



# LSPSM / inversion for pre- and poststack time lapse studies

2012 CREWES  
Sponsors' Meeting

Naser Yousefzadeh\*, John Bancroft

# Outline

- I. Review on Least Squares PreStack Kirchhoff Migration (LSPSM)
- II. Review on time lapse seismic/ challenges
- III. Separate inversion
  - Final section
  - Prestack data
- IV. Joint inversion
  1. Multiple Image Joint Inversion
  2. Image Difference Joint Inversion
- V. Summary

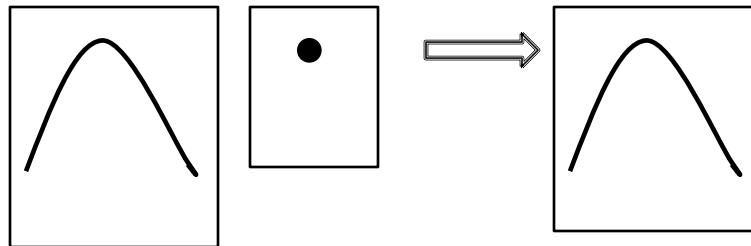
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# Kirchhoff Modeling/Migration

- Modeling:

$$Gm = d$$



$G$  : Kirchhoff  
forward  
operator,

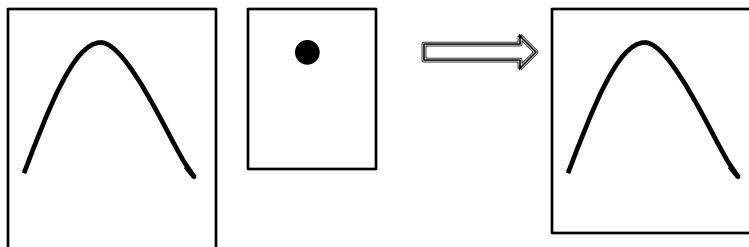
$m$  : Reflectivity,

$d$  : Real data.

# Kirchhoff Modeling/Migration

- Modeling:

$$Gm = d$$



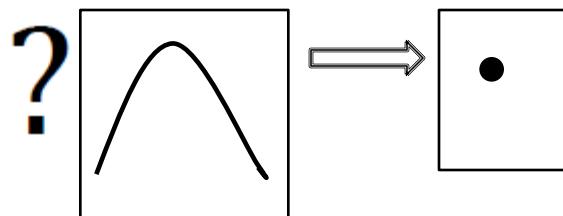
$G$  : Kirchhoff forward operator,

$m$  : Reflectivity,

$d$  : Real data.

- Inversion:

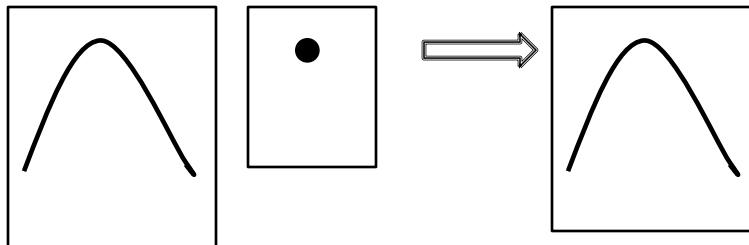
$$G^{-1}d = m$$



# Kirchhoff Modeling/Migration

- Modeling:

$$Gm = d$$



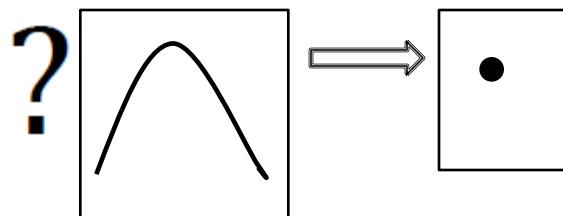
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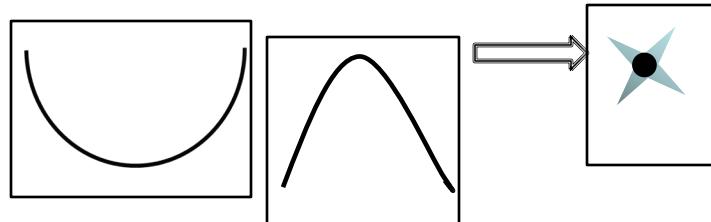
- Inversion:

$$G^{-1}d = m$$



- Migration:

$$G^T d = \hat{m}$$



# LSPSM, how?

$$Gm = d \quad (\text{Modeling})$$

$$G^T G m = G^T d$$

$$m = (G^T G)^{-1} G^T d \quad (\text{LSPSM})$$

# LSPSM, how?

$$Gm = d \quad (\text{Modeling})$$

$$G^T G m = G^T d$$

$$m = (G^T G)^{-1} G^T d \quad (\text{LSPSM})$$

- Minimizing a general cost function:

$$J(m) = \|Gm - d\|^2 + \mu^2 \mathcal{R}(m)$$


Misfit term

$\mathcal{R}$  : Regularization term,  
 $\mu$  : Trade-off parameter

# LSPSM, how?

$$Gm = d$$

$$G^T G m = G^T d$$

$$m = (G^T G)^{-1} G^T d$$

**Simplest solution: Damped LSM:**

$$m_{DLS} = (G^T G + \mu^2 I)^{-1} G^T d$$

# Outline

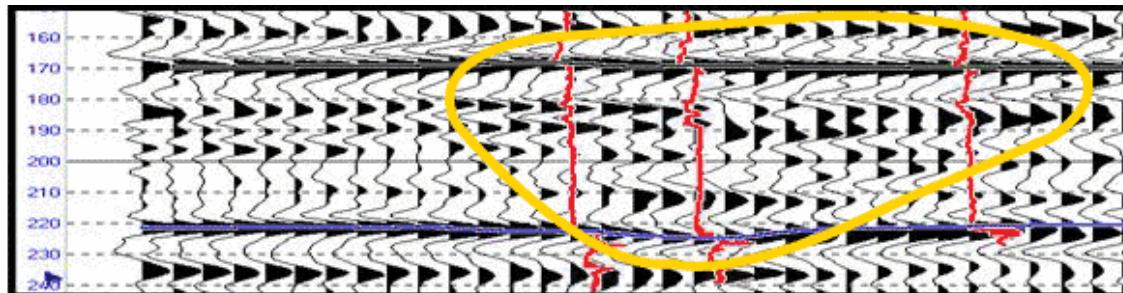
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# Time lapse seismic

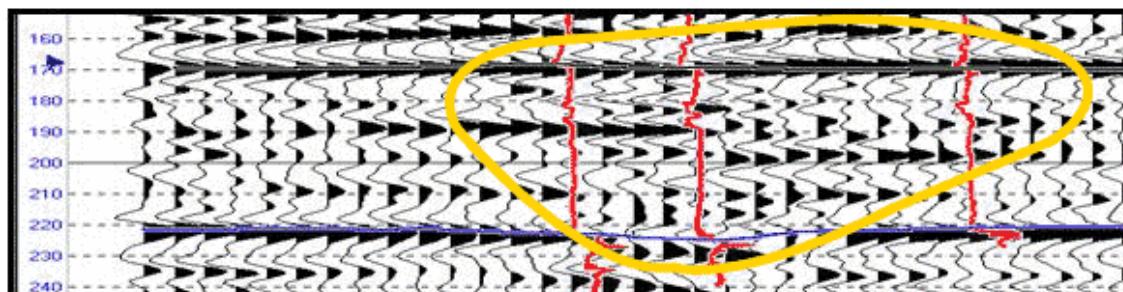
- Time lapse study of seismic data includes recording and analysing a secondary seismic survey after a period of time in order to detect the subtle changes in the physical properties of the hydrocarbon reservoirs.
- These changes can be due to changes in the fluid (oil, gas, water, steam, etc ) saturation.

# Time lapse seismic terminology

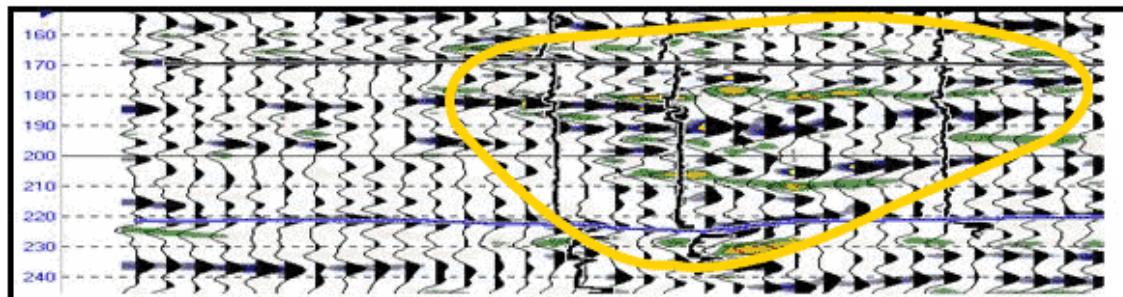
- Baseline survey



- Monitor survey



- Time lapse image



# Time lapse seismic challenges

- All acquisition geometries, instruments, environmental noises, near surface effects, and processing flows must be equivalent,
- Then differences in the migration images will be due to changes in the physical properties of the reservoir rocks/ fluids.
- Different acquisition geometries produce different patterns of the acquisition footprints.
- Resulting time lapse image may show the difference in artifacts, **not** changes in the model parameters.

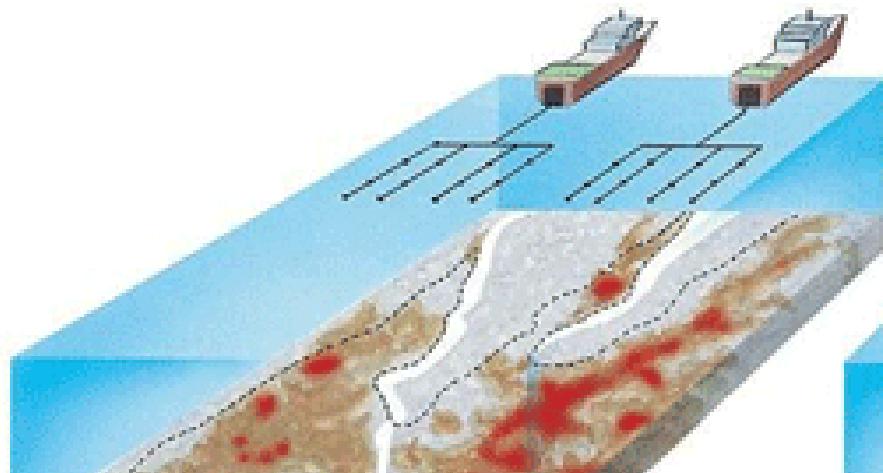
# Time lapse seismic challenges

- Repeating same geometry for baseline and monitor surveys is not always feasible:
  - New construction in land (& marine)
  - Marine streamers have feathering.
- OBC in marine , Cemented receivers in land:
  - effect of losing receivers by time.

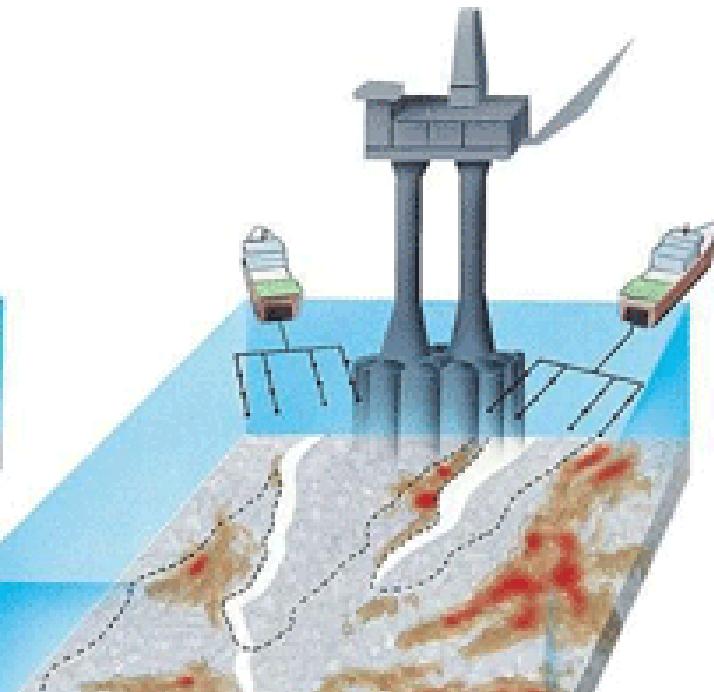
# Time lapse seismic challenges

May use solid streamers, Q technology (Western Geophysical).

It is not always possible.



**Baseline**



**Monitor**

# LSPSM/inversion of time lapse data

**We are reducing the effects of different acquisition geometries**

**by**

# LSPSM/inversion of time lapse data

**III. Separate LSPSM/inversion of baseline and monitor surveys data.**

or

**IV. Joint LSPSM/inversion of baseline and monitor surveys data.**

# LSPSM/inversion of time lapse data

**III. Separate LSPSM/inversion of baseline and monitor surveys data is used to**

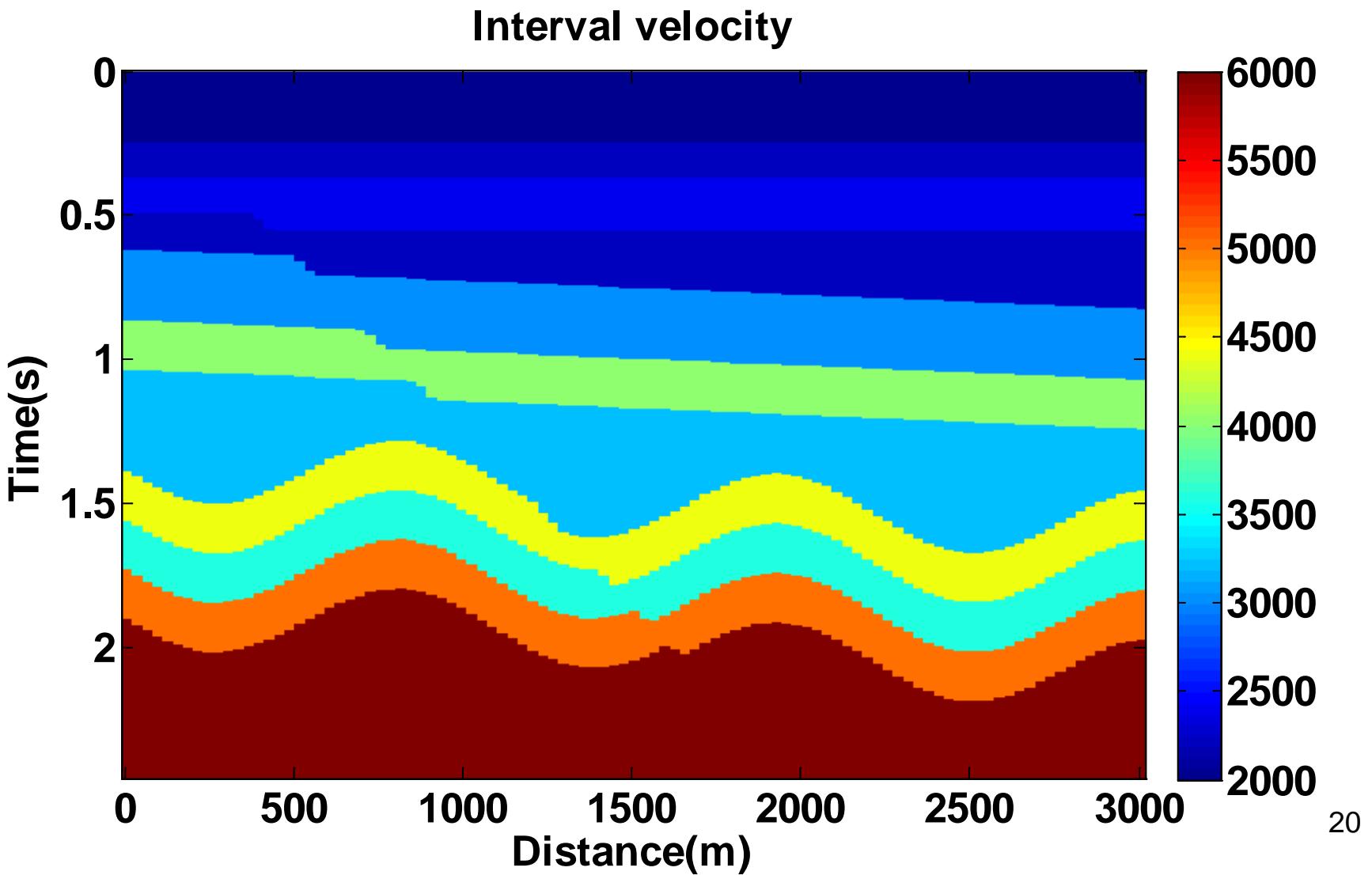
- 1) Remove the effect of having different acquisition geometries**
- 2) Remove the effect of losing receivers in OBC**
- 3) Increase the resolution of time lapse image**

# LSPSM/inversion of time lapse data

## III. Separate LSPSM/inversion of baseline and monitor surveys data is used to

- 1) Remove the effect of having different acquisition geometries
- 2) Remove the effect of losing receivers in OBC
- 3) Increase the resolution of time lapse image

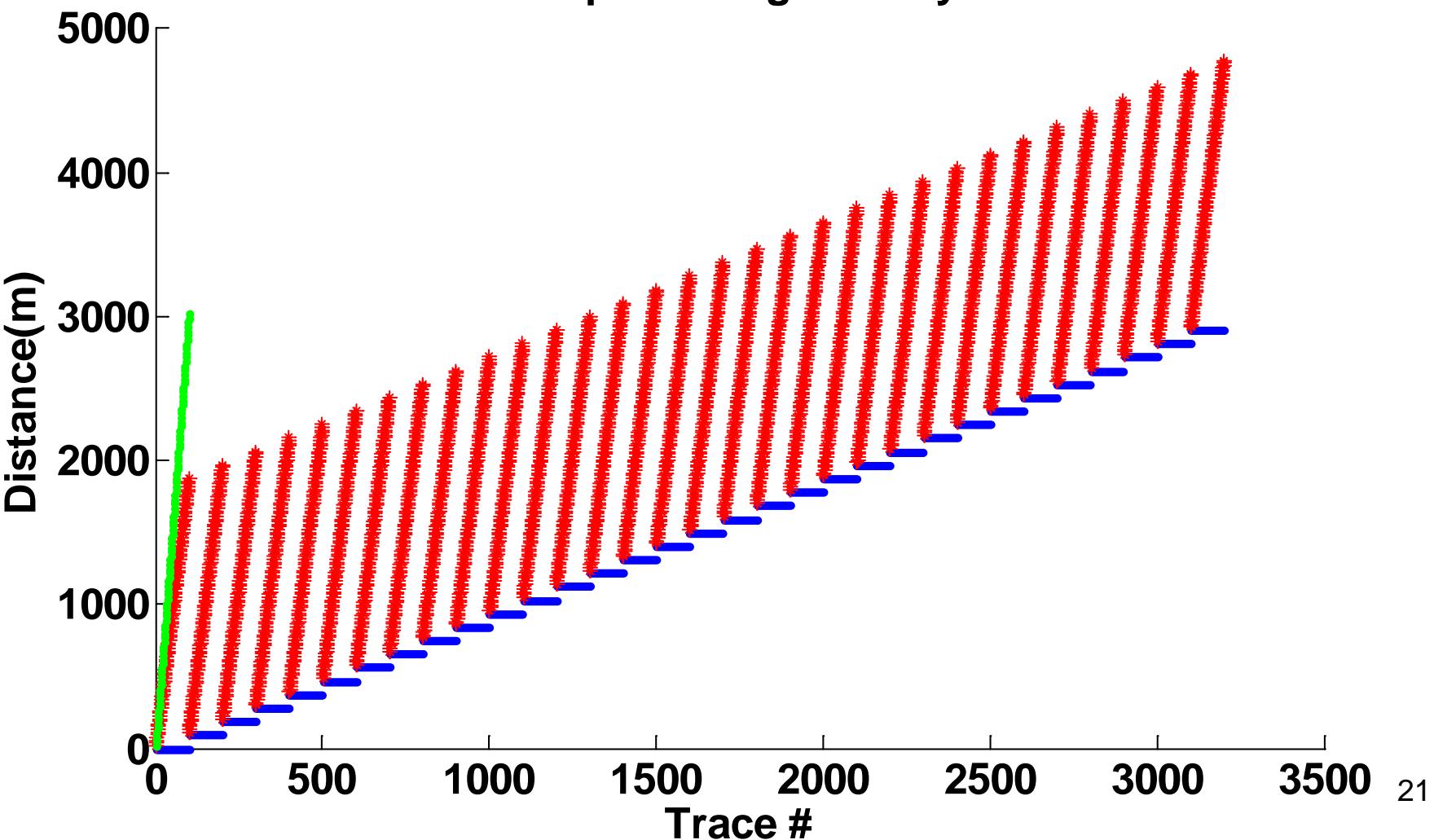
# Velocity model



# Baseline Survey

32 S, 100R/S, SI=100m, RI=18m

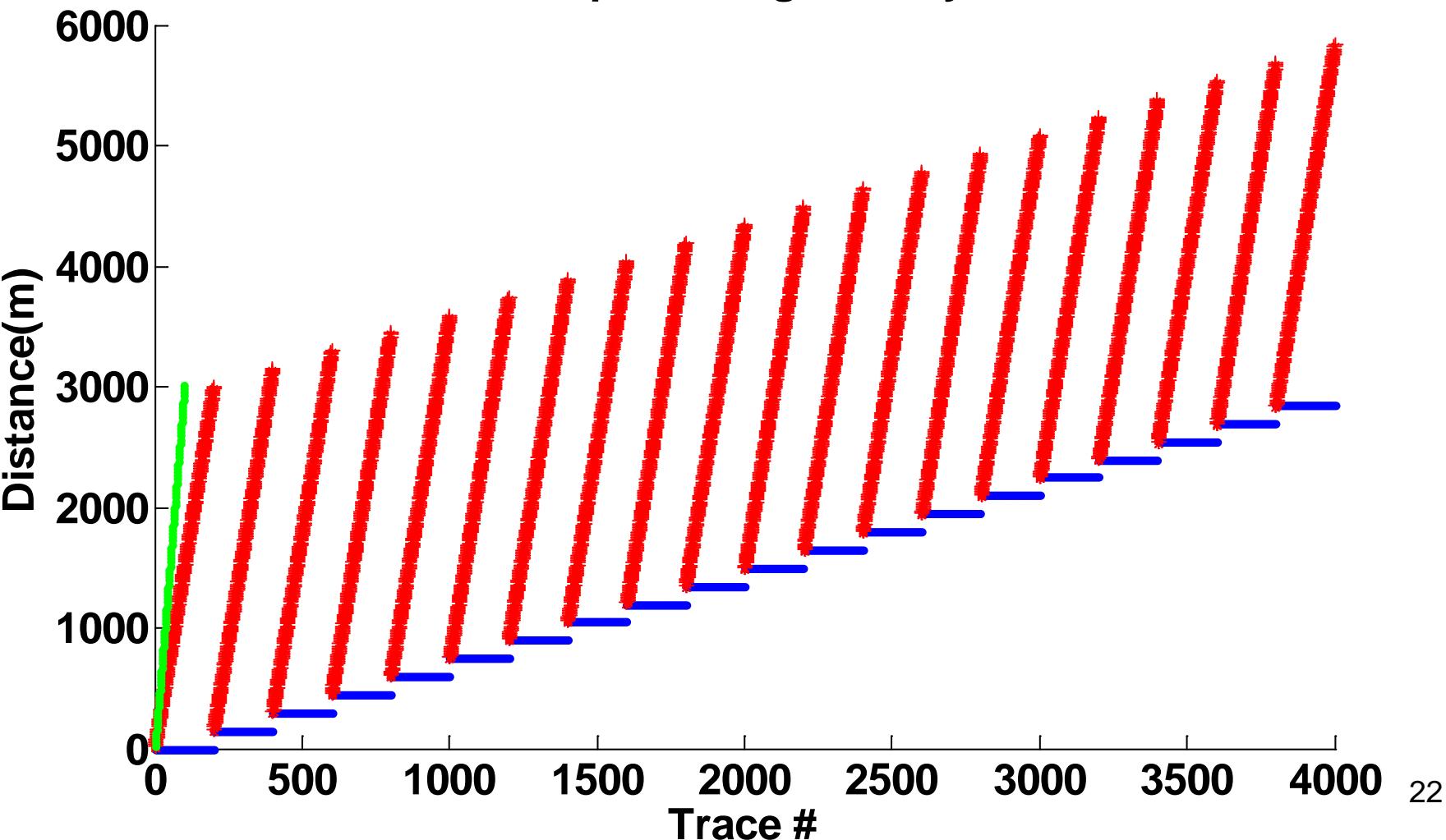
Acquisition geometry



# Monitor Survey

20S, 200R/S, SI=150m, RI=15m

Acquisition geometry

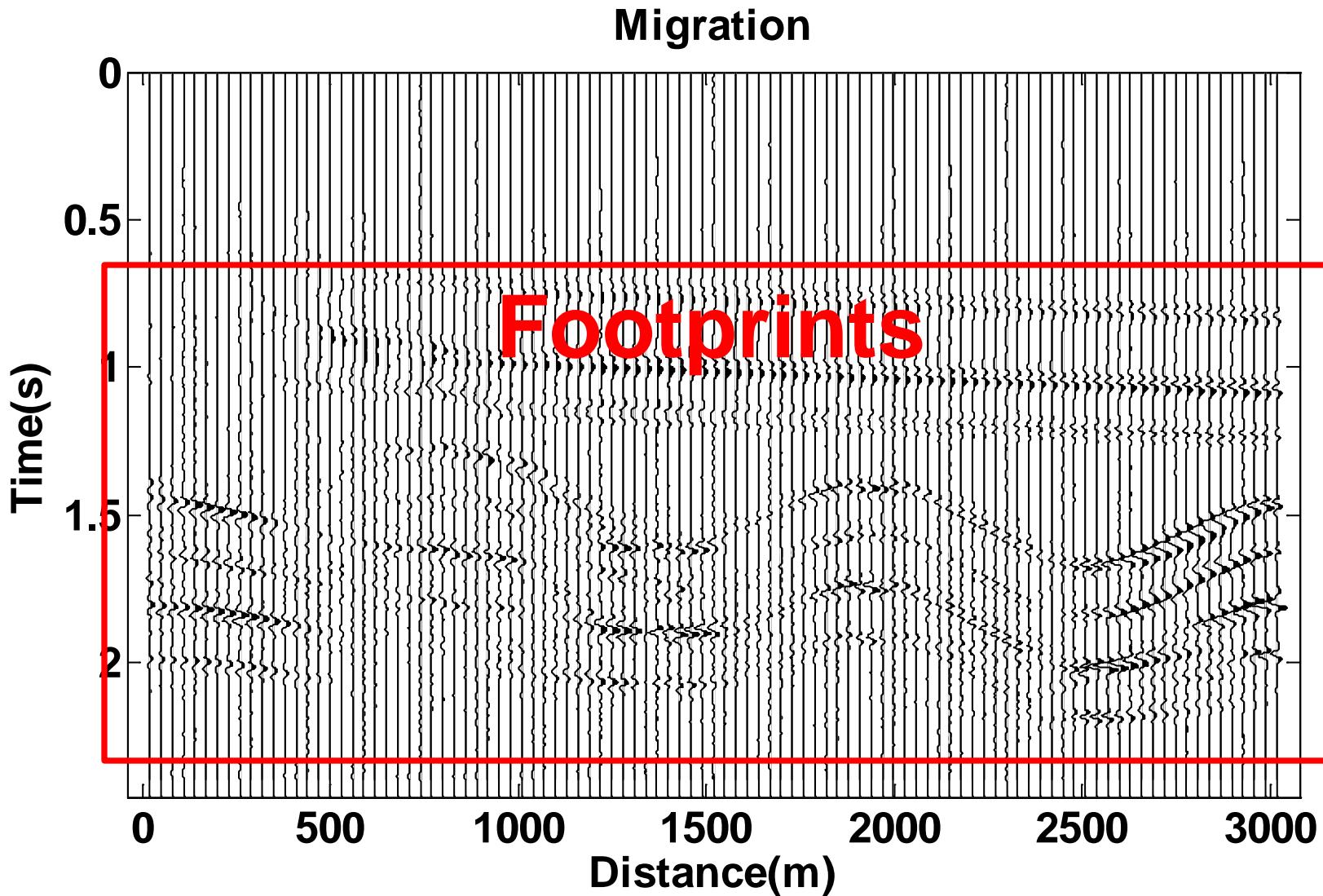


# Time lapse seismic challenges

- Both surveys are dense and regular,

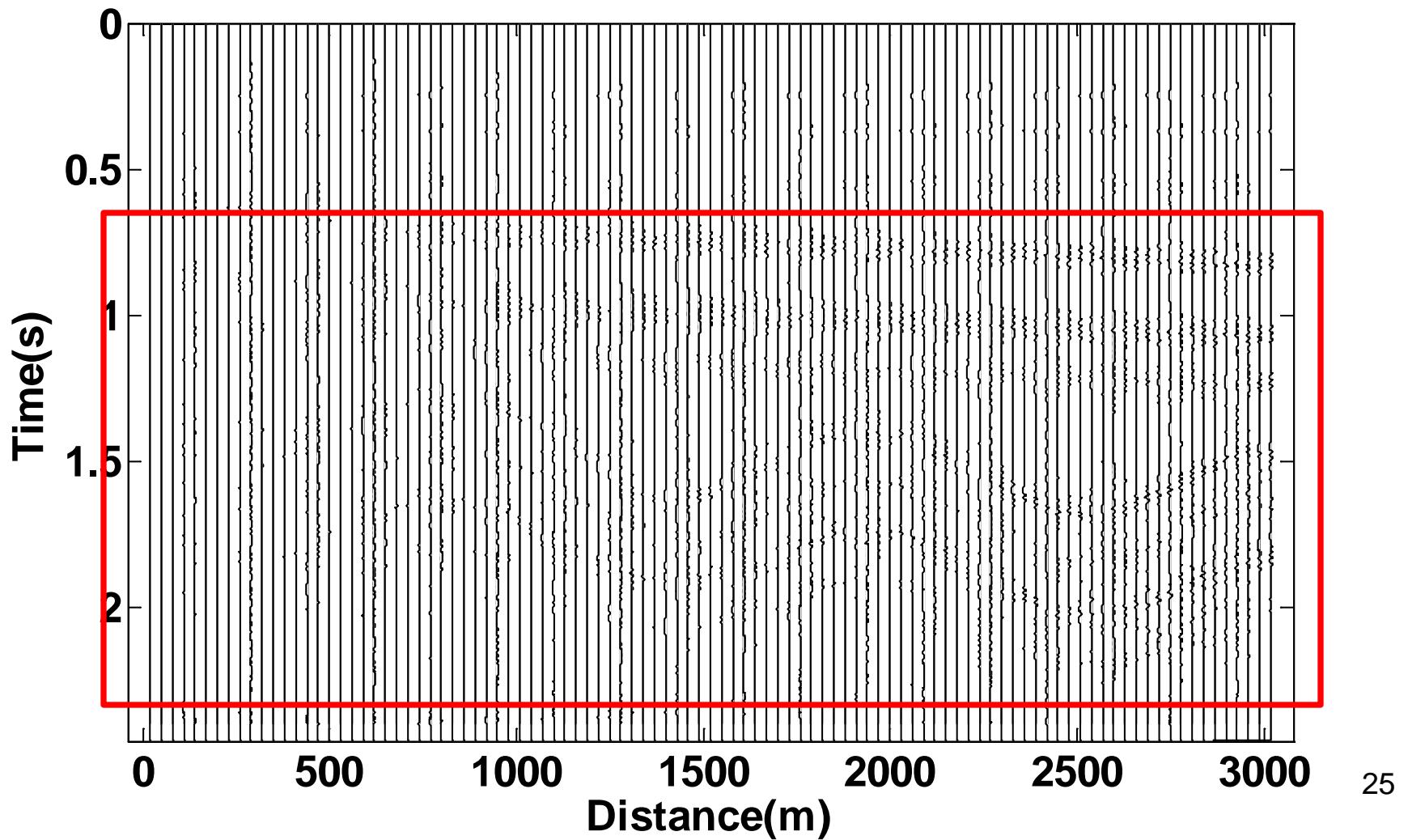
**BUT**

# Migration time lapse



# LSPSM time lapse

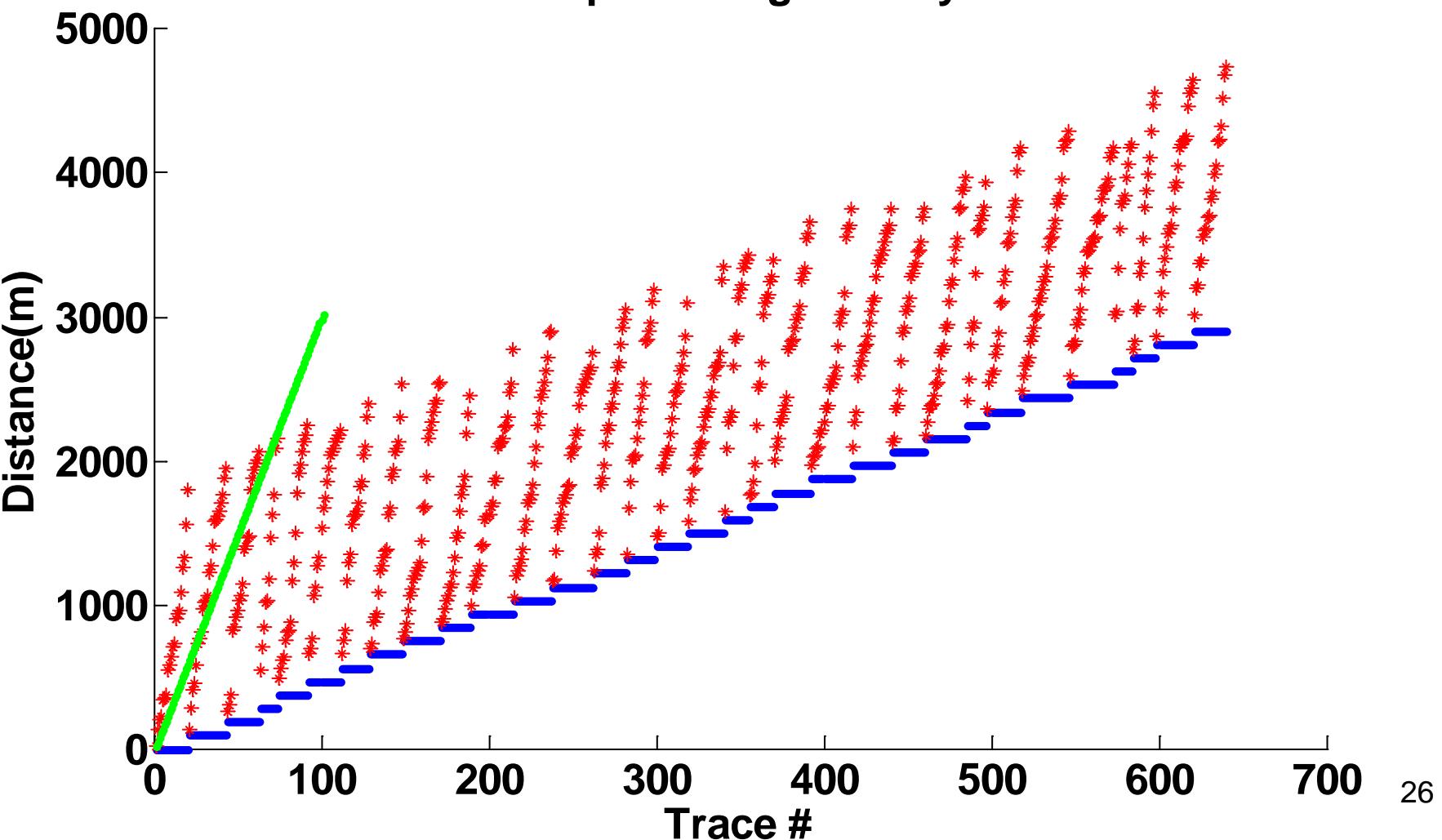
Inversion LSCG



# Baseline Survey

32S, 100R/S, SI=100m, RI=18m, 80% decimation

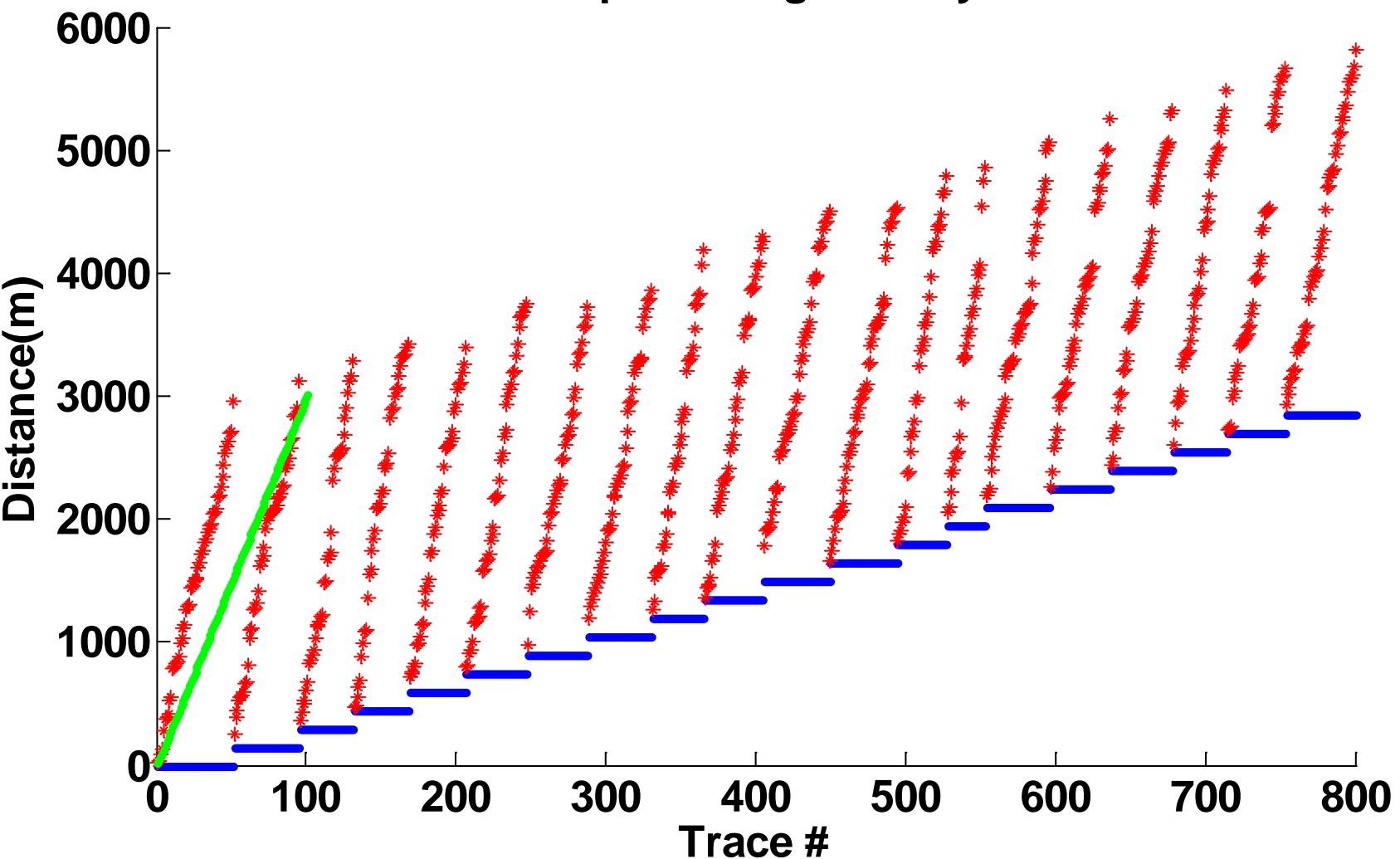
Acquisition geometry



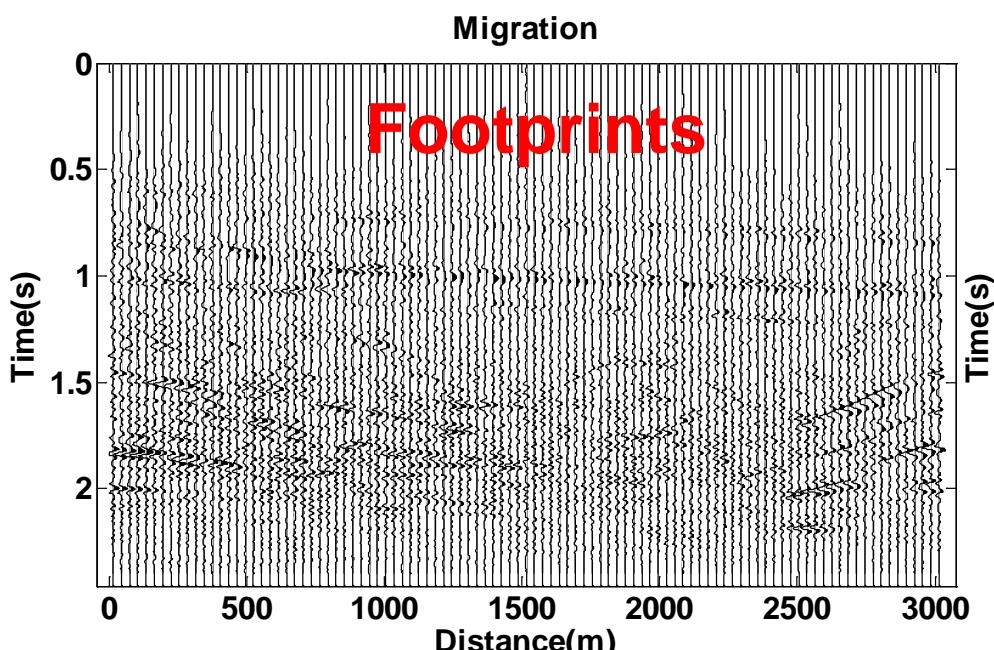
# Monitor Survey

20S, 200R/S, SI=150m, RI=15m, 80% decimation

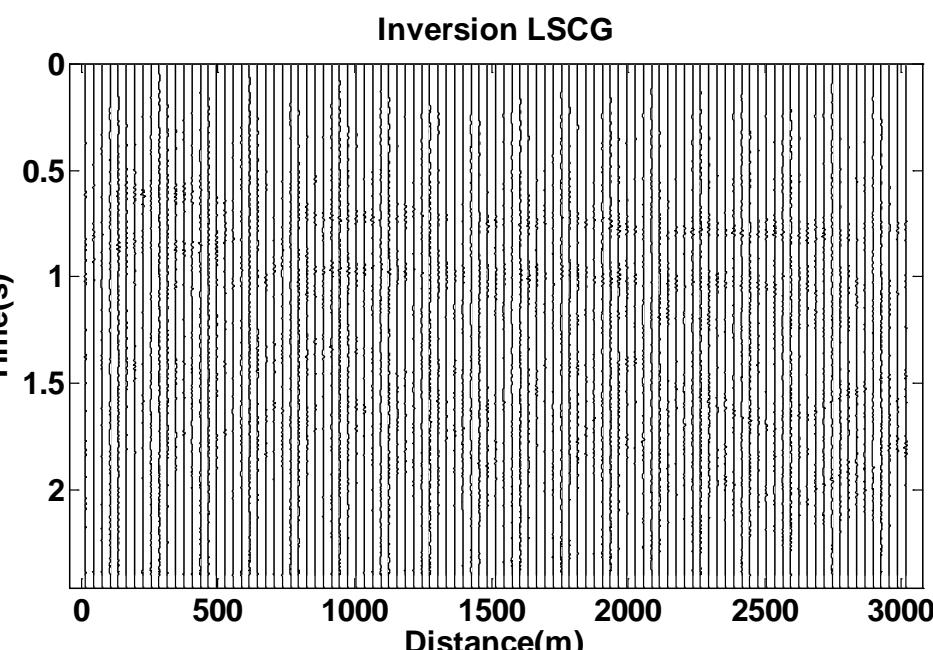
Acquisition geometry



# Time lapse images

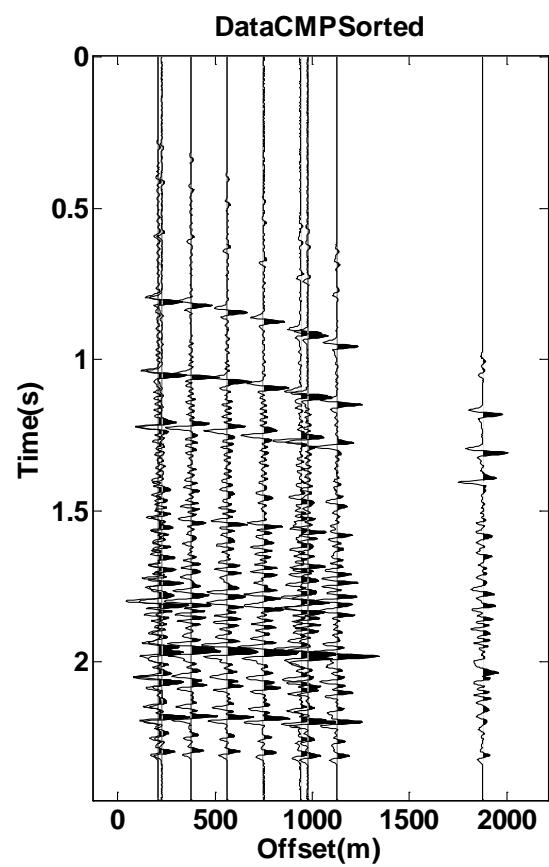


**Migration**

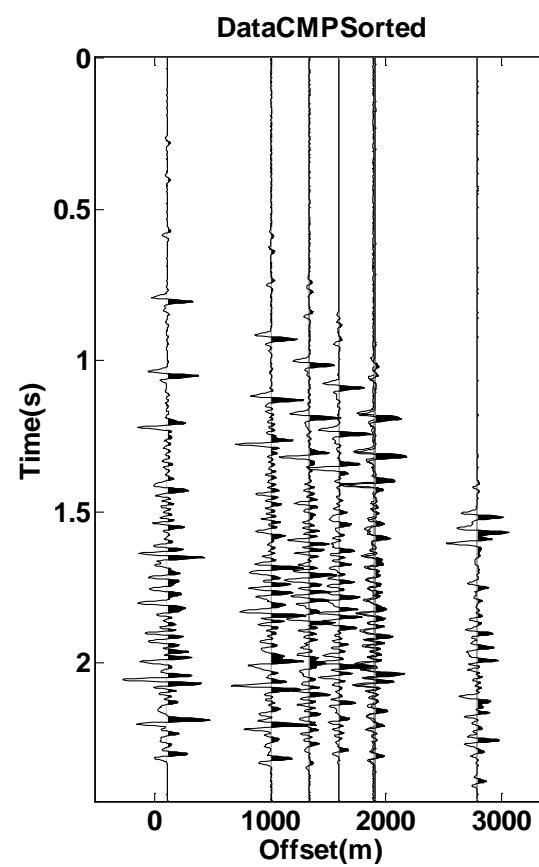


**LSPSM**

# Prestack time lapse, Decimated data

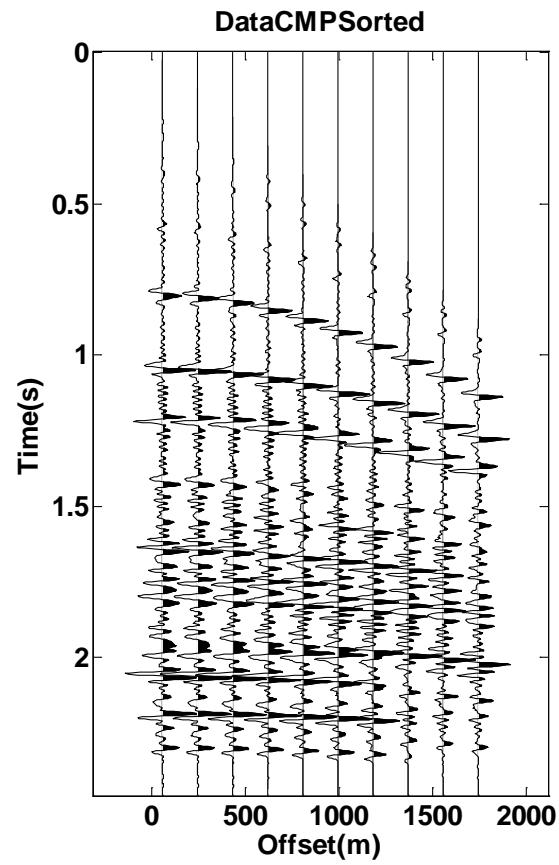


Baseline

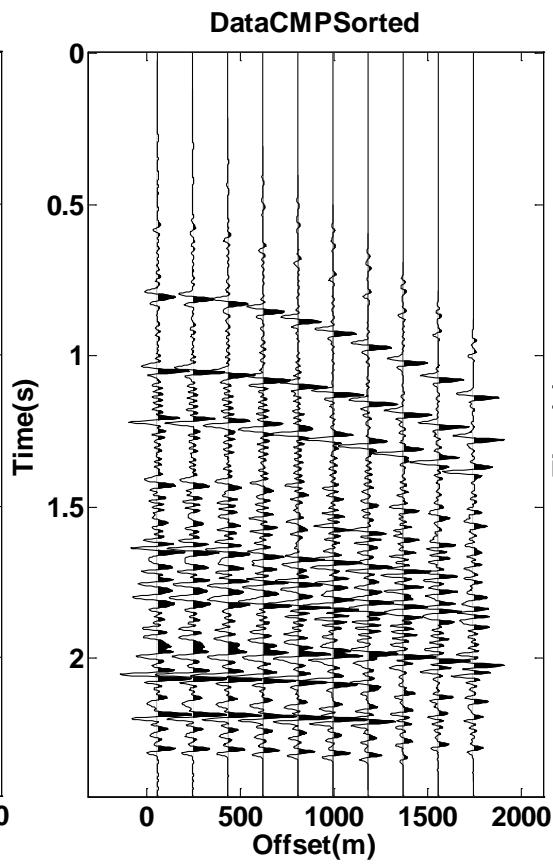


Monitor

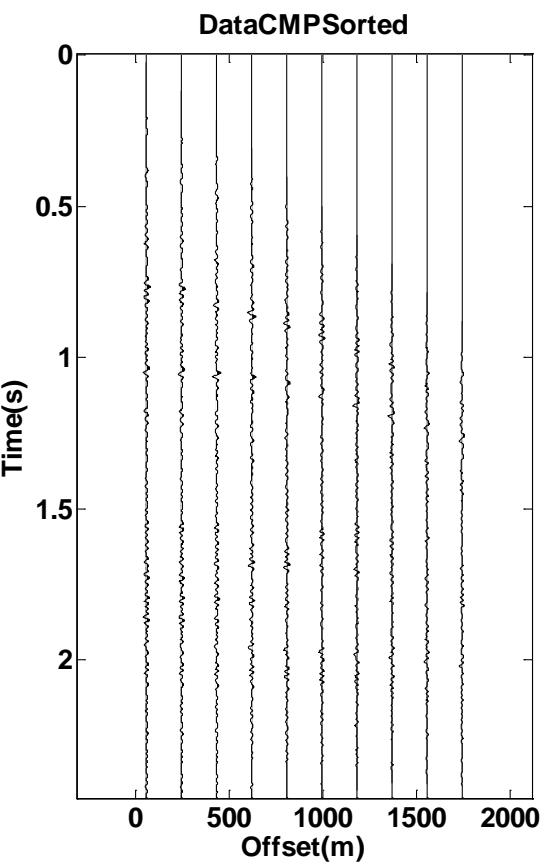
# Prestack time lapse, Reconstructed Data



**Baseline**



**Monitor**



**Difference**

# LSPSM/inversion of time lapse data

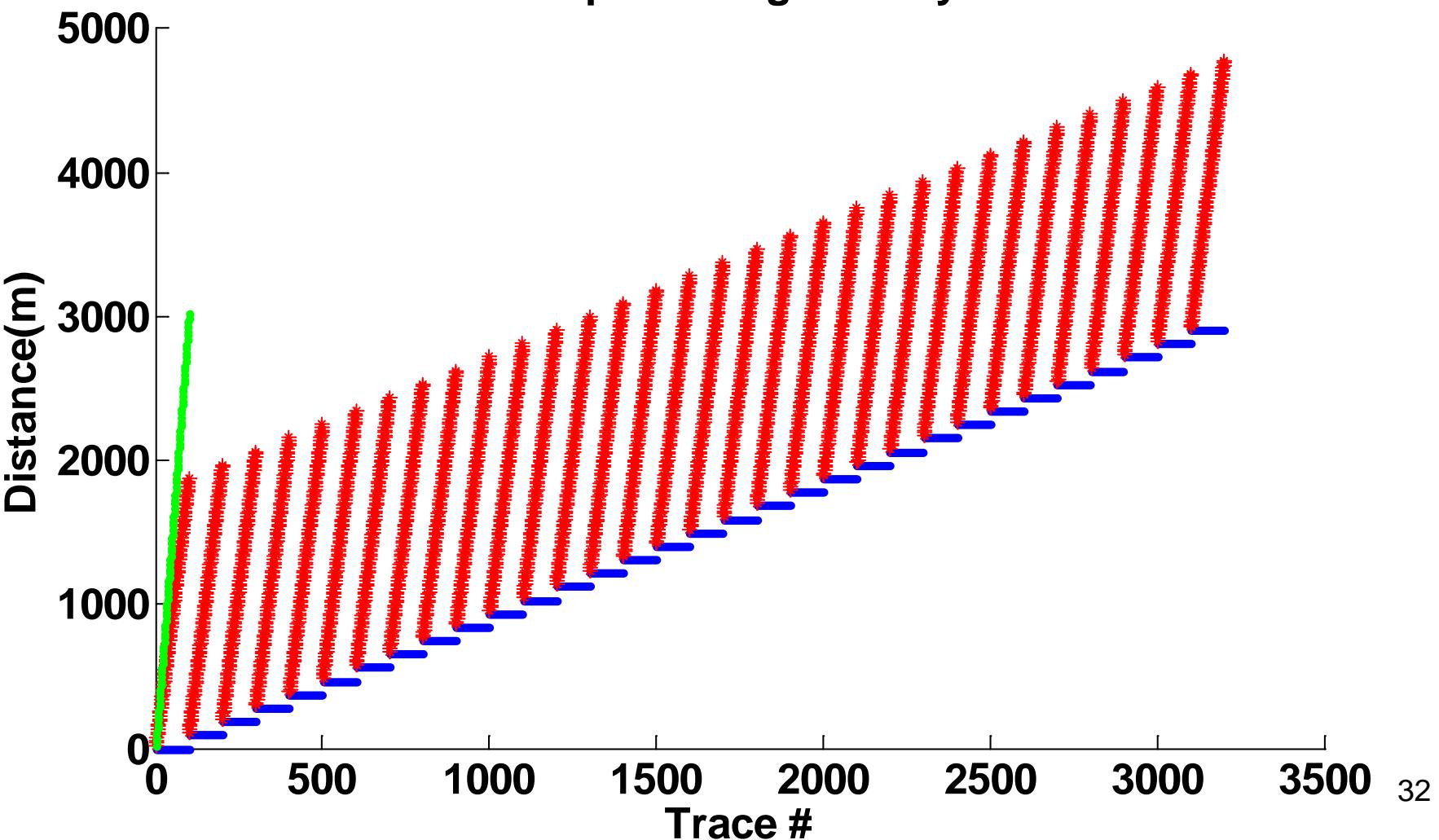
## **III. Separate LSPSM/inversion of baseline and monitor surveys data is used to**

- 1) Remove the effect of having different acquisition geometries
- 2) Remove the effect of losing receivers in OBC
- 3) Increase the resolution of time lapse image

# Baseline Survey

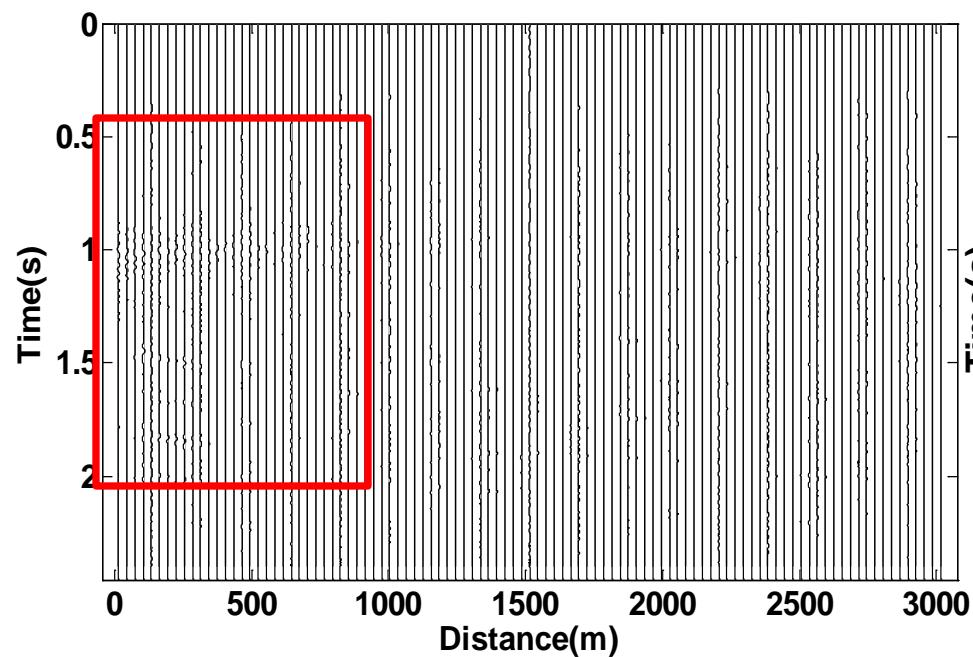
32S, 100R/S, SI=100m, RI=18m

Acquisition geometry

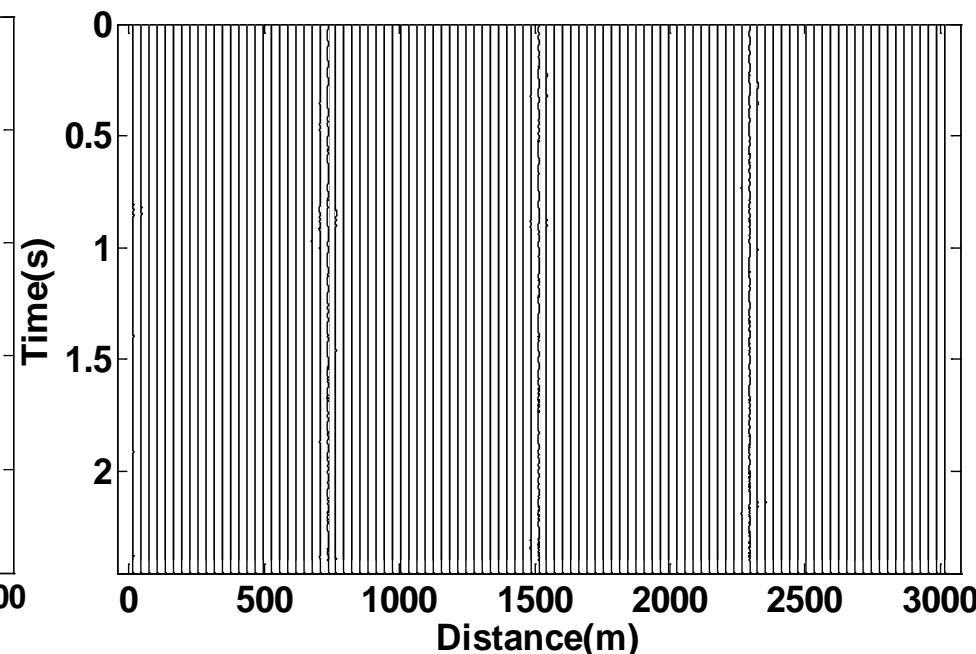


# Time lapse, effect of loosing receivers

Losing 50% of data  
Migration                    LSPSM



Footprints

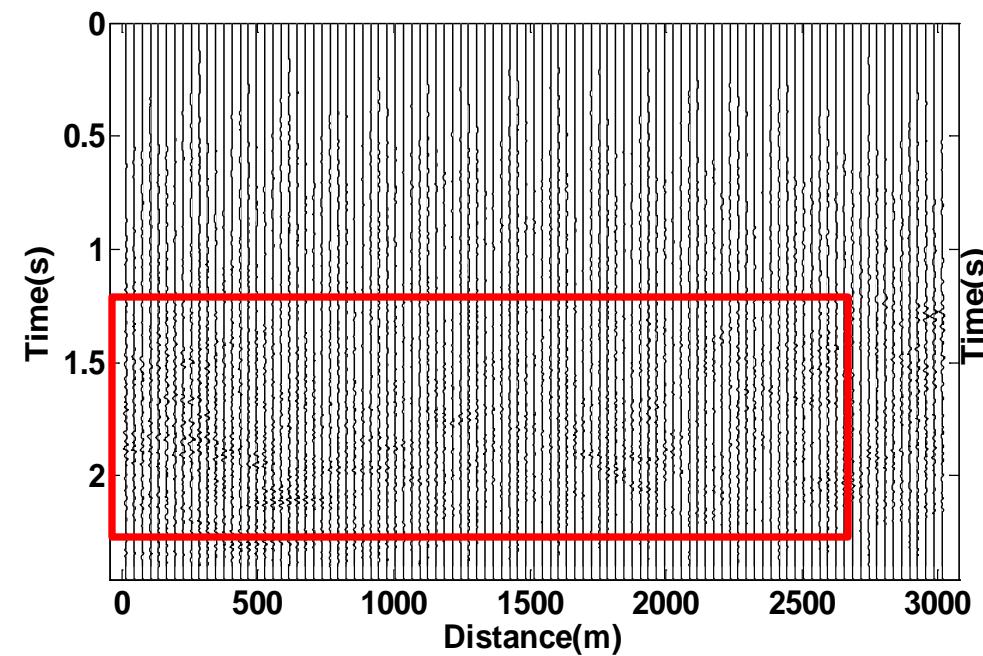


# Time lapse, effect of loosing receivers

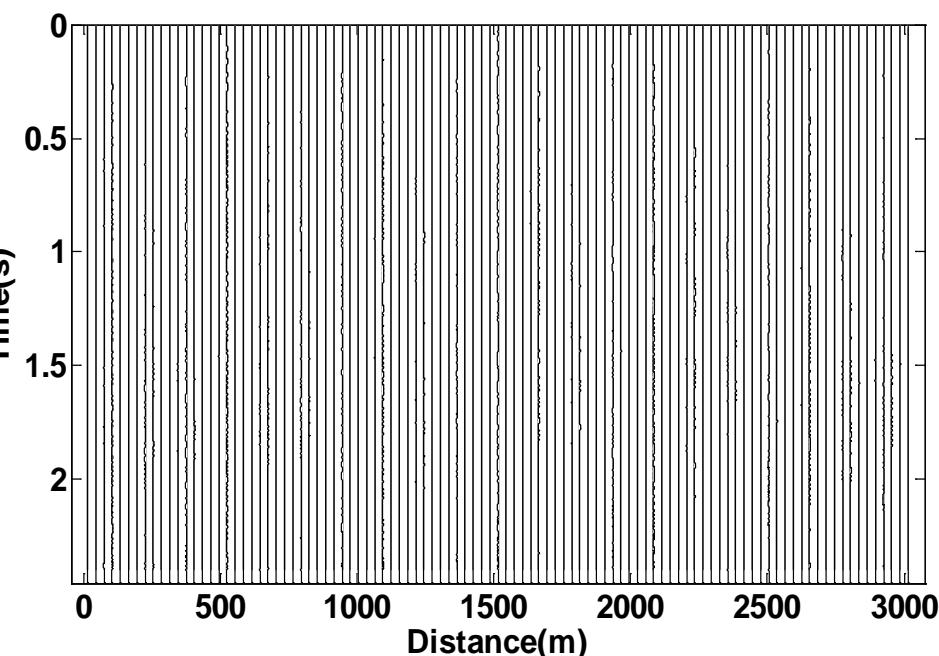
30% of data

Migration

LSPSM



Footprints

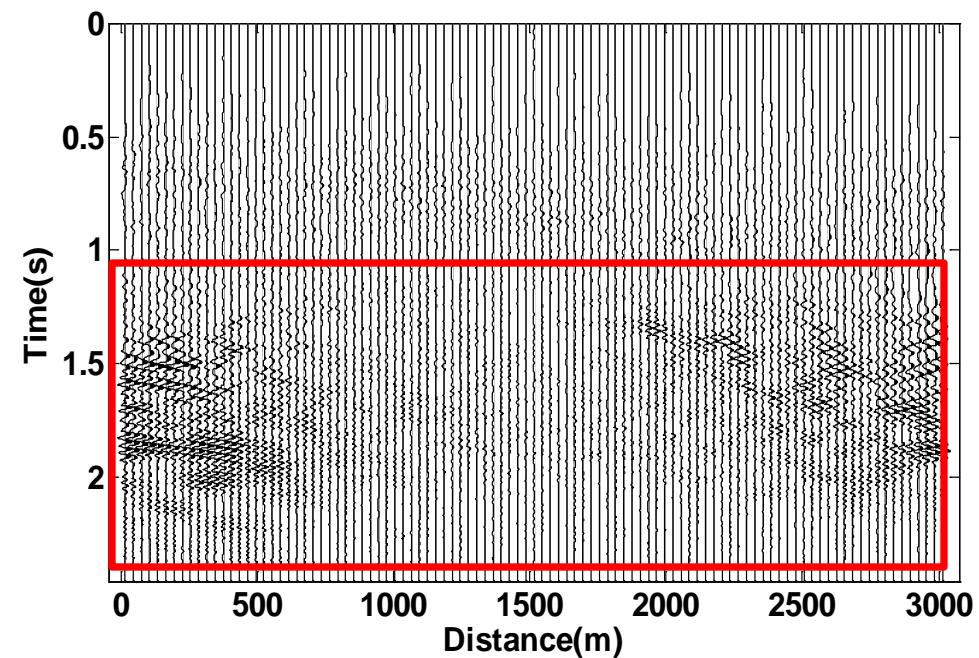


# Time lapse, effect of loosing receivers

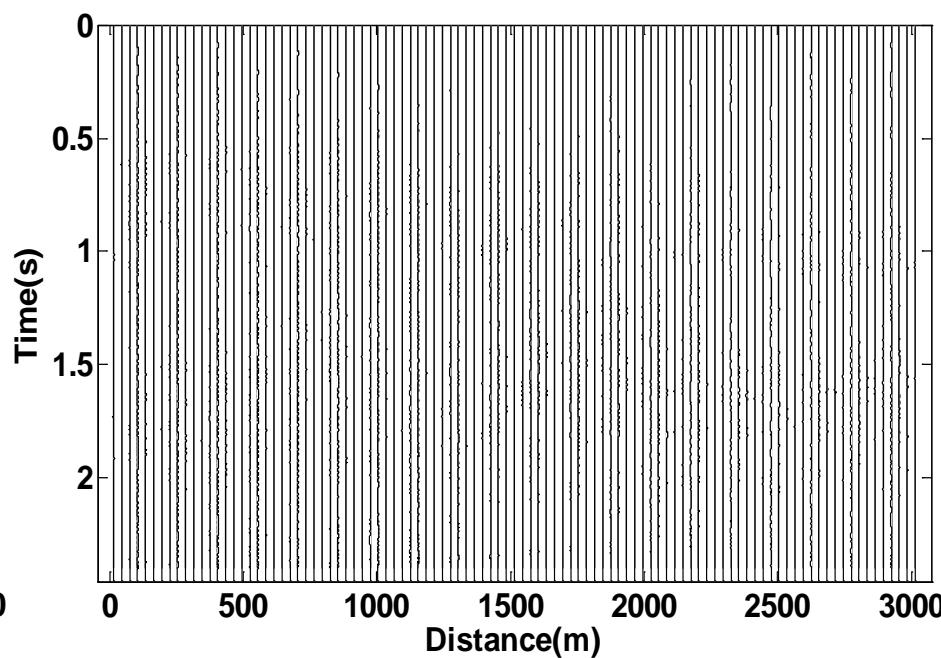
20% of data

Migration

LSPSM



Footprints

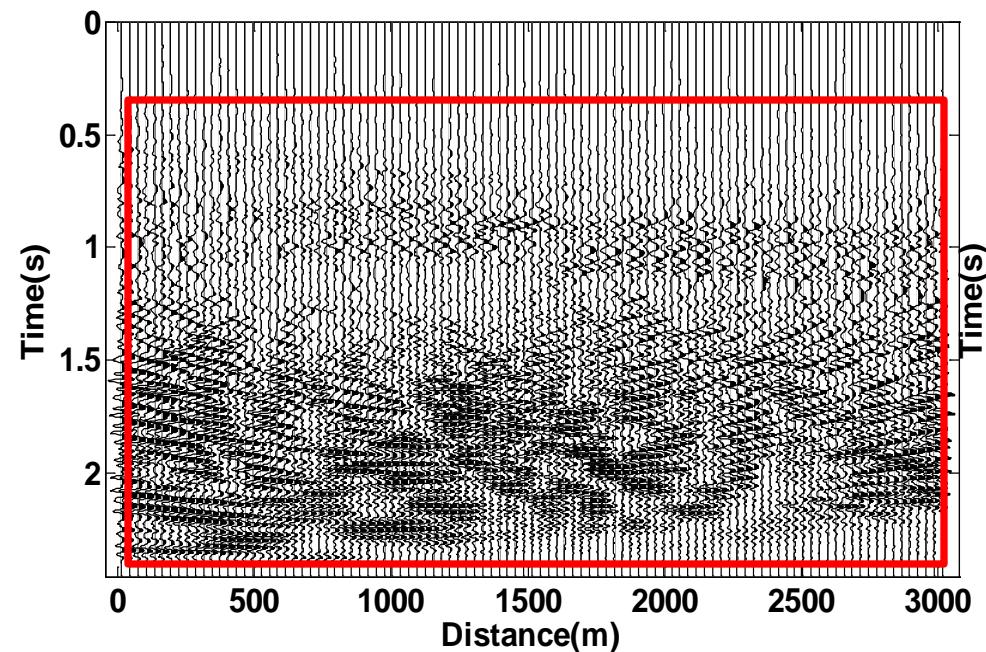


# Time lapse, effect of loosing receivers

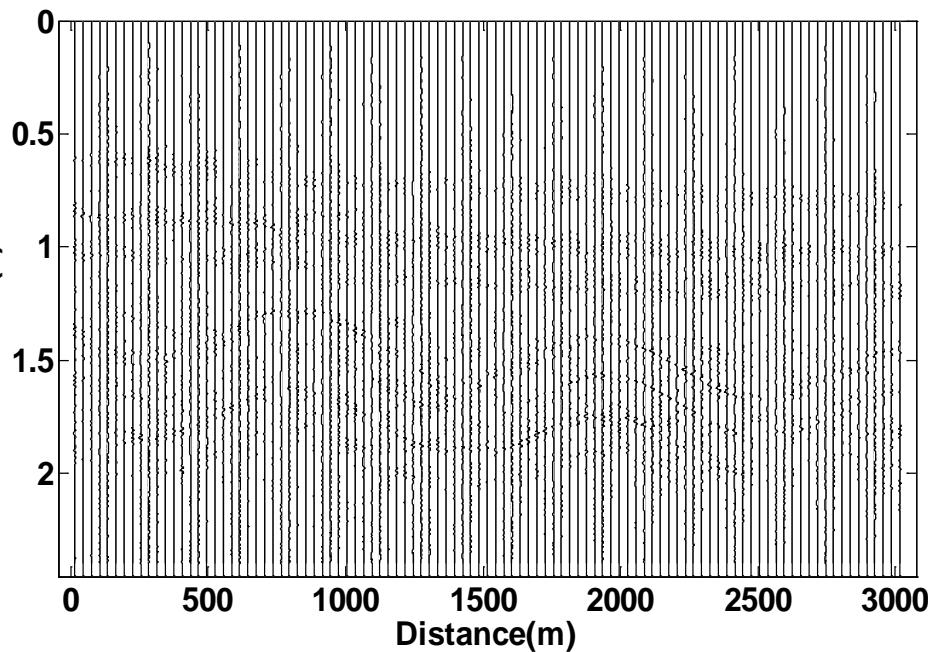
10% of data

Migration

LSPSM

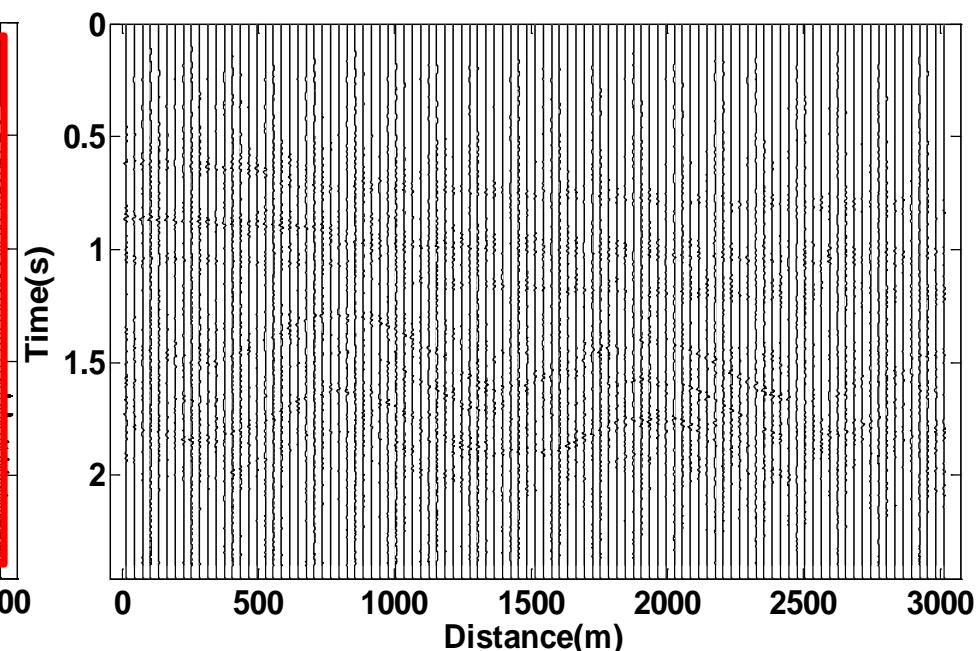
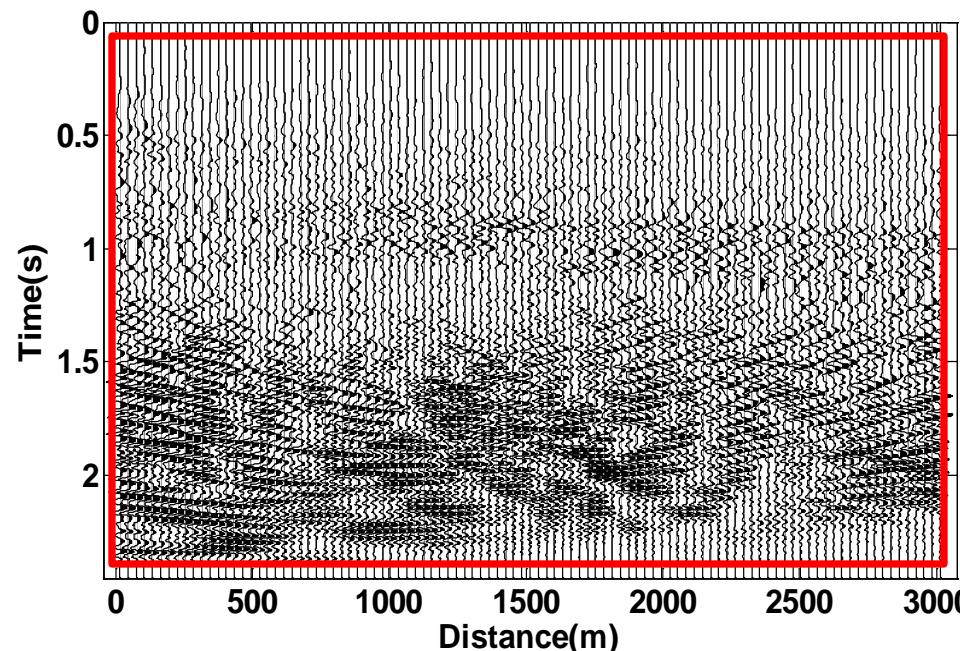


Footprints



# Time lapse, effect of loosing receivers

5% of data  
Migration                    LSPSM



Footprints

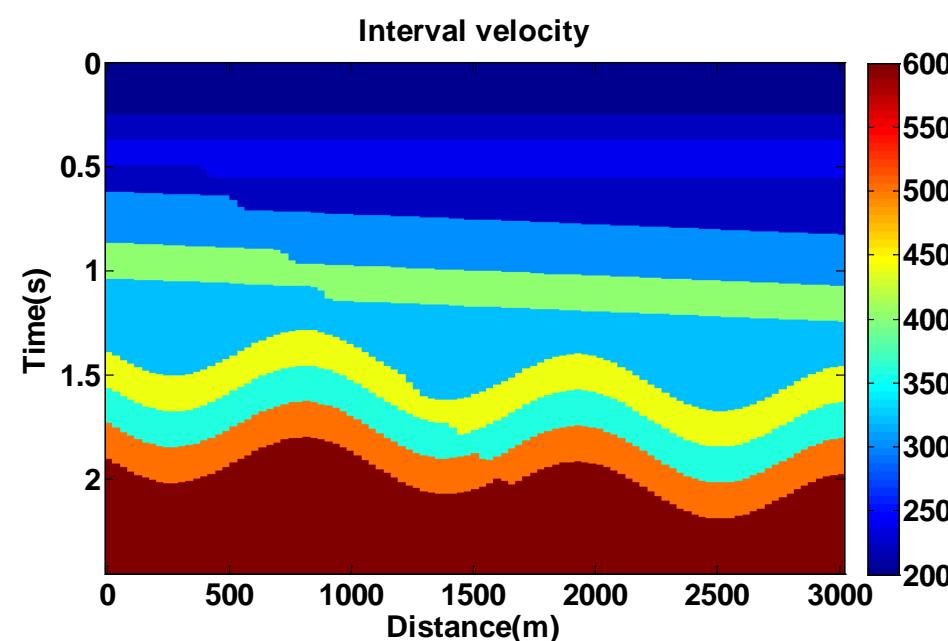
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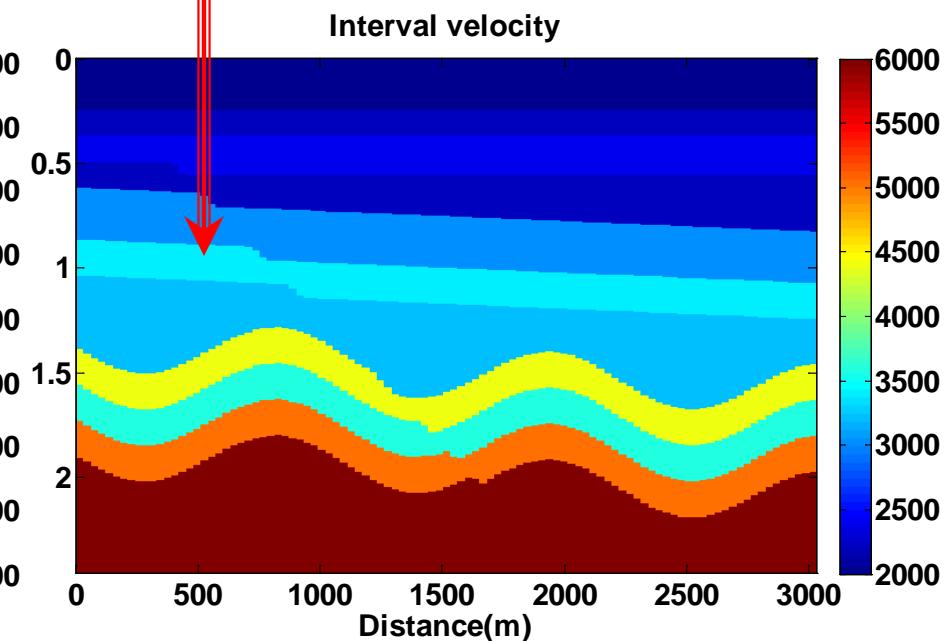
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# Change in velocity model

15% less velocity,  $4000 >> 3400 \text{ m/s}$

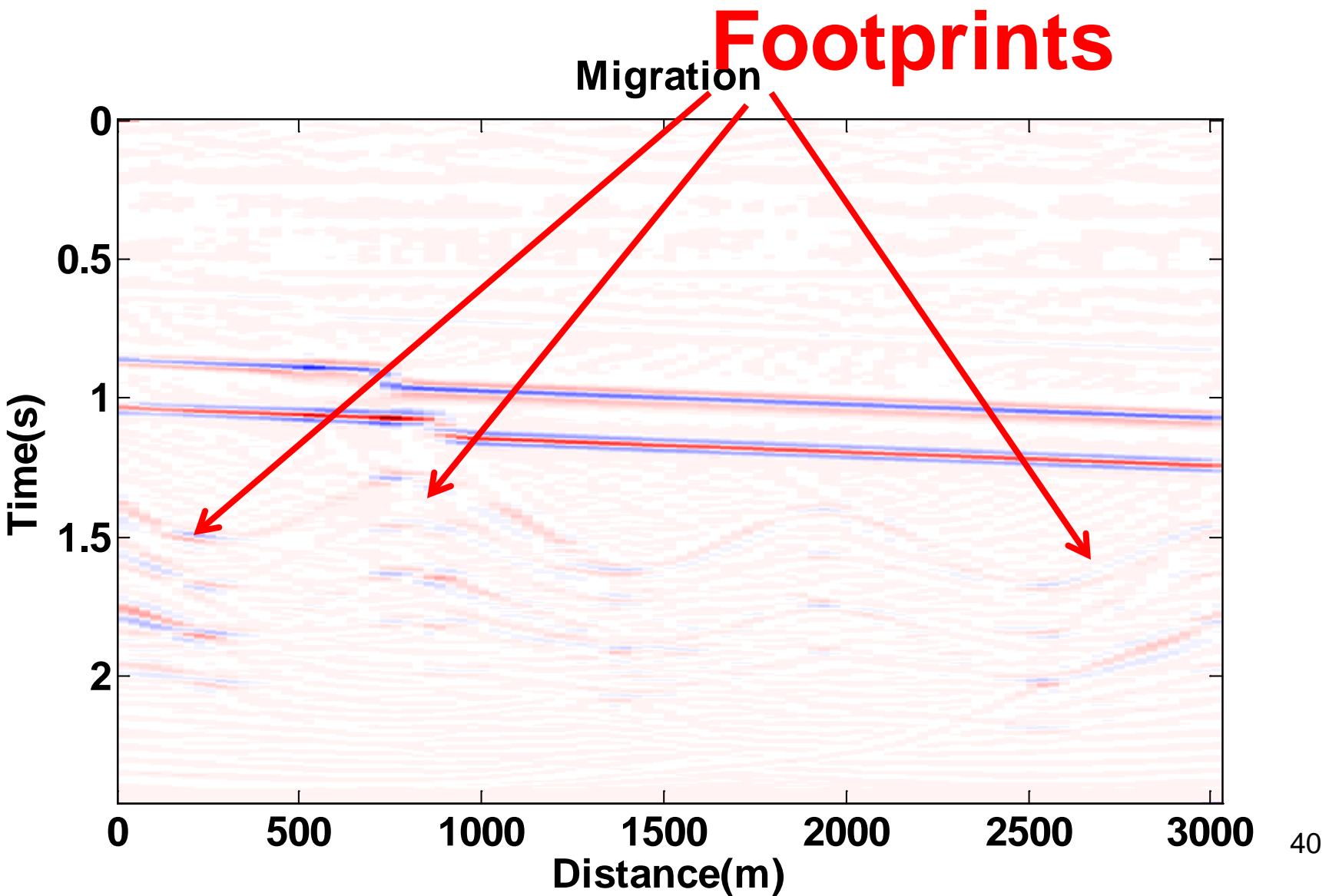


Baseline



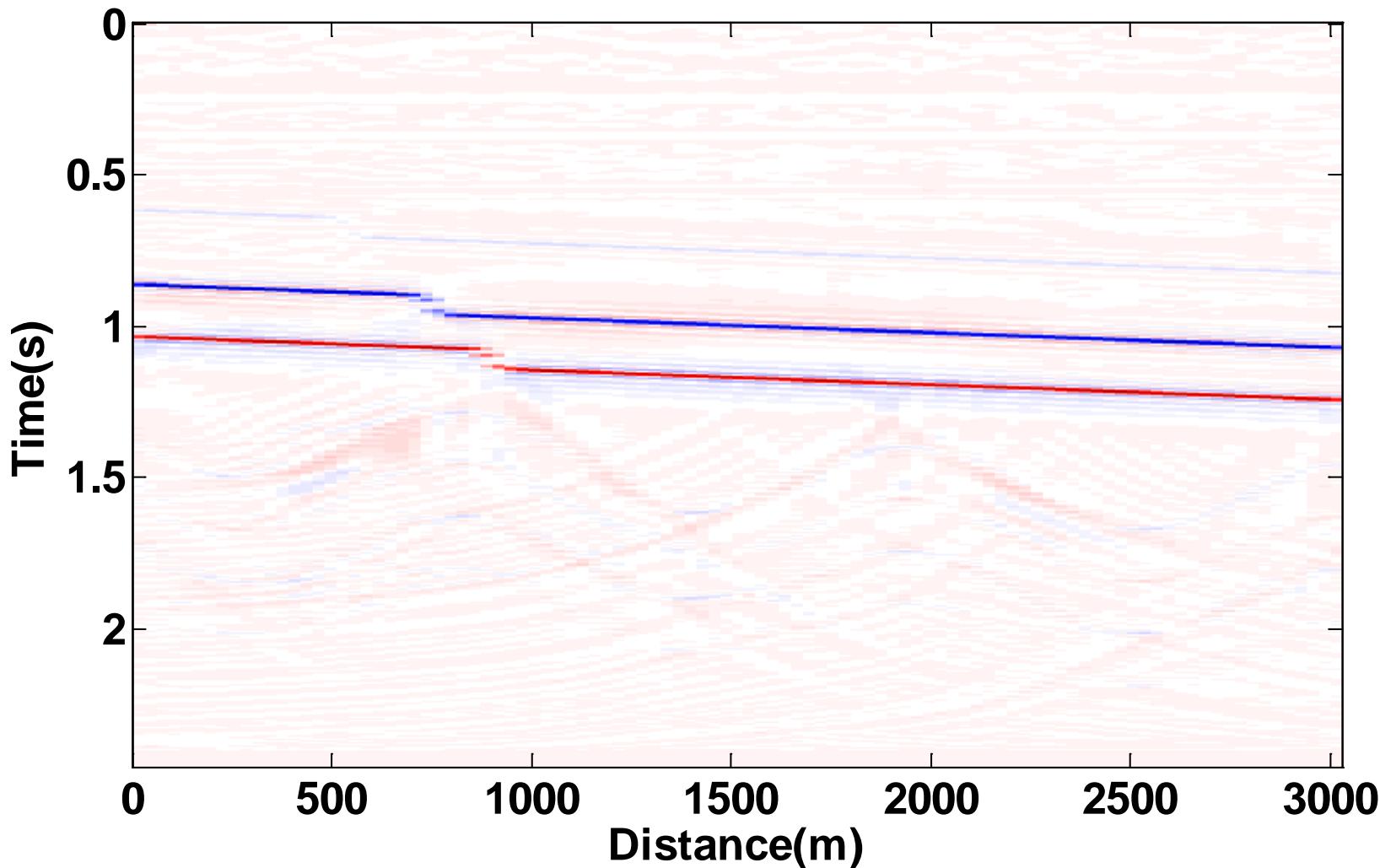
Monitor

# Migration time lapse



# LSPSM time lapse

Inversion LSCG



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Inverting for:

1. Multiple Image Joint Inversion (MIJI)
2. Image Difference Joint Inversion (IDJI)

I. Summary

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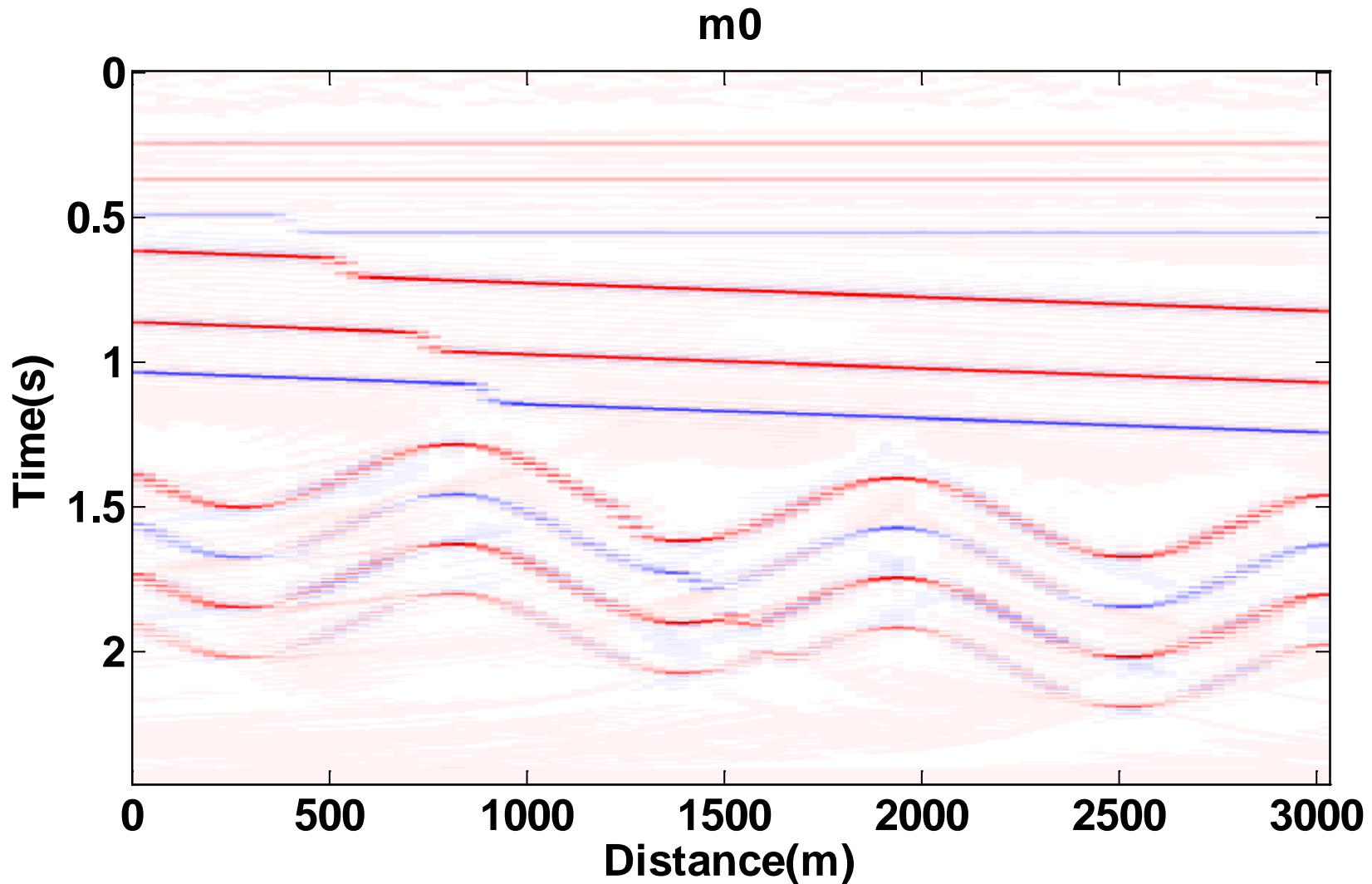
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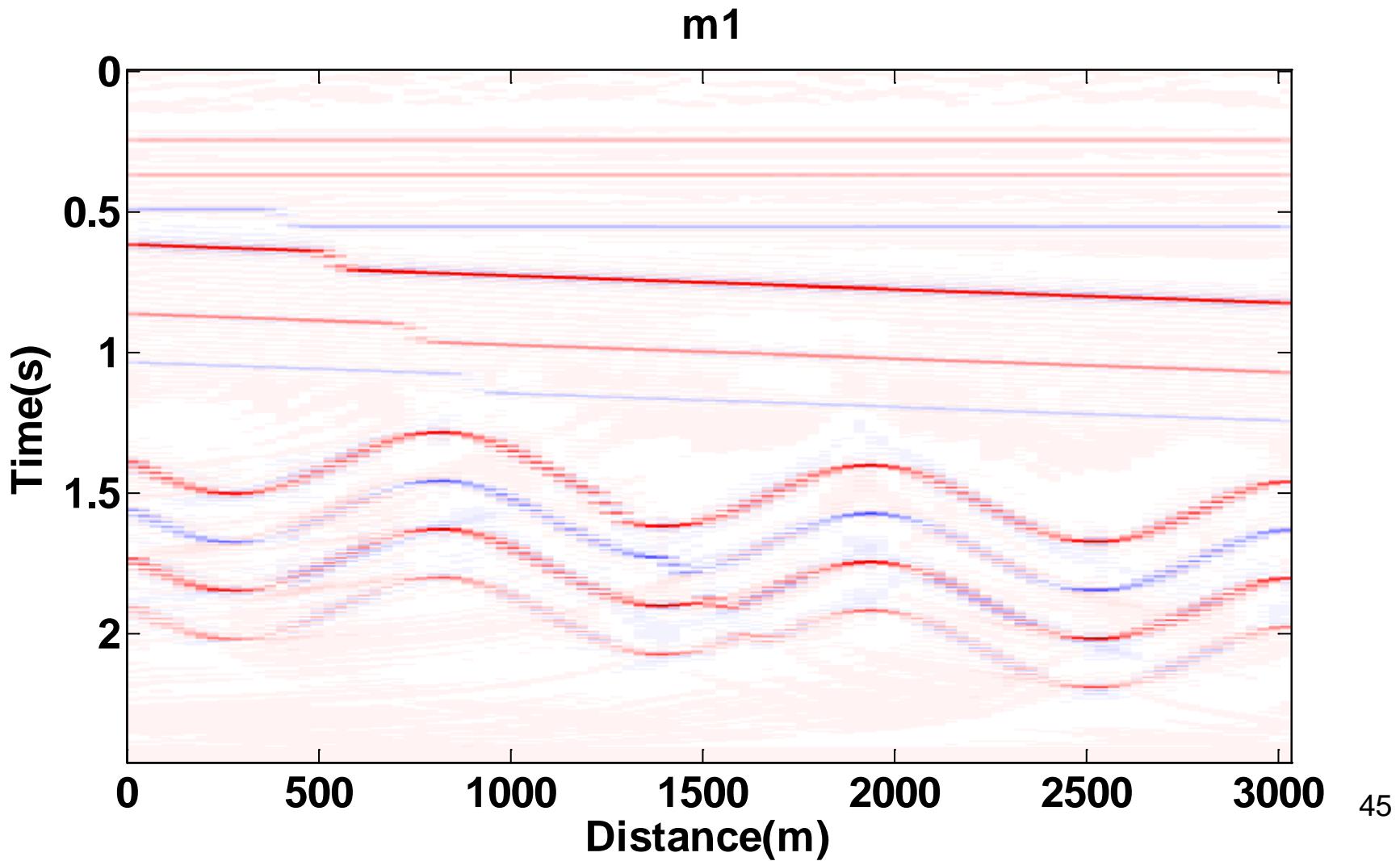
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I. Summary

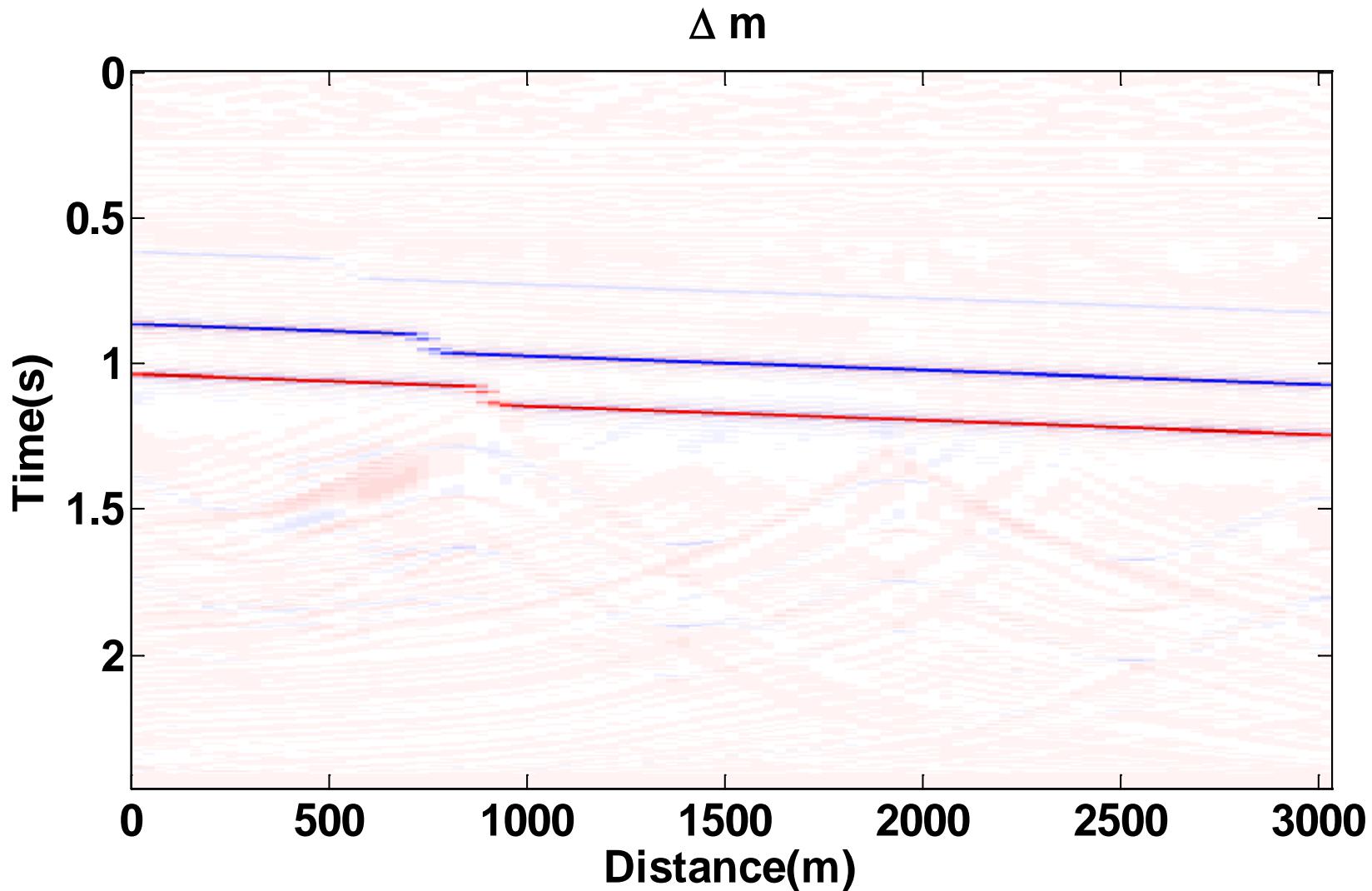
# Joint inversion for baseline & monitor (MIJI)



# Joint inversion for baseline & monitor (MIJI)



# Joint inversion for baseline & monitor (MIJI)



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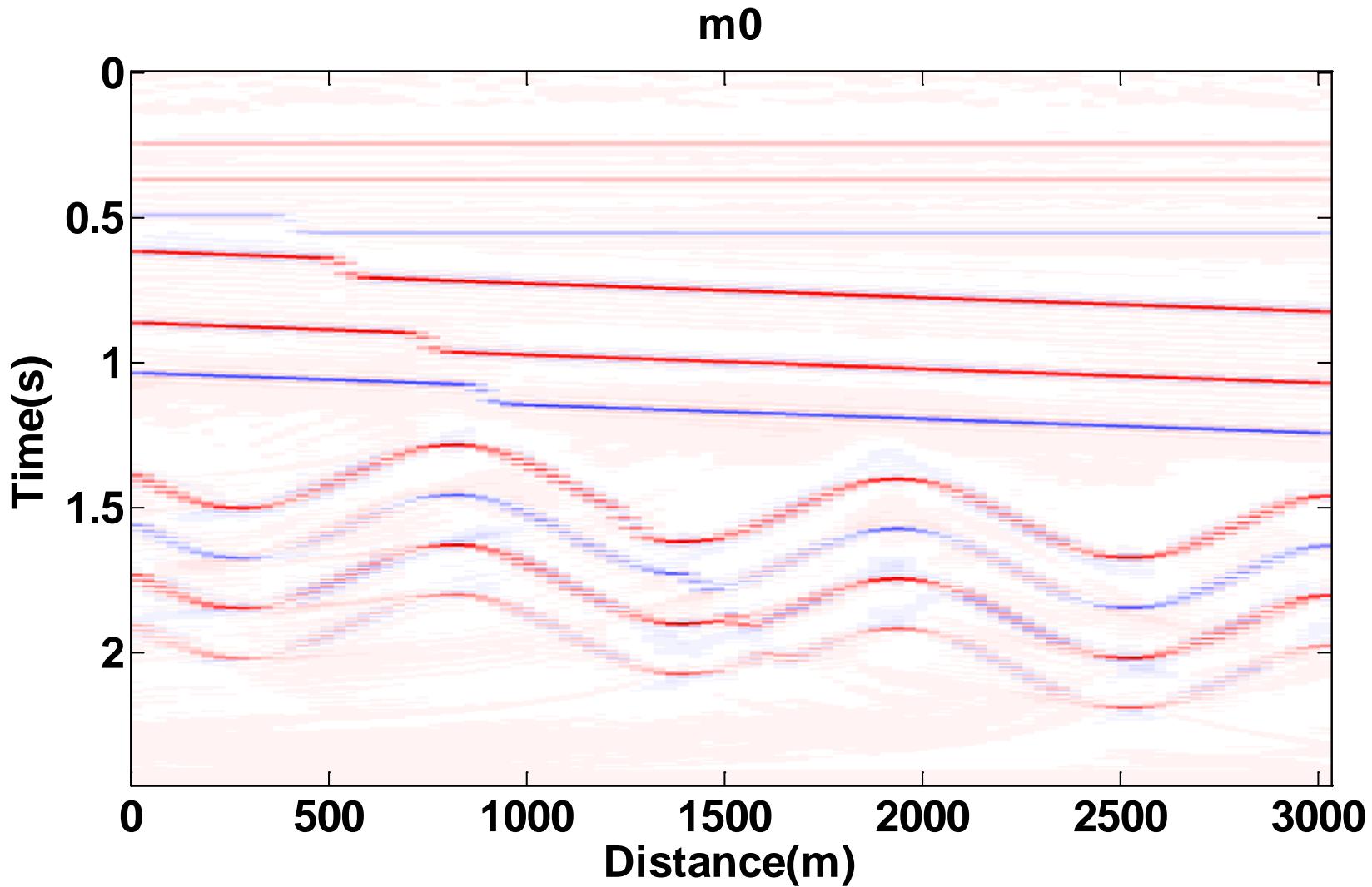
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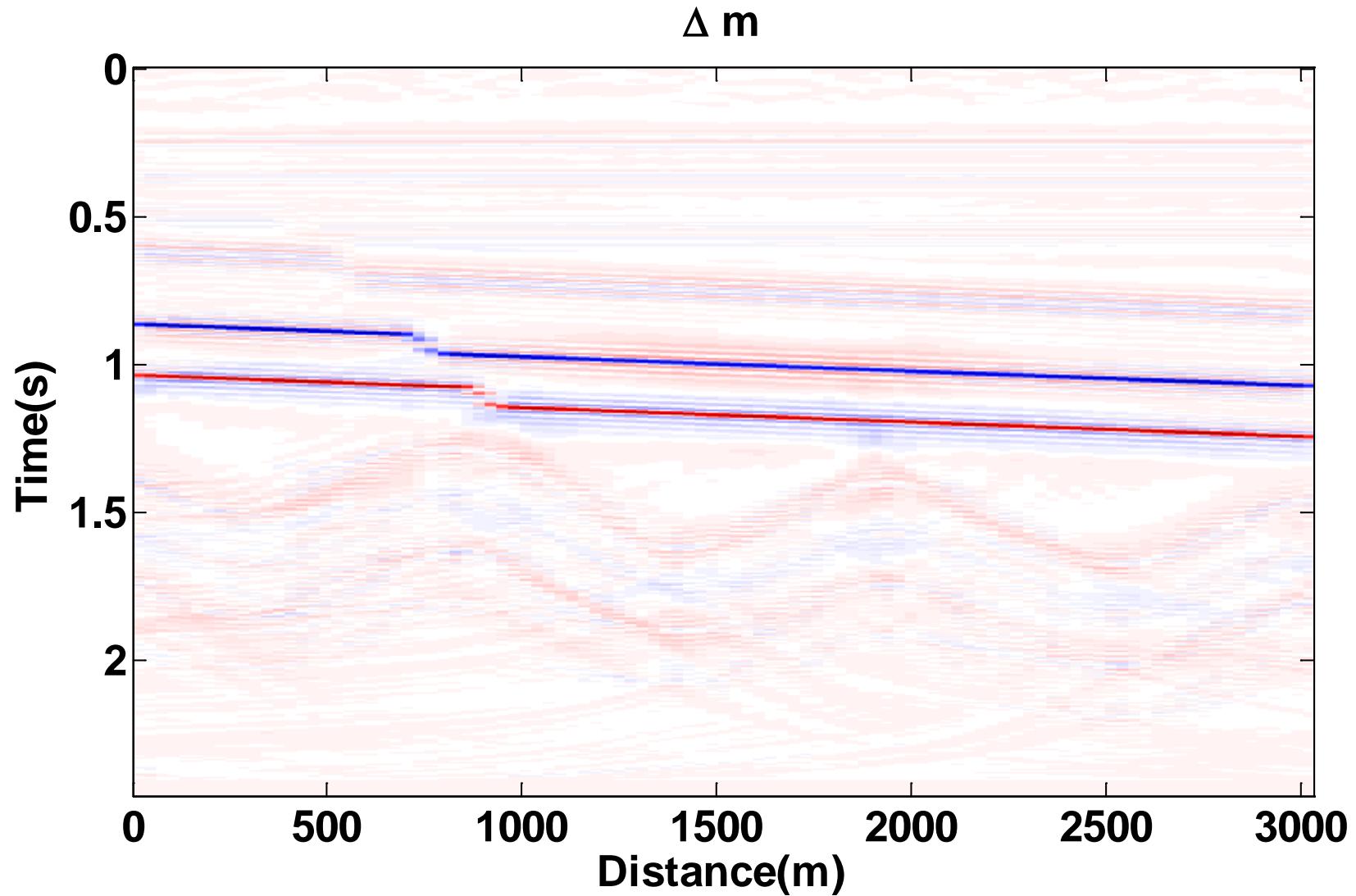
1. Multiple Image Joint Inversion (MIJI)
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I. Summary

# Joint inversion for baseline & difference (IDJI)



# Joint inversion for baseline & difference (IDJI)



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# Summary

- Difference in acquisition geometries leaves different artifacts at the baseline and monitor migration images.
- Separate LSPSM/inversion of both datasets removes these artifacts.
- and produces comparable data for prestack time lapse studies.

# Summary

- Joint inversion of both datasets produces a high resolution time lapse image.
- Best result achieved with the Multiple Image Joint Inversion (MIJI).
- Each iteration in LSCG to solve MIJI or IDJI costs 4 times more than a conventional migration of baseline data.
- Method is easily extendable for the joint inversion of baseline survey and **multiple monitor surveys**.

# Summary

- It is possible to add regularization terms:  
highlighting the changes in the time lapse  
images by adding sparse regularization.

# Acknowledgments:

- I would like to thank:
  - NSERC and other CREWES sponsors, YOU,
  - CREWES faculty, staff and previous and current students,
  - Kevin Hall and Rolf Maier,
- Especial thanks to Dr. John Bancroft, and other people that helped me in last 4 years.