

# Hydrocarbon discrimination with AVO analysis

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# Motivation

- Summarize various hydrocarbon indicators
- Which indicator can easily discriminate the gas/oil sand from the background
- Which indicator is more sensitive to pore-fluid content

# Outline

- Hydrocarbon indicators
- Sensitivity analysis for hydrocarbon indicators
- $(V_p/V_s)_{\text{dry}}^2$  value analysis
- Conclusion & future work

# Hydrocarbon indicator

## $R_p - g * R_s$

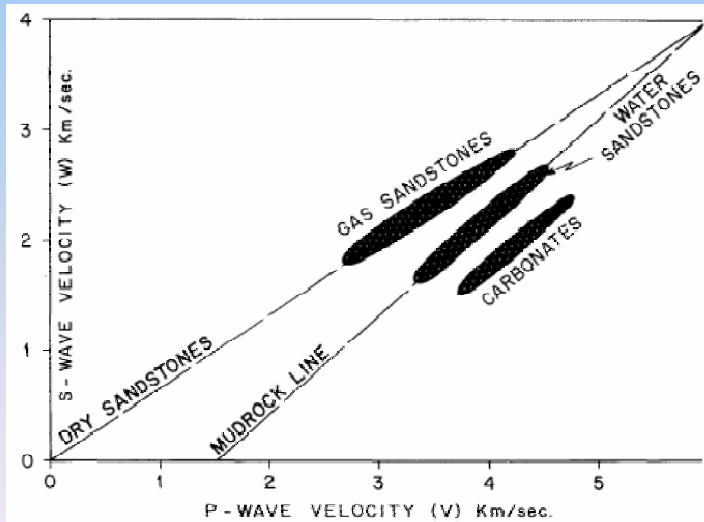
(Smith, Gidlow, 1987 and Fatti, 1994)

$$\Delta F = R_p - 1.16 \frac{V_p}{V_s} * R_s$$

Smith and Gidlow (1987)

For gas saturated rocks,  $\Delta F < 0$

For water saturated rocks,  $\Delta F \approx 0$



$$V_p \approx 1360 + 1.16V_s$$

Castagna et al. (1985)

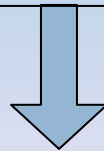
# Hydrocarbon indicator

## The Elastic Constants

(Russell, Gray and Hampson, 2006)

$$R(\theta) = \left[ \frac{1}{4} - \frac{1}{2} \frac{\beta^2}{\alpha^2} \right] \sec^2 \theta \frac{\Delta\lambda}{\lambda} + \frac{\beta^2}{\alpha^2} \left[ \frac{1}{2} \sec^2 \theta - 2 \sin^2 \theta \right] \frac{\Delta\mu}{\mu} + \left[ \frac{1}{2} - \frac{1}{4} \sec^2 \theta \right] \frac{\Delta\rho}{\rho}$$

$$R(\theta) = \left[ \frac{1}{4} - \frac{1}{3} \frac{\beta^2}{\alpha^2} \right] \sec^2 \theta \frac{\Delta K}{K} + \frac{\beta^2}{\alpha^2} \left[ \frac{1}{3} \sec^2 \theta - 2 \sin^2 \theta \right] \frac{\Delta\mu}{\mu} + \left[ \frac{1}{2} - \frac{1}{4} \sec^2 \theta \right] \frac{\Delta\rho}{\rho}$$



$\lambda$  = incompressibility  
 $\mu$  = rigidity

$\kappa$   $\lambda$   $\mu$   $\rho$

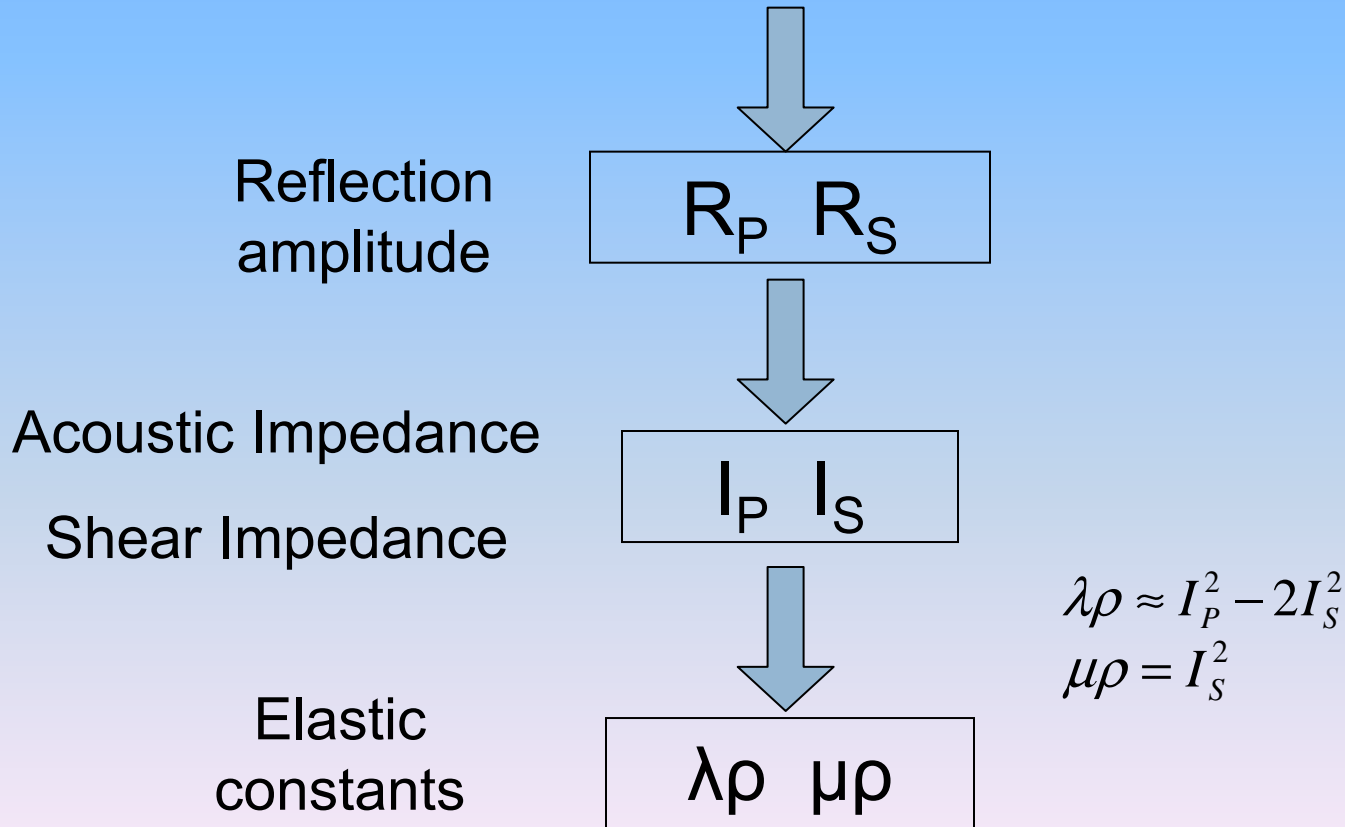
Low  $\lambda$  suggests gas saturation  
High  $\mu$  suggests sand

# Hydrocarbon indicator

## The LMR Parameters

(Goodway, et al., 1997)

$$R(\theta) \approx (1 + \tan^2 \theta)R_p - (2 \sin^2 \theta)R_s$$



# Hydrocarbon indicator

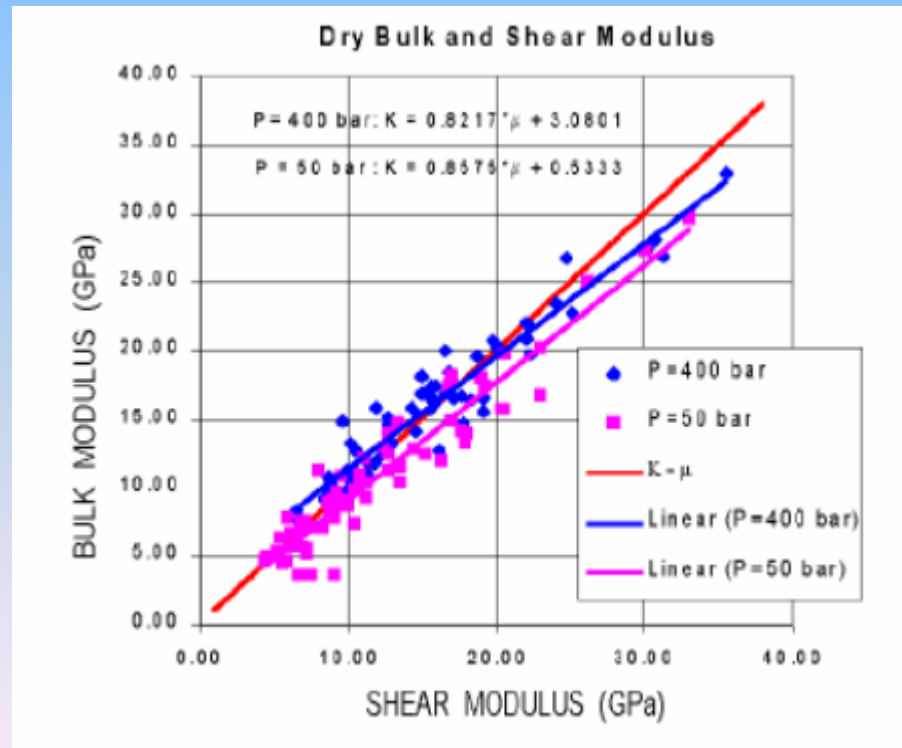
$$(K - \mu)$$

(Batzle, Han, and Hofmann, 2001)

$$K_{sat} - \mu = K_{dry} + \Delta K - \mu$$

$$= \Delta K$$

when  $K_{dry} \approx \mu$



# Hydrocarbon indicator

$$I_p^2 - c I_s^2$$

(Russell et al., 2003)

**Gassmann Equation:**  $K_{sat} = K_{dry} + \Delta K$

**Basic equations for  $V_p$  and  $V_s$  in isotropic, elastic media**

$$V_p = \sqrt{\frac{K_{dry} + 4/3\mu + \Delta K}{\rho_{sat}}} \quad V_s = \sqrt{\frac{\mu}{\rho_{sat}}}$$

$$I_p^2 - c I_s^2 = \rho_{sat} (\Delta K + K_{dry} + 4/3\mu - c\mu)$$

**When**  $c = \frac{K_{dry}}{\mu} + \frac{4}{3} = \left[ \frac{V_p}{V_s} \right]_{dry}^2$

$$I_p^2 - c I_s^2 = \rho_{sat} \Delta K$$

**Fluid Term**



# Are they related to each other?

$$\lambda \rho_{sat} = Ip^2 - 2Is^2$$

Goodway et al. ,1997

Implies that  $c=2$  and Poisson's ratio is 0.

$$K_p - \mu = Ip^2 - 2.233Is^2$$

Hedlin, 2000

when ratio of  $K_{dry}$  to  $\mu$  is equal to 0.9, which implies that  $c=2.233$

$$K - \mu \approx (K_{dry} + \Delta K - \mu) \rho = Ip^2 - 2.333Is^2$$

Batzle et al. ,2001

when  $K_{dry} \approx \mu$  , which Implies that  $c=2.333$

# Sensitivity analysis

## Clean sand

Hydrocarbon indicators		Vp (km/s)	Vs (km/s)	Vp/Vs (-)	$\rho$ (g/cc)	Ip (km/s.g/cc)	Is (km/s.g/cc)	$u\rho$ (GPa.g/cc)	$\lambda\rho$ (GPa.g/cc)
		Dry	Mean value	4.39	2.91	1.51	2.26	10.01	6.63
Std.dev.	0.66		0.46	0.04	0.17	2.18	1.52	21	5.28
Wet	Mean value	4.71	2.95	1.61	2.41	11.4	7.13	52.47	27.99
	Std.dev.	0.56	0.44	0.06	0.1	1.85	1.36	20.02	5.88
Fluid indicator coefficient		<b>0.48</b>	<b>0.09</b>	<b>2.50</b>	<b>0.88</b>	<b>0.64</b>	<b>0.33</b>	<b>0.30</b>	<b>2.95</b>
Hydrocarbon indicators		K (GPa)	u (GPa)	$\lambda$ (GPa)	$u/\lambda$ (-)	$\sigma$ (-)	K-u (GPa)	$Ip^2-cIs^2$ (GPa.g/cc)	Fluid Factor (-)
Dry	Mean value	18.71	19.9	5.45	0.29	0.11	-1.19	0.89	-0.3
	Std.dev.	6.51	7.73	2.14	0.13	0.04	2.37	4.57	0.07
Wet	Mean value	25.94	21.53	11.58	0.59	0.18	4.41	14.87	-0.16
	Std.dev.	5.88	7.33	2.08	0.19	0.04	2.67	5.53	0.07
Fluid indicator coefficient		<b>1.11</b>	<b>0.21</b>	<b>2.86</b>	<b>2.31</b>	<b>1.75</b>	<b>2.36</b>	<b>3.06</b>	<b>2.00</b>

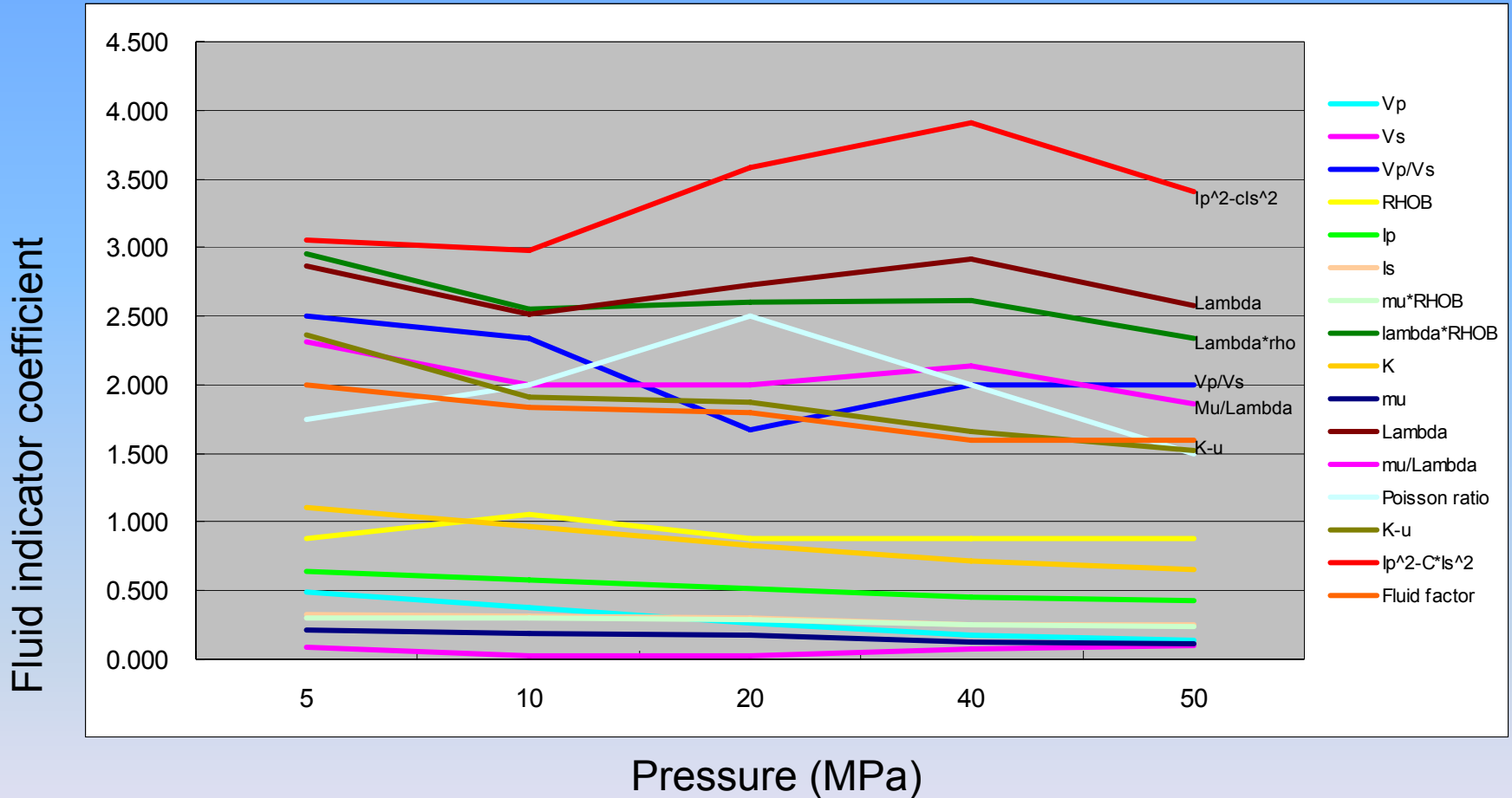
Fluid indicator coefficient:

$$\frac{|Mean_{dry} - Mean_{wet}|}{Std_{wet}}$$

(Han's dataset)

# Sensitivity analysis

Clean sand



The most sensitive indicators:  $Ip^2-c*Is^2$ ,  $\Lambda$ ,  $\Lambda*rho$ ,  $\mu/\Lambda$

# Sensitivity analysis

## Whole dataset

		Vp (km/s)	Vs (km/s)	Vp/Vs (-)	$\rho$ (g/cc)	Ip (km/s.g/cc)	Is (km/s.g/cc)	up (GPa.g/cc)	$\lambda\rho$ (GPa.g/cc)	
5MPa	Hydrocarbon indicators									
	Dry	Mean value	3.33	2.22	1.5	2.2	7.4	4.94	26.34	6.29
		Std.dev.	0.73	0.49	0.06	0.2	2.07	1.41	15.74	4.68
	Wet	Mean value	3.84	2.19	1.77	2.37	9.15	5.22	29.19	28.59
		Std.dev.	0.6	0.48	0.12	0.13	1.8	1.34	15.76	6.97
	Fluid indicator coefficient		<b>0.70</b>	<b>0.06</b>	<b>4.50</b>	<b>0.85</b>	<b>0.85</b>	<b>0.20</b>	<b>0.18</b>	<b>4.76</b>
	Hydrocarbon indicators		K (GPa)	u (GPa)	$\lambda$ (GPa)	u/ $\lambda$ (-)	$\sigma$ (-)	K-u (GPa)	Ip <sup>2</sup> -cIs <sup>2</sup> (GPa.g/cc)	Fluid Factor (-)
	Dry	Mean value	10.61	11.62	2.86	0.26	0.1	-1.01	-0.29	-0.29
		Std.dev.	5.5	6.13	2.01	0.17	0.06	1.86	3.85	0.06
	Wet	Mean value	20.03	12.11	11.96	1.16	0.26	7.92	21.29	-0.04
Std.dev.		5.35	6.07	2.42	0.42	0.05	2.6	6.31	0.08	
Fluid indicator coefficient		<b>1.71</b>	<b>0.08</b>	<b>4.53</b>	<b>5.29</b>	<b>2.67</b>	<b>4.80</b>	<b>5.61</b>	<b>4.17</b>	

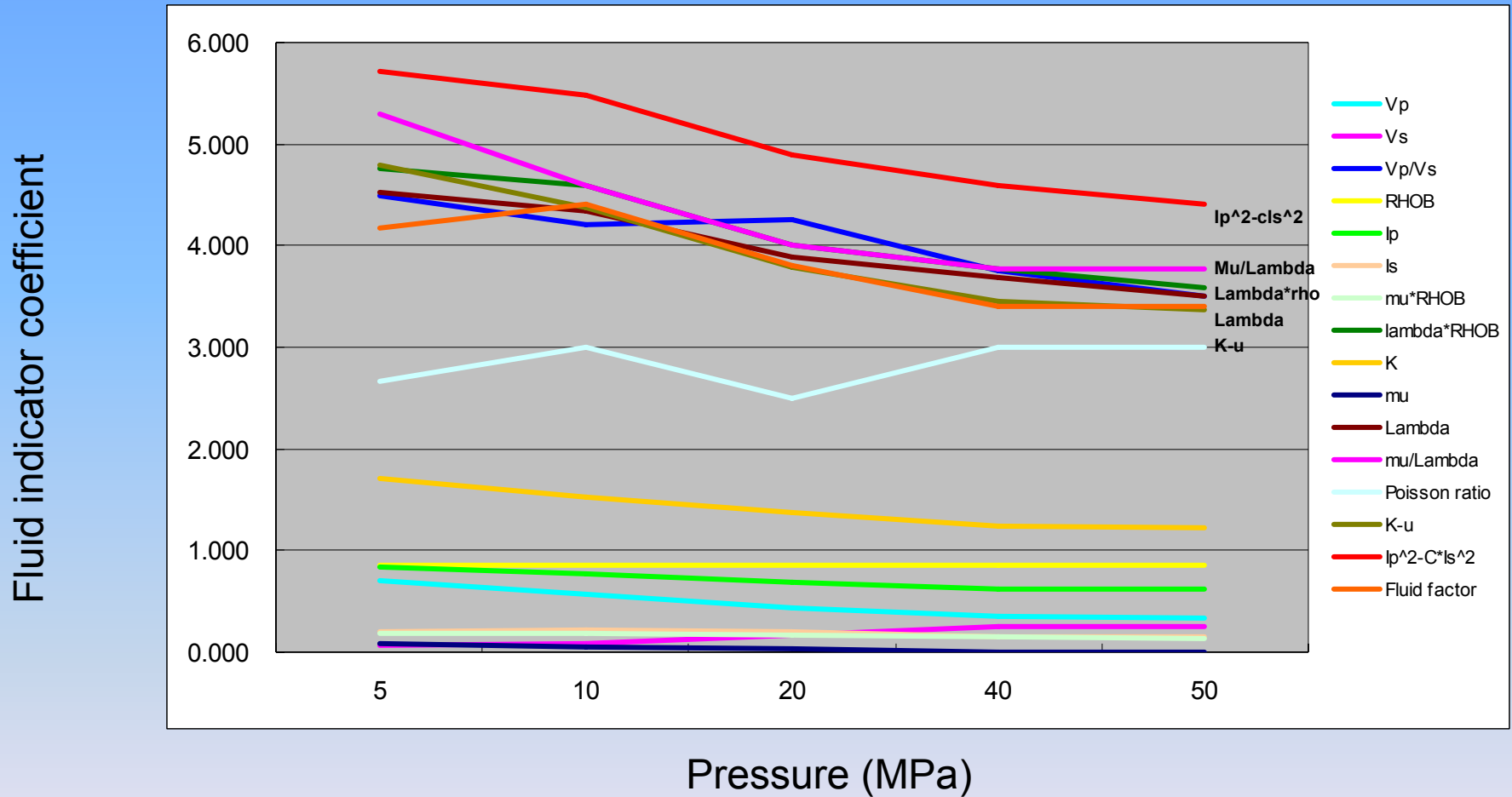
Fluid indicator coefficient:

$$\frac{|Mean_{dry} - Mean_{wet}|}{Std_{wet}}$$

(Han's dataset)

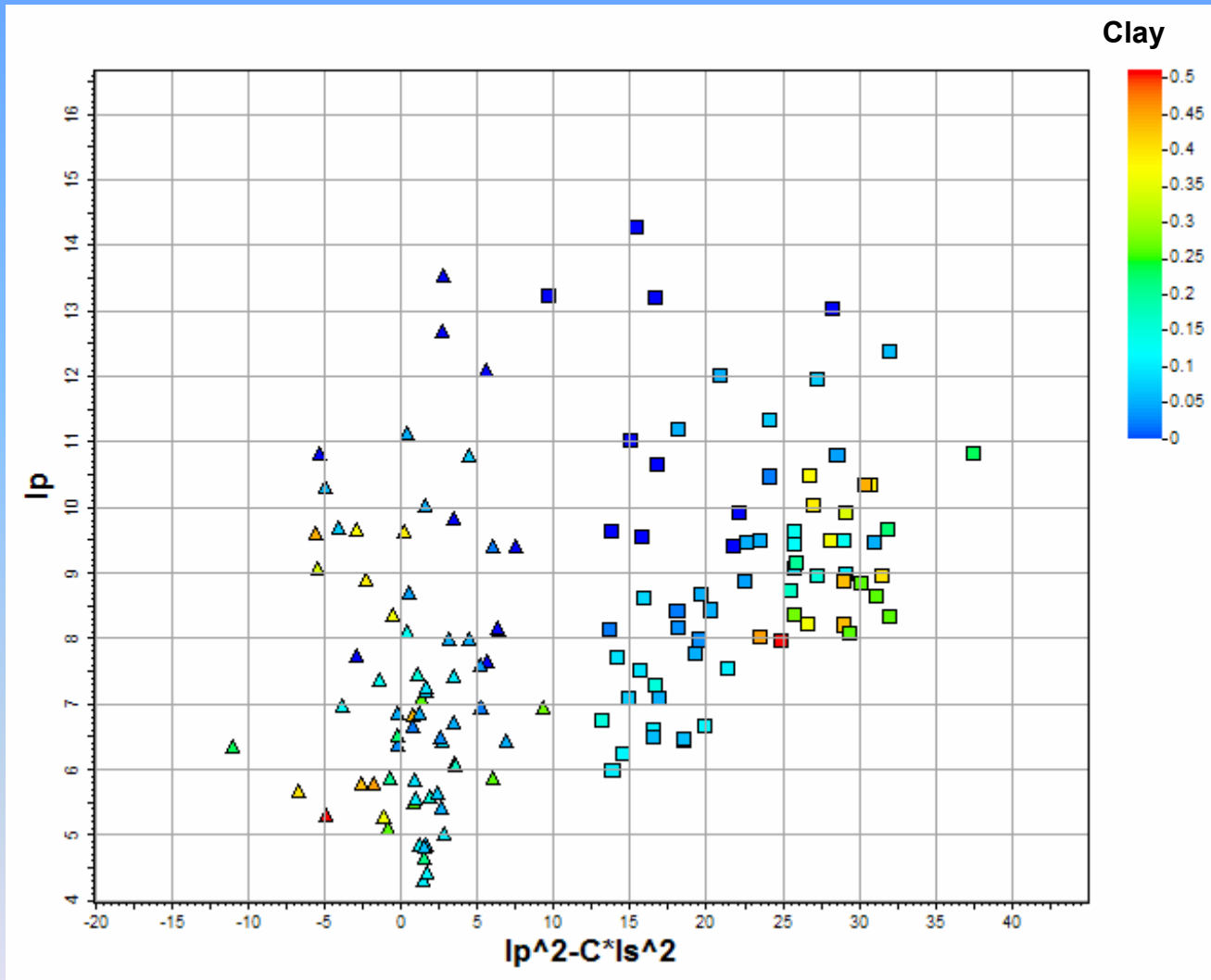
# Sensitivity analysis

Whole dataset



The most sensitive indicators:  $Ip^2-c*Is^2$ ,  $\Lambda$ ,  $\Lambda * \rho$ ,  $K-u$

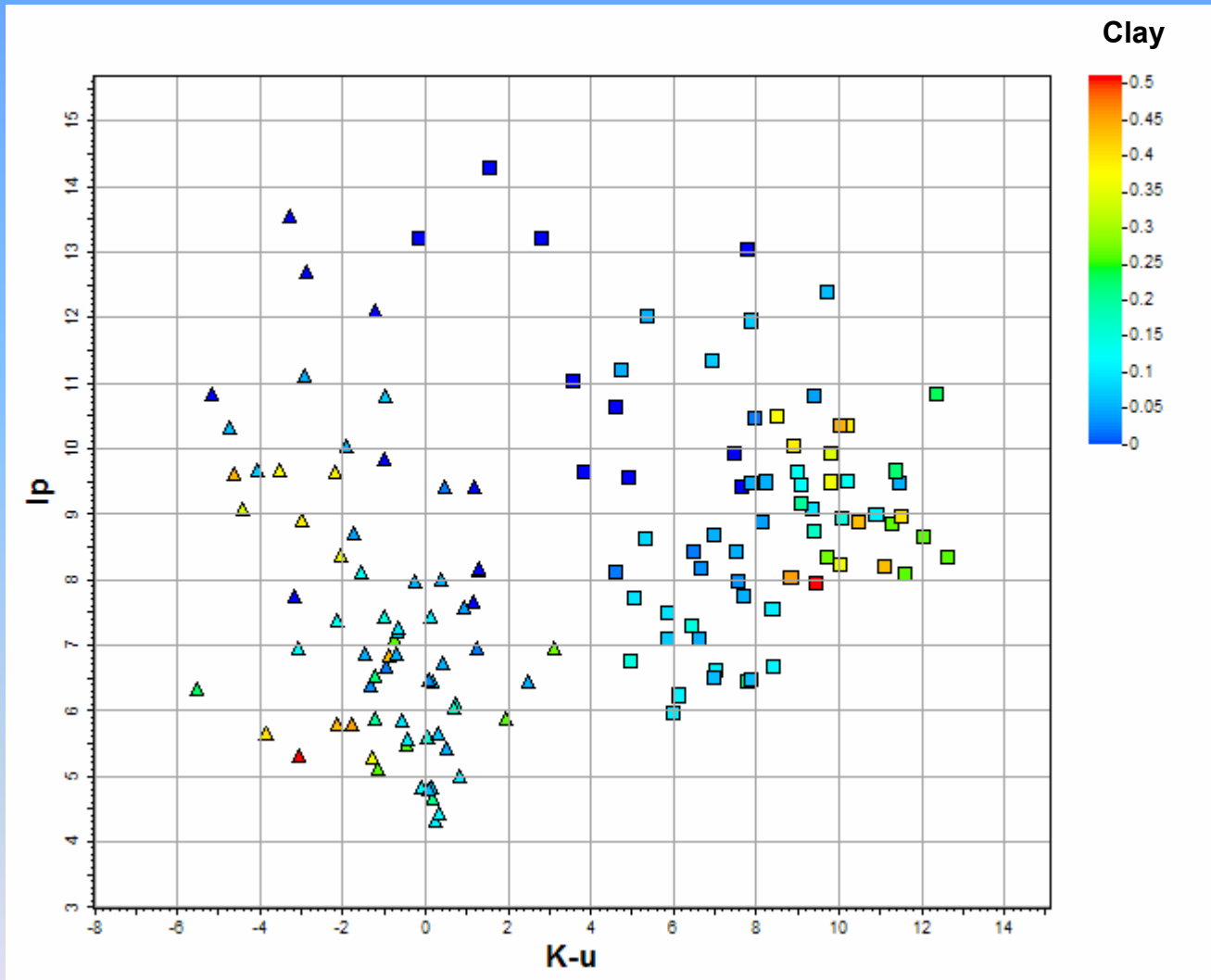
# Sensitivity analysis



△ Dry sand (5MPa)

□ Wet sand (5MPa)

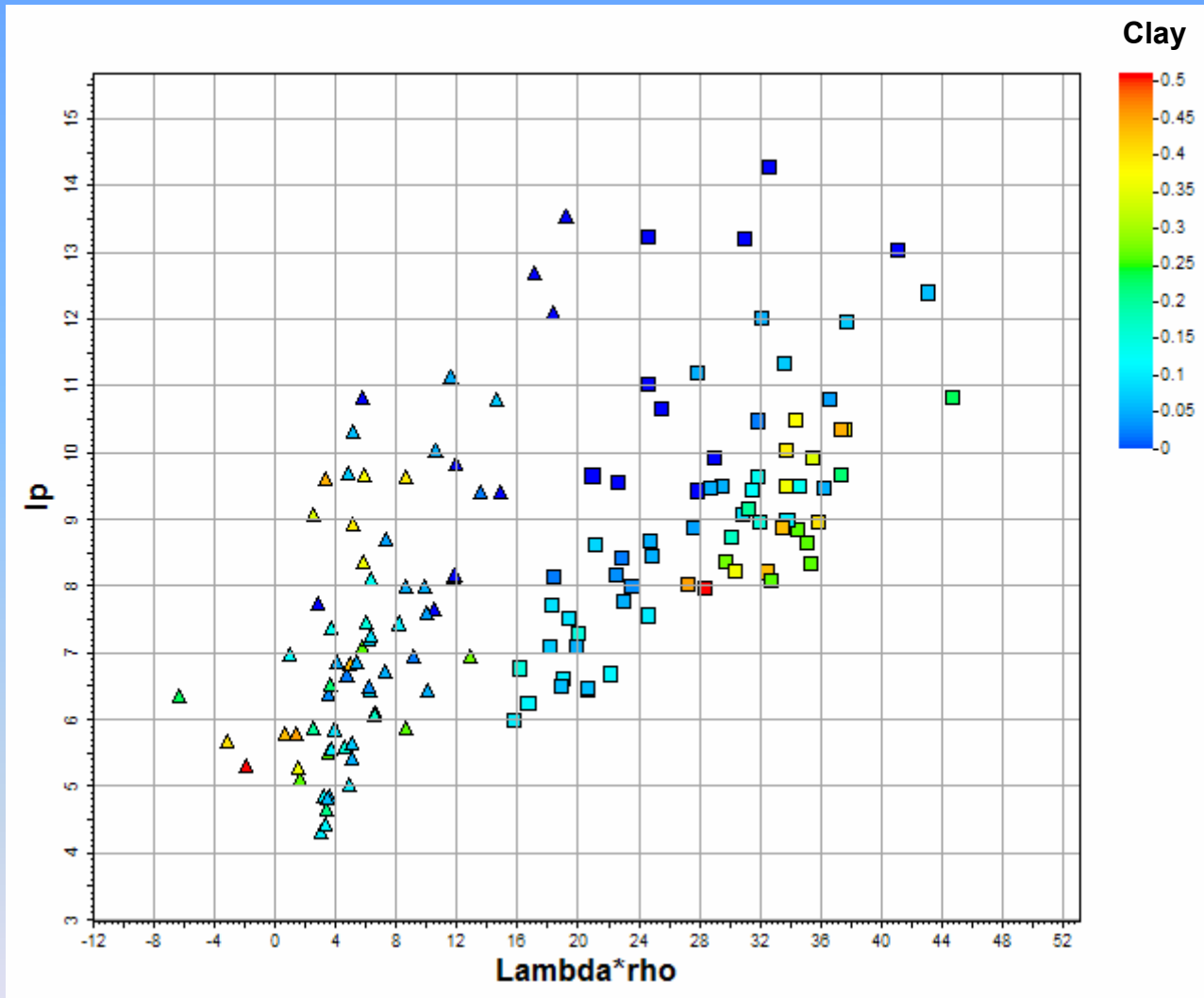
# Sensitivity analysis



△ Dry sand (5MPa)

□ Wet sand (5MPa)

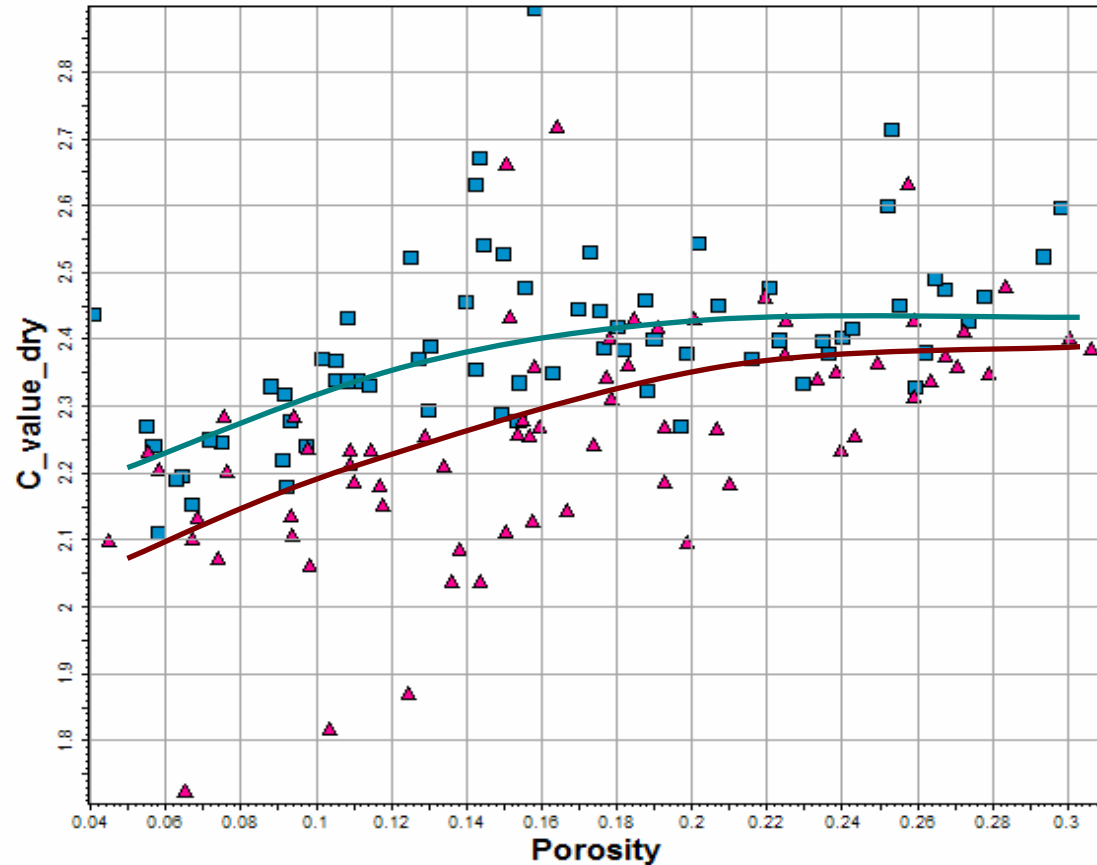
# Sensitivity analysis



- △ Dry sand (5MPa)
- Wet sand (5MPa)



# $C=(V_p/V_s)_{dry}^2$ value analysis

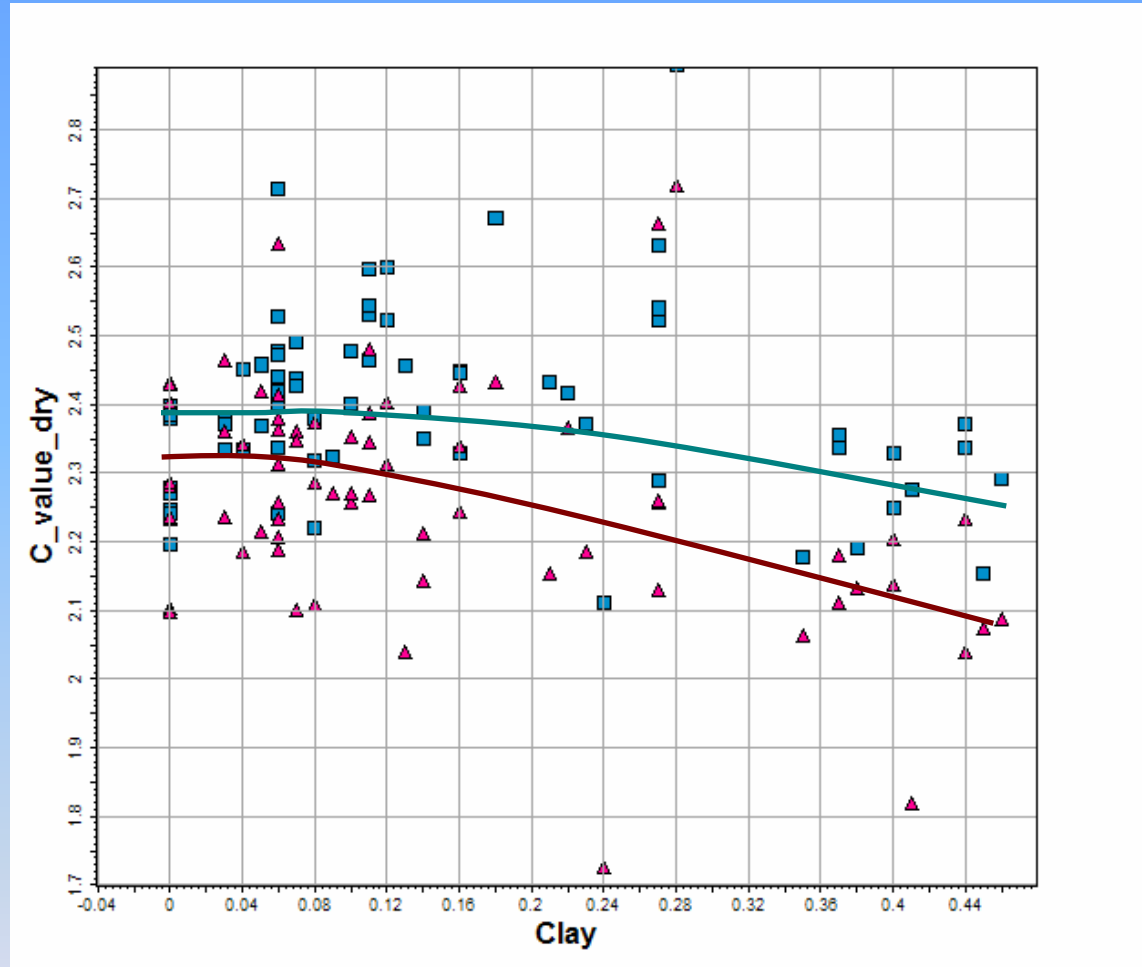


▲ 5 MPa

■ 50 MPa

Correlation between C value and porosity for 5 MPa and 50 MPa. Note that C increase with porosity.

# $C=(V_p/V_s)_{dry}^2$ value analysis

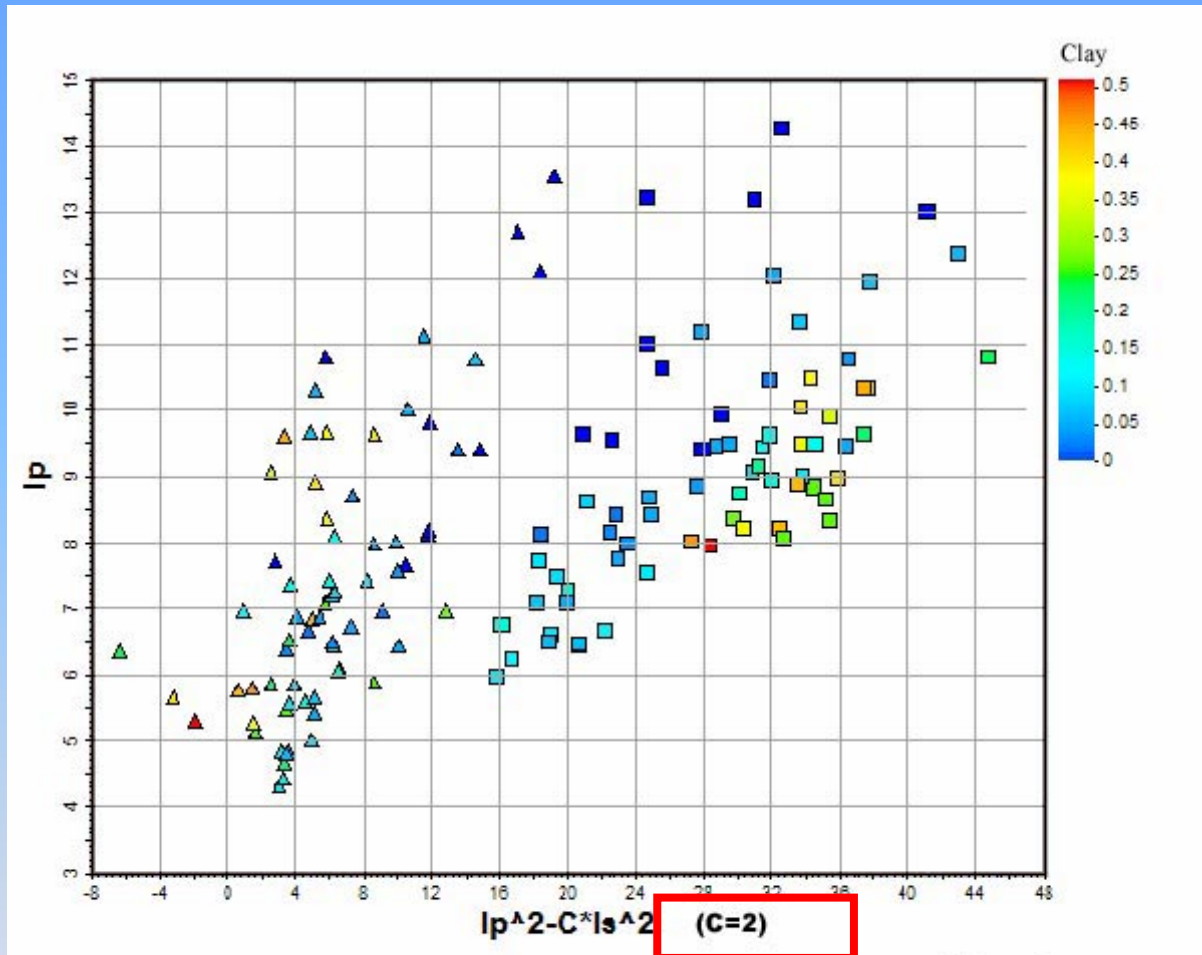


▲ 5 MPa

■ 50 MPa

Correlation between C value and porosity for 5 MPa and 50 MPa. Note that C decrease with clay content.

# $C=(V_p/V_s)_{dry}^2$ value analysis

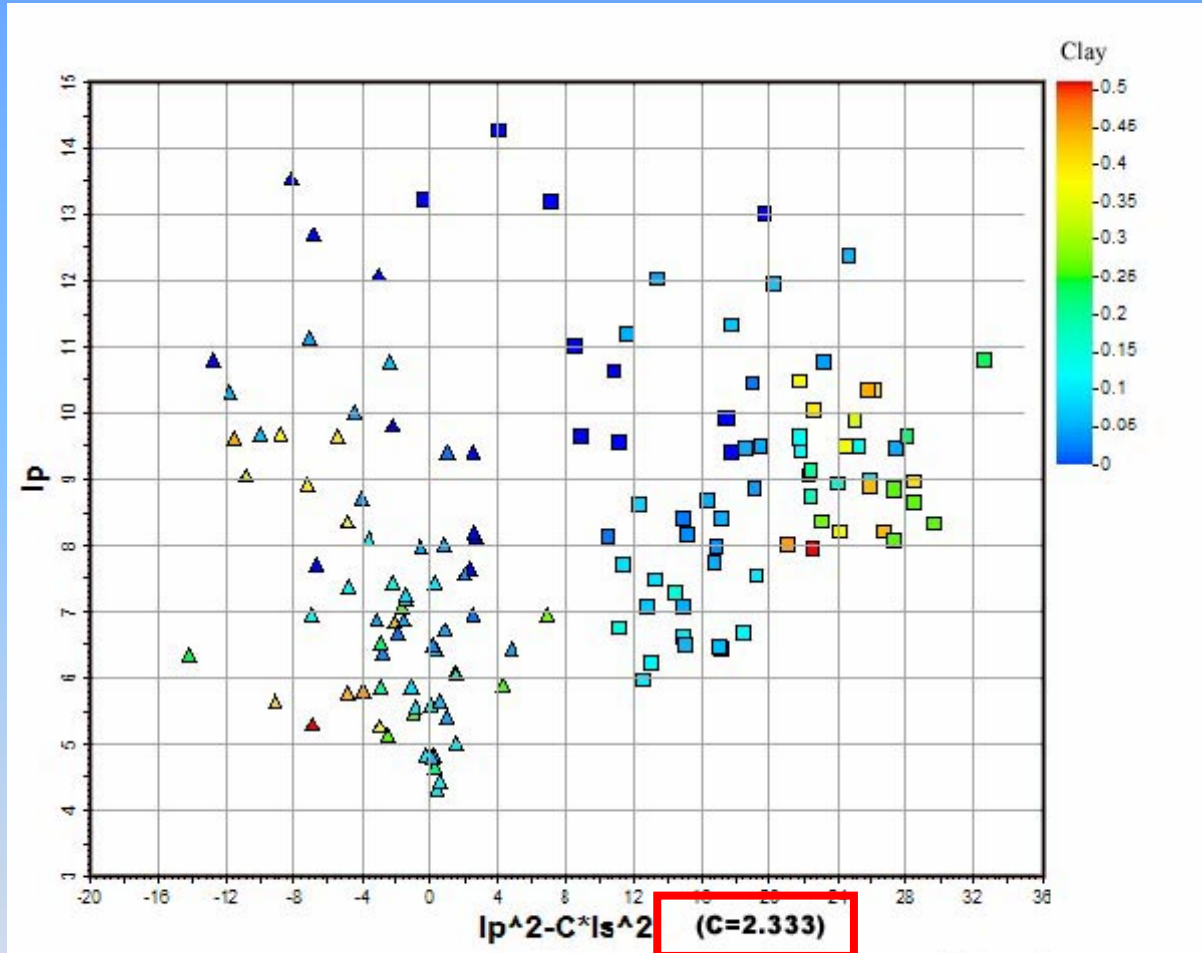


△ Dry sand (5MPa)

□ Wet sand (5MPa)

Crossplot of  $Ip^2 - c*Is^2$  versus  $Ip$  for 5 MPa pressure with different  $c$  value. Observe that there is a best separation between dry sand and wet sand for  $c=2.233$

# $C=(V_p/V_s)_{dry}^2$ value analysis

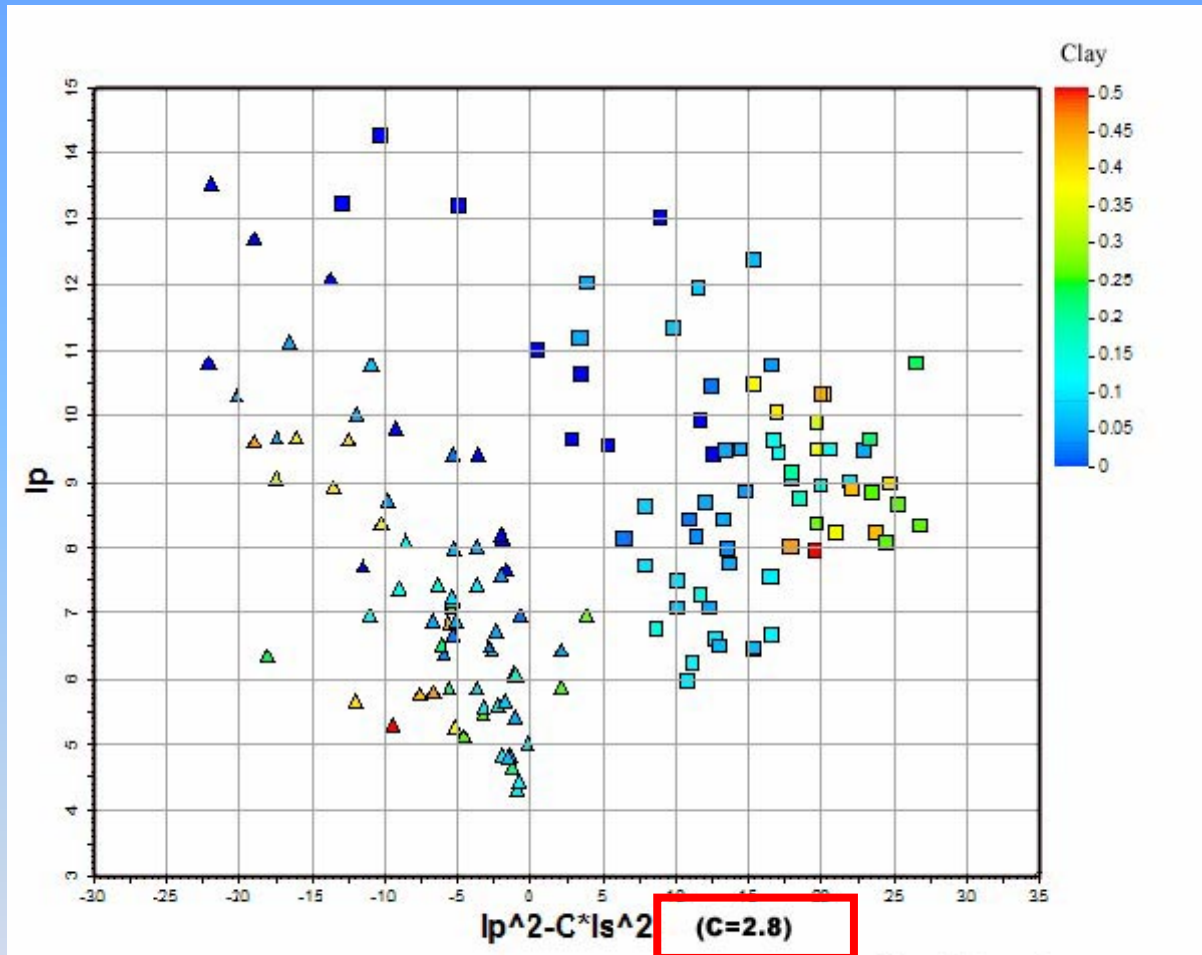


△ Dry sand (5MPa)

□ Wet sand (5MPa)

Crossplot of  $I_p^2 - c \cdot I_s^2$  versus  $I_p$  for 5 MPa pressure with different  $c$  value. Observe that there is a best separation between dry sand and wet sand for  $c=2.233$

# $C=(V_p/V_s)_{dry}^2$ value analysis



△ Dry sand (5MPa)

□ Wet sand (5MPa)

Crossplot of  $I_p^2 - c \cdot I_s^2$  versus  $I_p$  for 5 MPa pressure with different  $c$  value. Observe that there is a best separation between dry sand and wet sand for  $c=2.233$

# Conclusions

- Sensitive indicators for pore fluid are

$$Ip^2 - cIs^2$$

$$K_{sat} - \mu$$

$$\lambda\rho$$

- $(Vp/Vs)_{dry}^2$  value depend on porosity, clay content and pressure. The best C value need to be calibrated and tested for the local situation.

# Future work

- Continue studying on the quantitative estimation of fluid indicator by using well logs and seismic data.
- Apply AVO inversion to the seismic data to derive all these fluid indicators to study the reservoir fluid properties.

# Acknowledgments

- CREWES sponsors