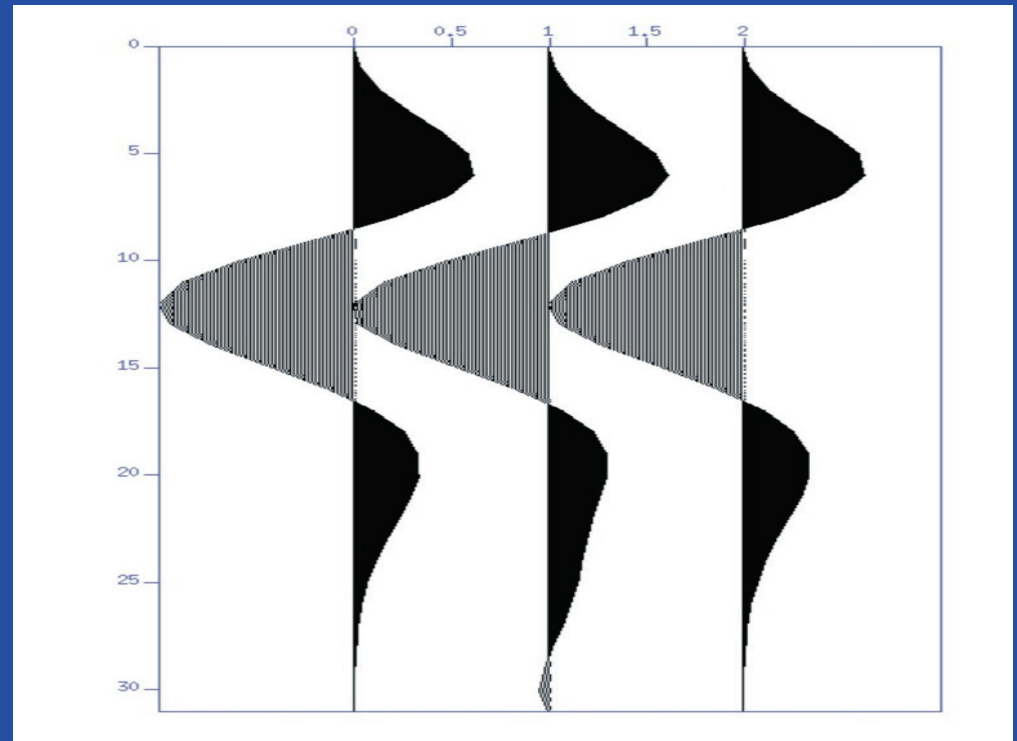
$$W(f) = \frac{Y(f)}{R(f)} \quad \left[W(\omega) = \frac{Y(\omega)}{R(\omega)} \right]$$

$$\hat{W}(f) = \frac{Y(f)}{R(f) + \varepsilon(f)} \quad \left[\hat{W}(\omega) = \frac{Y(\omega)}{R(\omega) + \varepsilon(\omega)} \right]$$

$$\hat{W}(f) \cong \frac{Y(f)}{R(f)} \left(1 - \frac{\varepsilon(f)}{R(f)} \right) \quad \left[\hat{W}(\omega) \cong \frac{Y(\omega)}{R(\omega)} \left(1 - \frac{\varepsilon(\omega)}{R(\omega)} \right) \right]$$

Log-Based Wavelet Estimates for P-wave Logs

- Wavelets derived from log-based wavelet estimation:
- $W(f) = Y(f) / R(f)$
- Left: actual wavelet
- Centre: Wavelet using “incorrect” log
- Right: Wavelet using “correct log”
- Error for centre wavelet = 3.58%
- Excellent consistency for these estimates

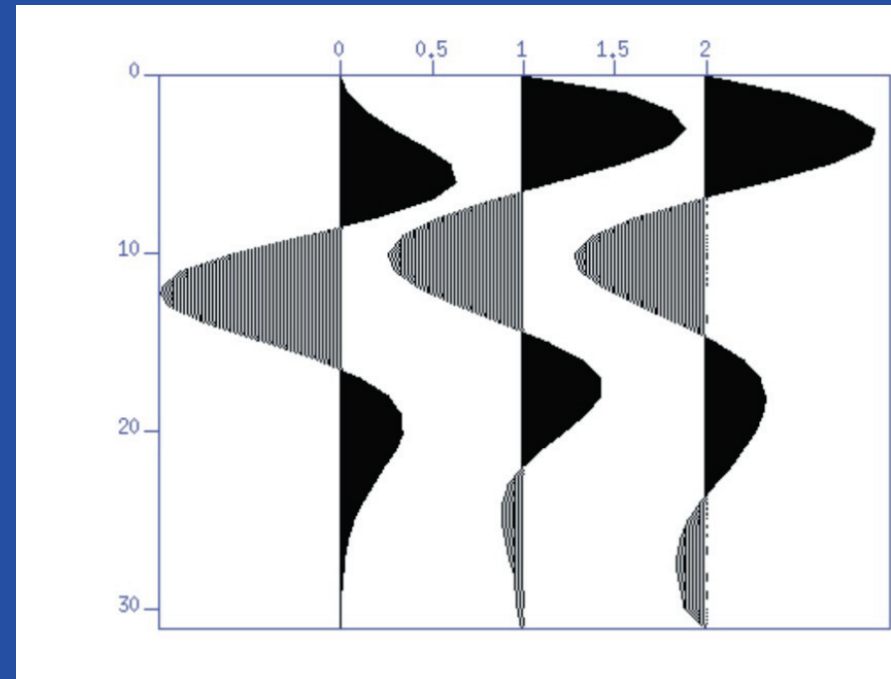


Minimum-phase Wavelet Estimation

- Two basic assumptions:
 - The wavelet is minimum phase, and hence can be derived from the log amplitude spectrum by Hilbert transform.
 - The reflectivity is random.

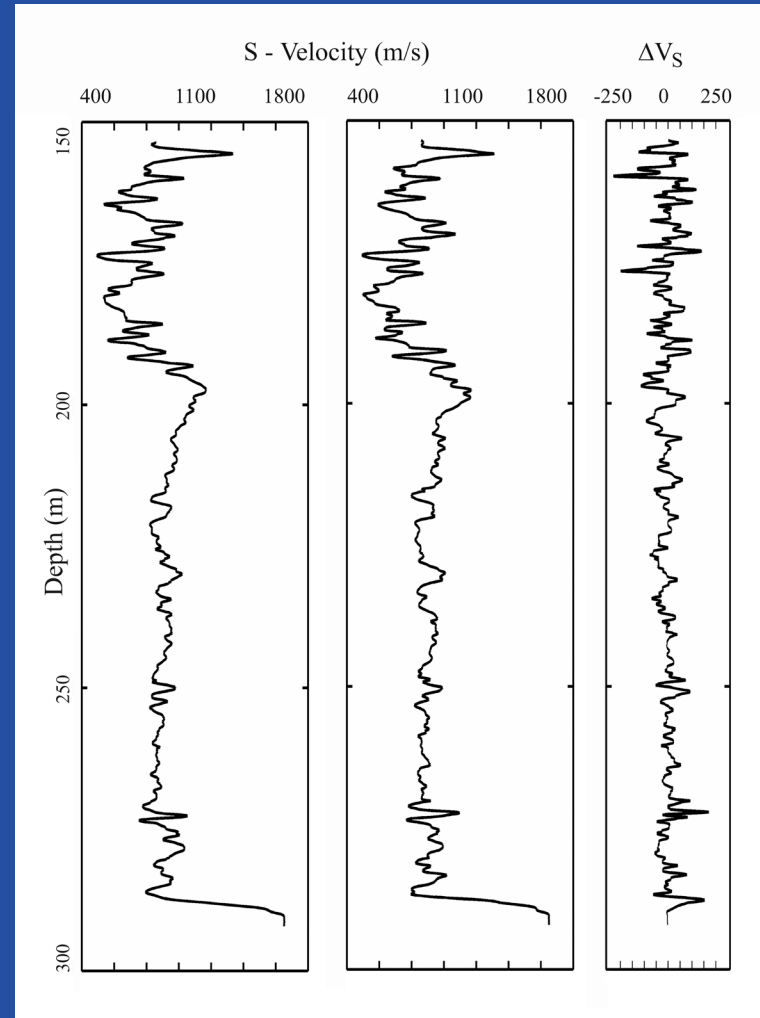
Minimum-phase Wavelet Estimates for P-wave Logs

- Wavelets derived from traces using minimum phase assumption and random reflectivity assumption.
- Fractional errors less than 3.50%
- Actual wavelet (left)
- Minimum phase wavelets from traces (middle, right)
- Errors about the same for log-based and statistical estimates.



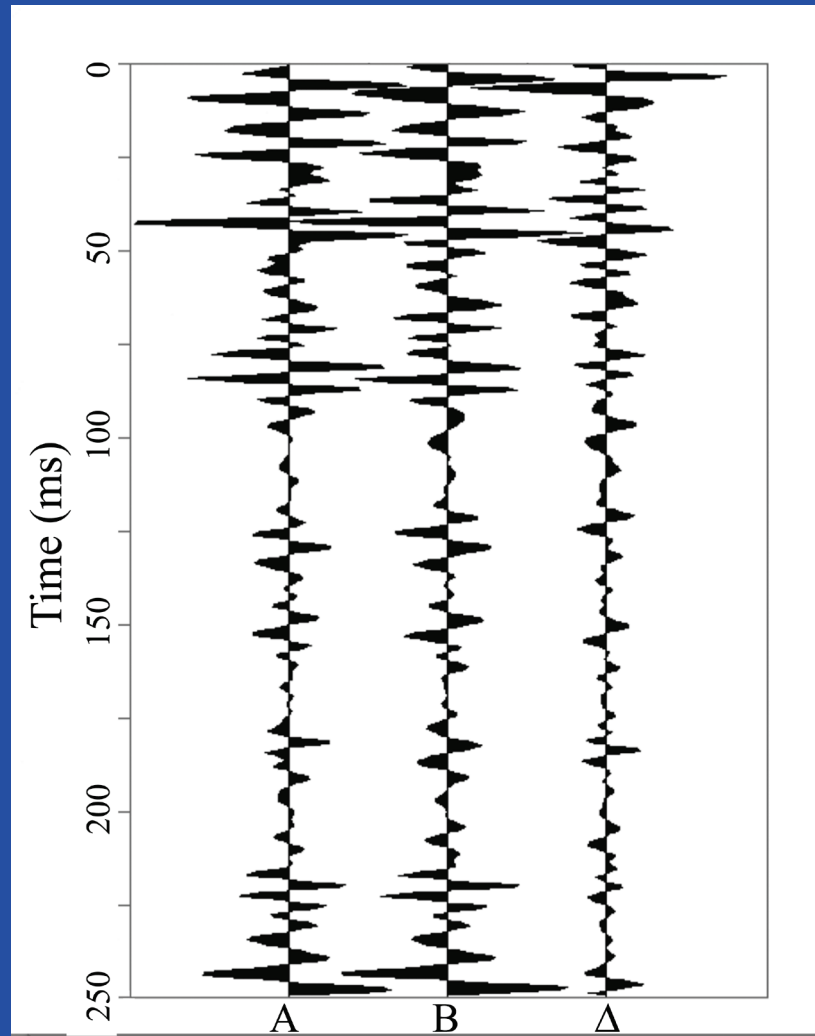
Shear-wave logs for Long Lake well (repeated log and original)

- Two shear-wave logs for Long Lake well between depths of 153.5-292m and the discrepancy log (on expanded scale).



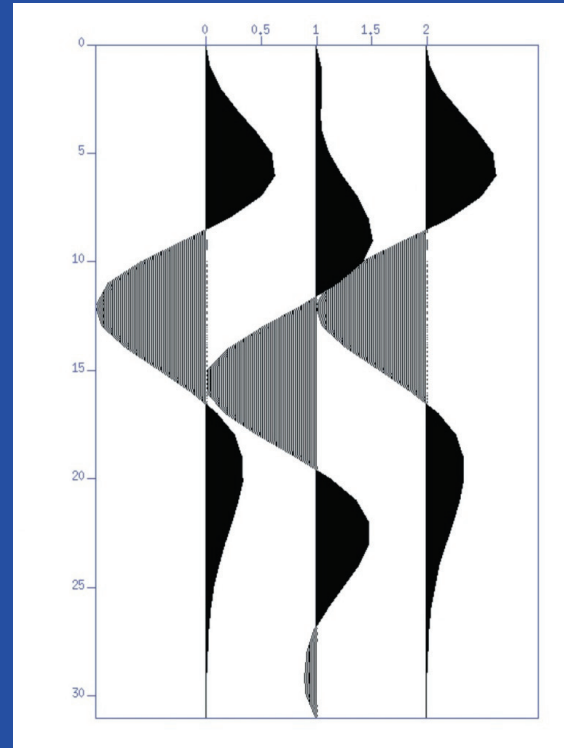
Synthetic Seismograms for Shear-wave sonic logs

- Synthetic seismogram using minimum phase equivalent of 150 Hz Ricker wavelet.
- Semblance for the two traces is 0.88
- Sample interval=0.5ms

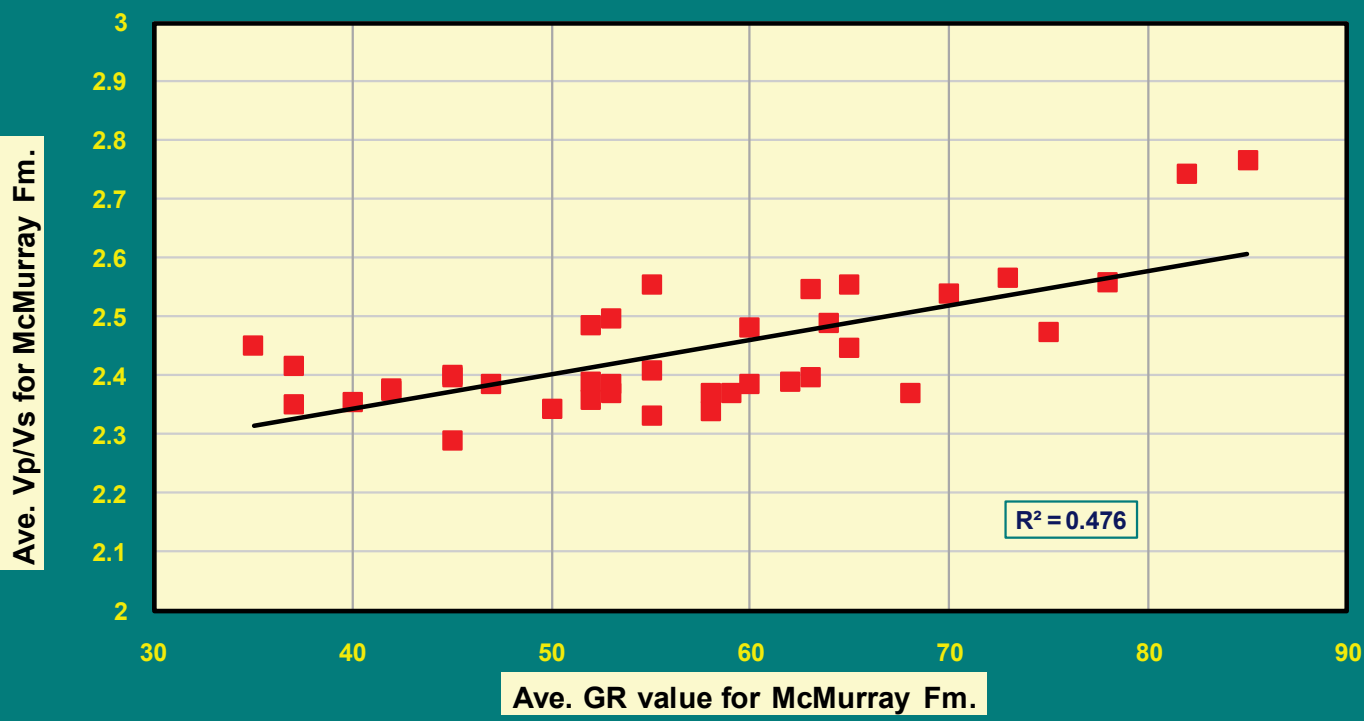


Log-Based Wavelet Estimates for Shear-wave Logs

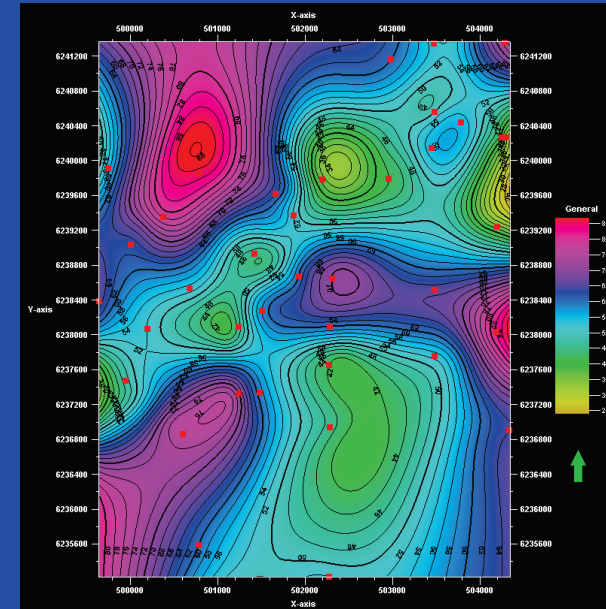
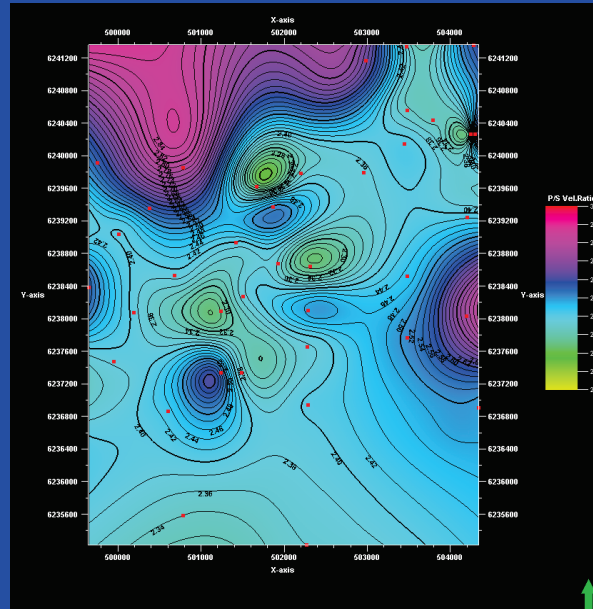
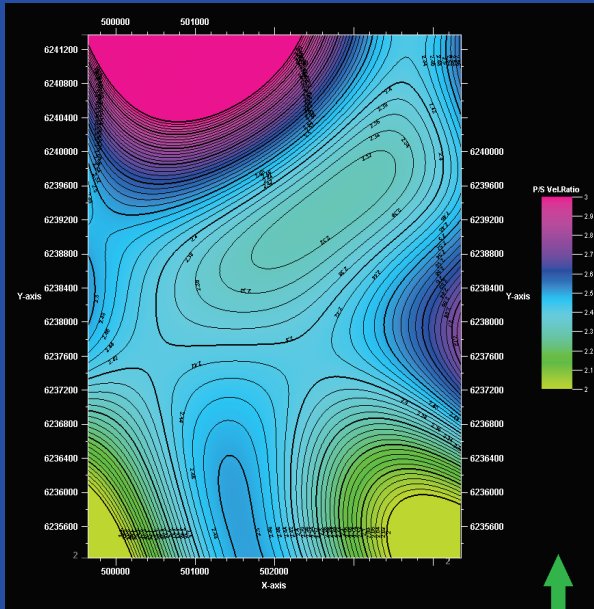
- Wavelets derived from log-based wavelet estimation:
- $W(f) = Y(f) / R(f)$
- Left: actual wavelet
- Centre: Wavelet using “incorrect” log
- Right: Wavelet using “correct log”
- Fractional error for middle wavelet = 3.58% (after time shifting)



Ave. Vp/Vs & Ave. GR Crossplot



Vp/Vs Ratio Map for the McMurray Formation using original dipole sonic logs (left), repeated dipole sonic logs (middle) and gamma ray logs (right).



Conclusions

- Repeated dipole sonic measurements allow us to evaluate reliability.
- For our data analysis, the repeatability of P-wave information appears to be excellent whereas repeatability of S-wave information appears to be very good.
- Log-based wavelet estimation shows excellent repeatability for P-wave information and very good repeatability for S-waves.
- Log-based wavelet estimates and statistical wavelet estimates show similar reliability.
- The VP/VS maps show some variability for logging runs with generally good agreement with gamma ray log maps.
- Given the small incremental costs, repeated dipole sonic measurements are worthwhile.

Acknowledgements

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