



UNIVERSITY OF  
CALGARY



**CMC**  
Containment &  
Monitoring Institute

# The seismic interpretability of a 4D data, a case study: The FRS project

Davood Nowroozi

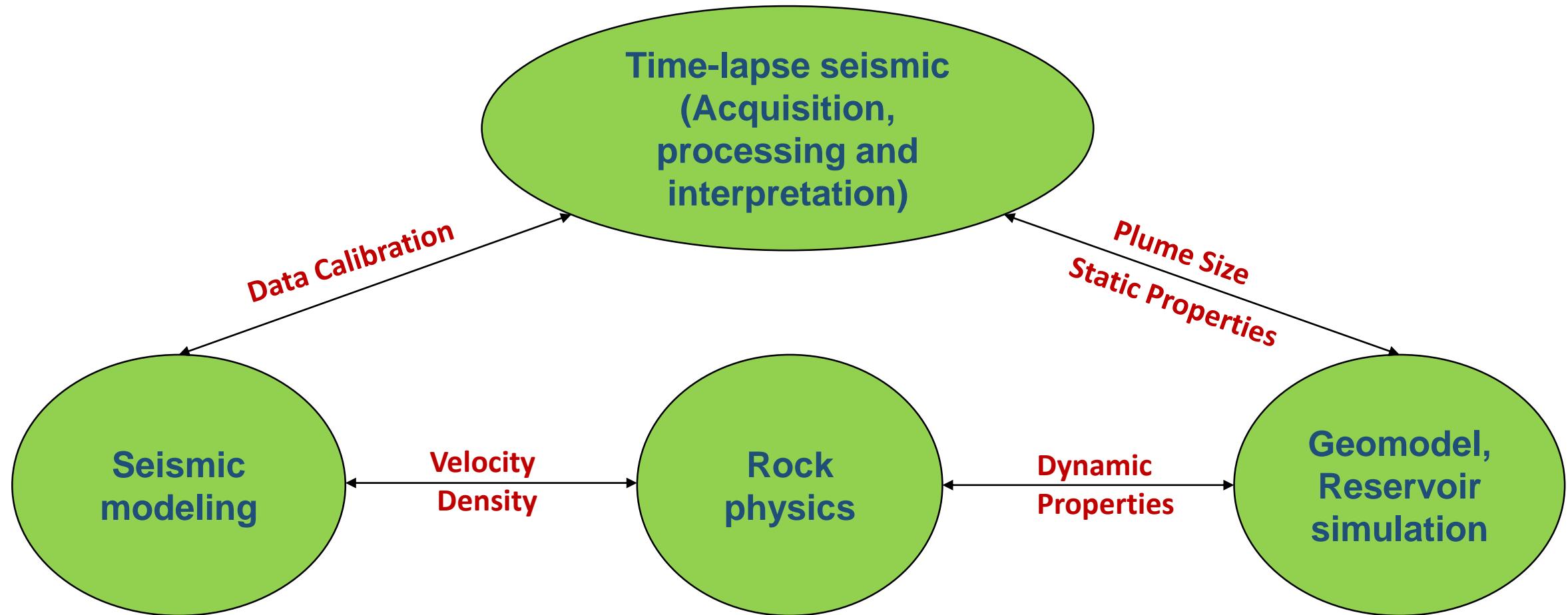
Don Lawton

Hassan Khaniani

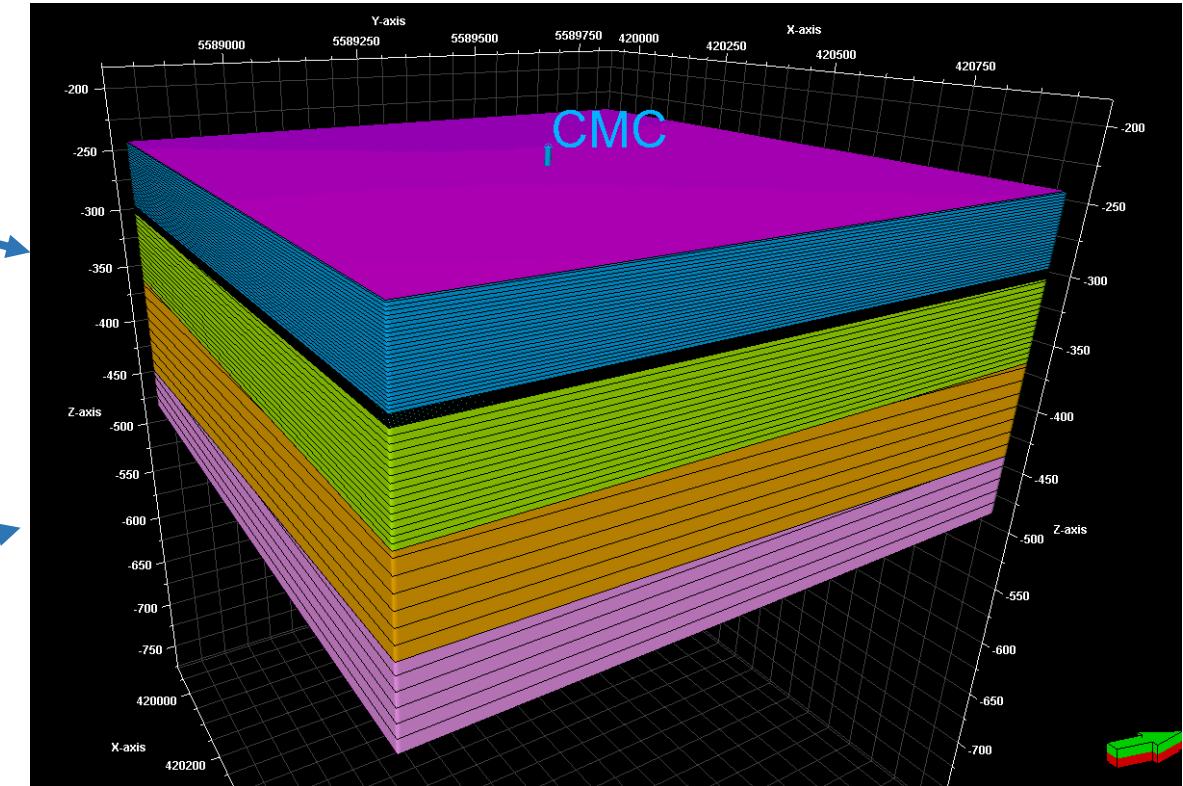
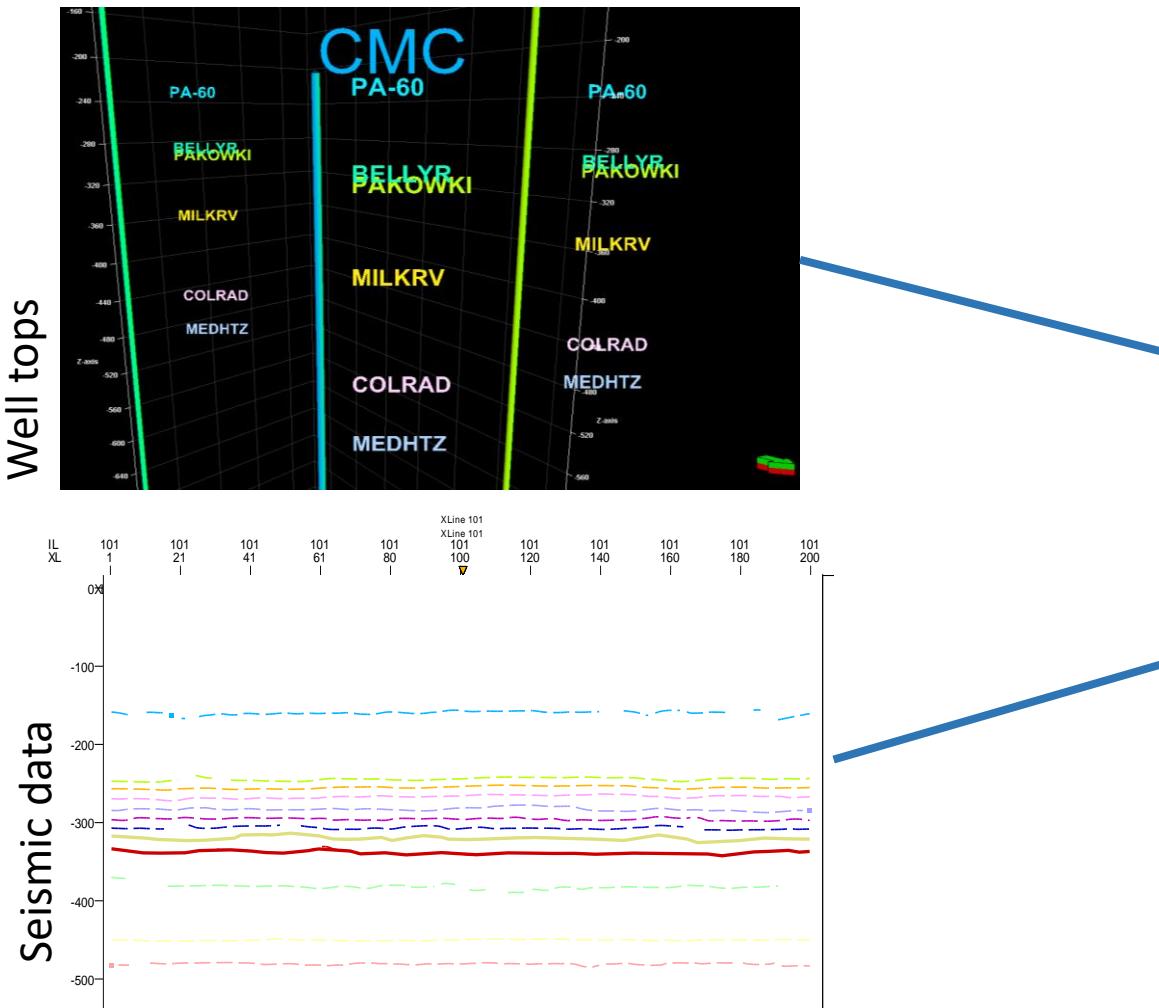
# Outline

- Introduction
- Reservoir simulation
- Rock physics and fluid substitution
- Velocity perturbation models
  - Solid
  - Diffusive
- Full waveform analysis and imaging (acoustic)
- Saturation and plume size influences in the seismic response
- Conclusions and acknowledgments

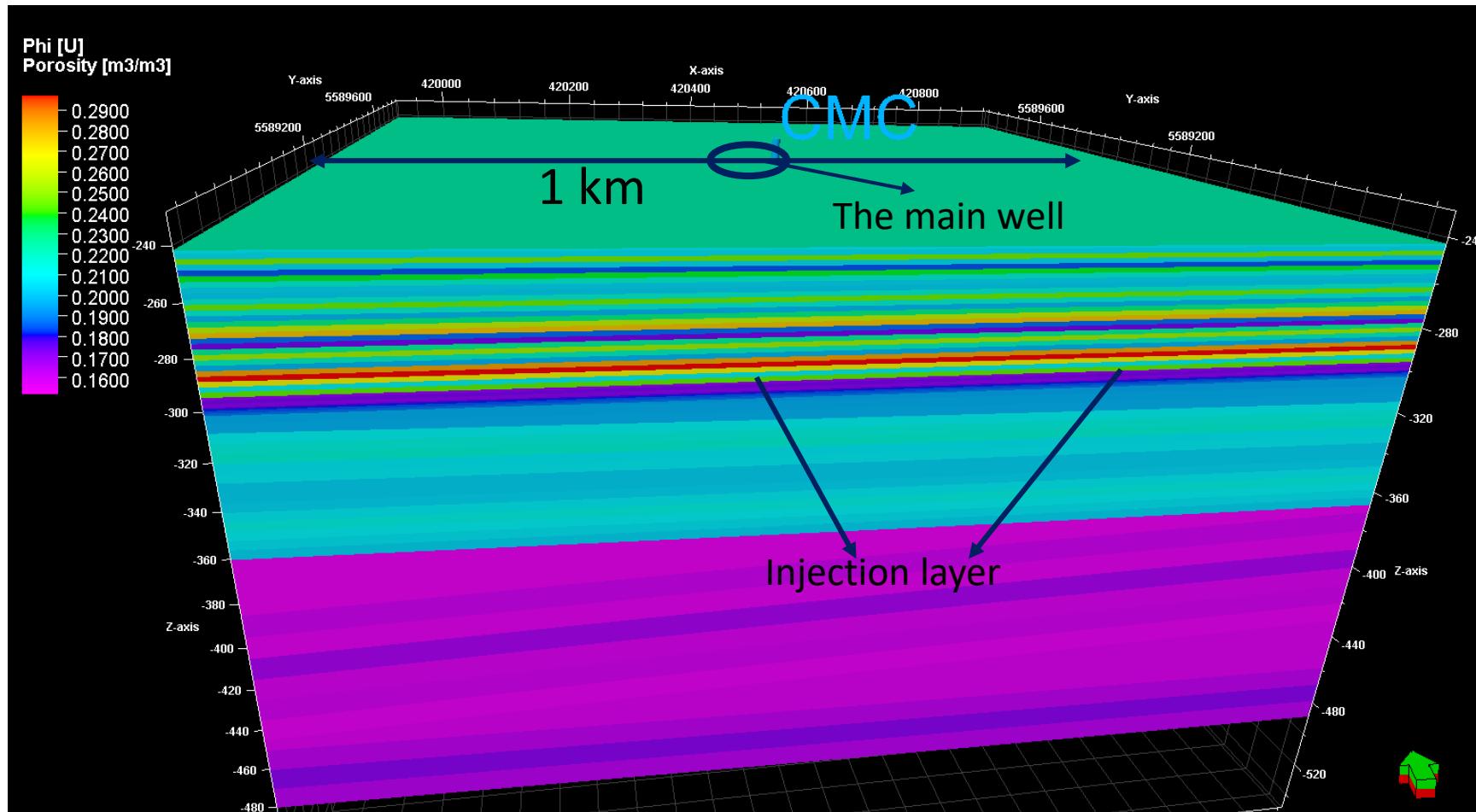
# The research workflow



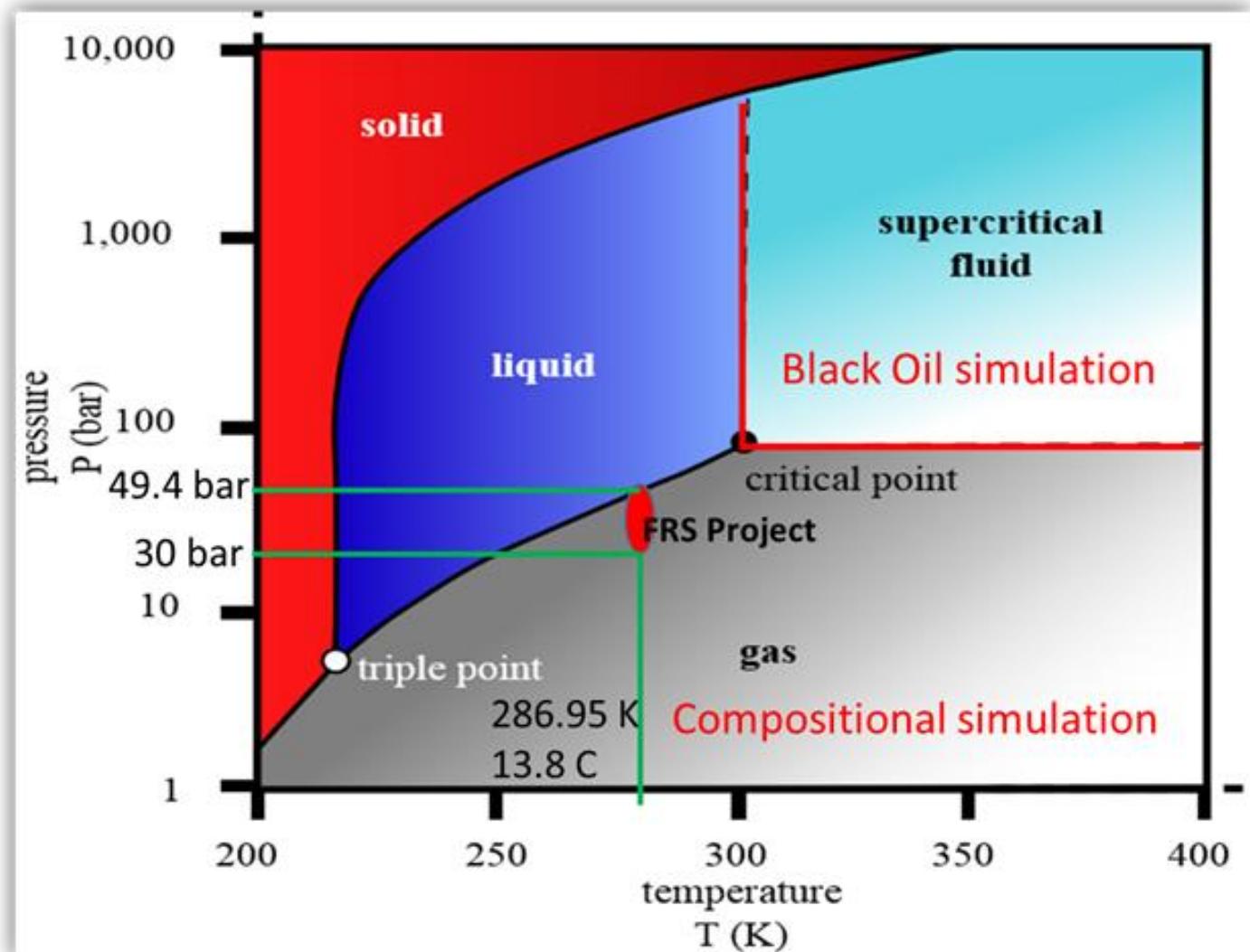
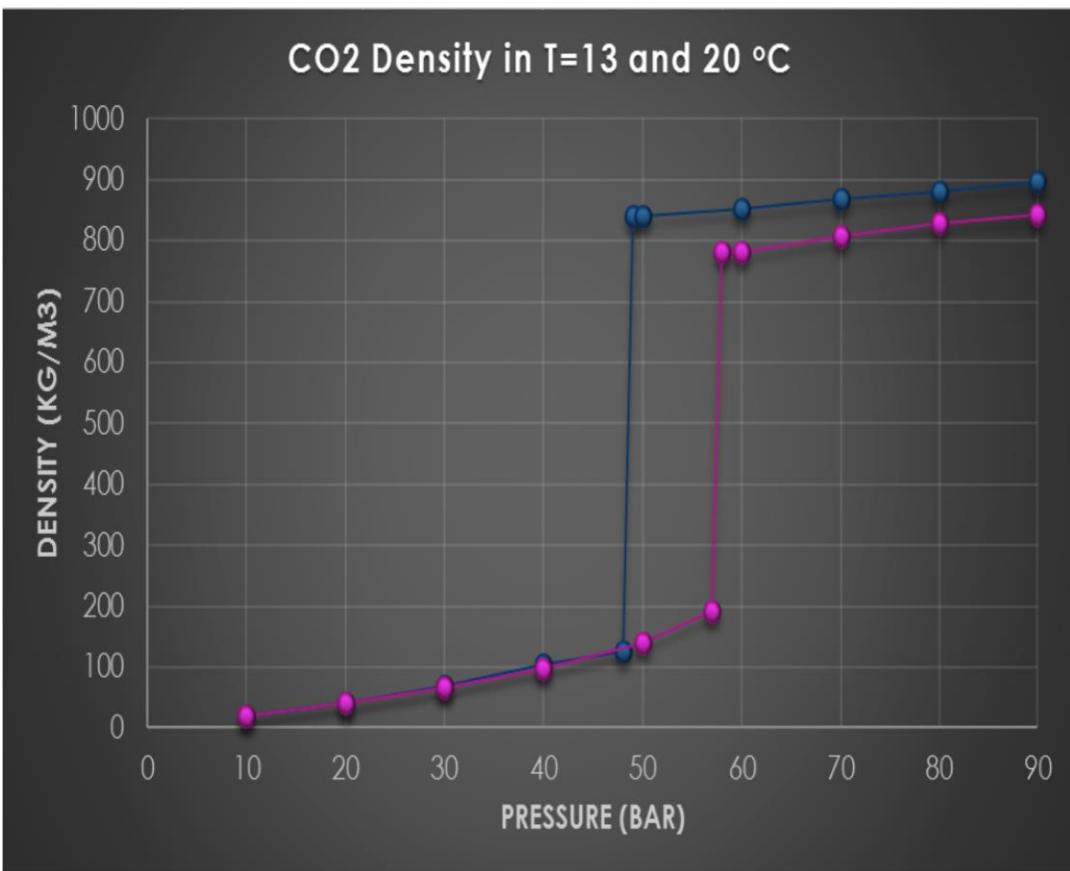
# The geometry of the formations



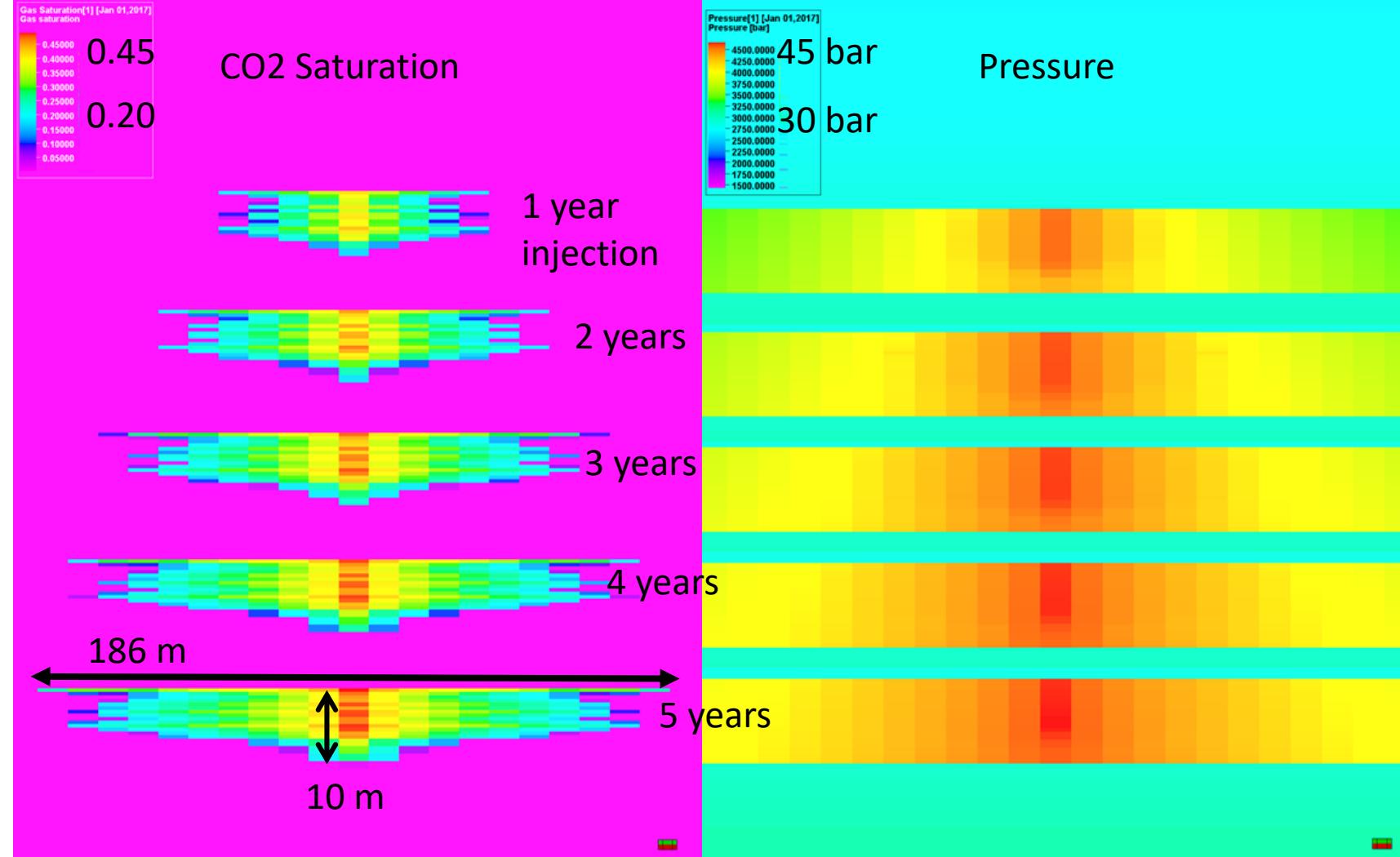
# Porosity geomodel



# CO<sub>2</sub> phase diagram

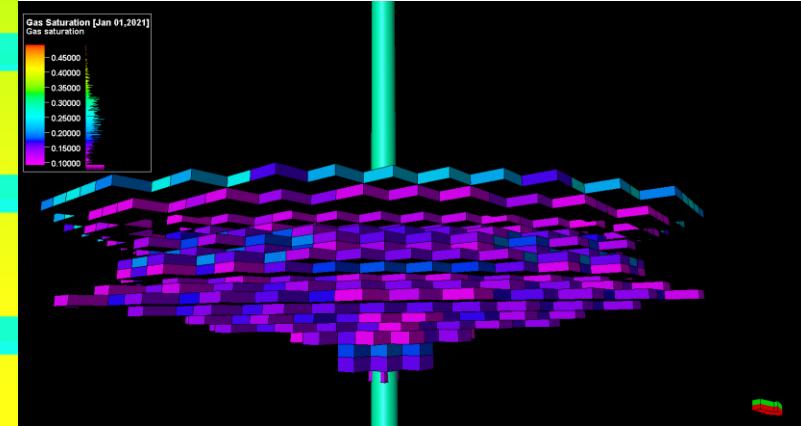


# The fluid simulation result

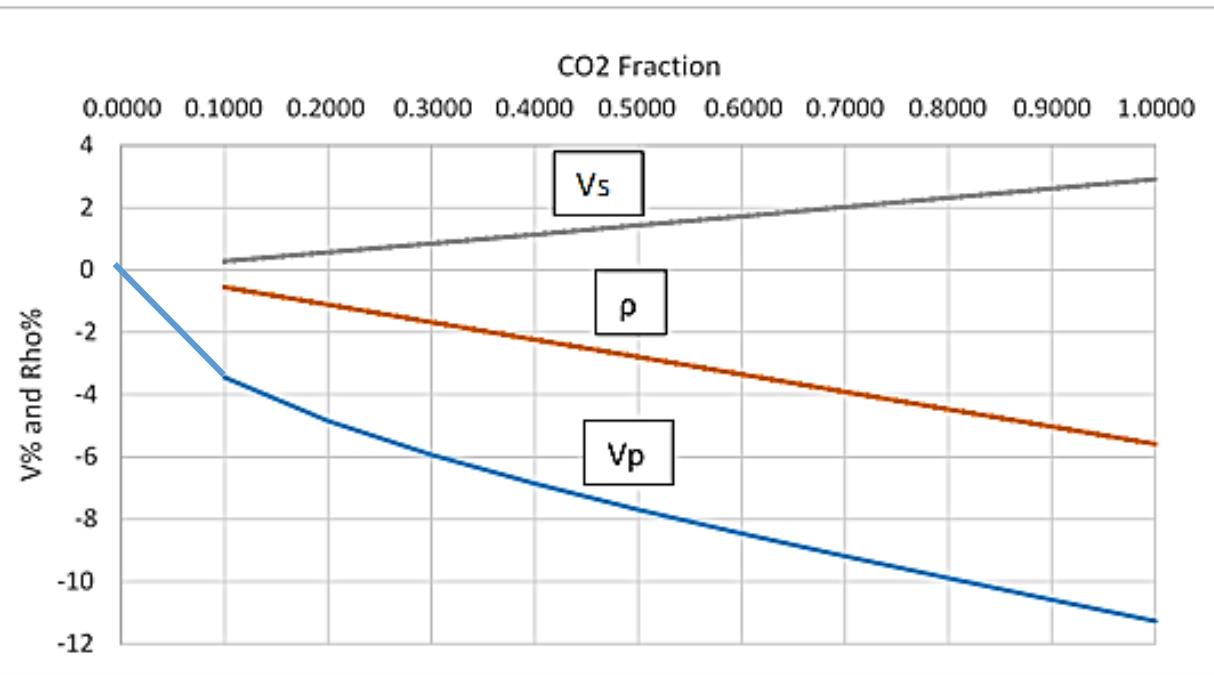


**Compositional simulator  
Unlimited boundaries  
condition**

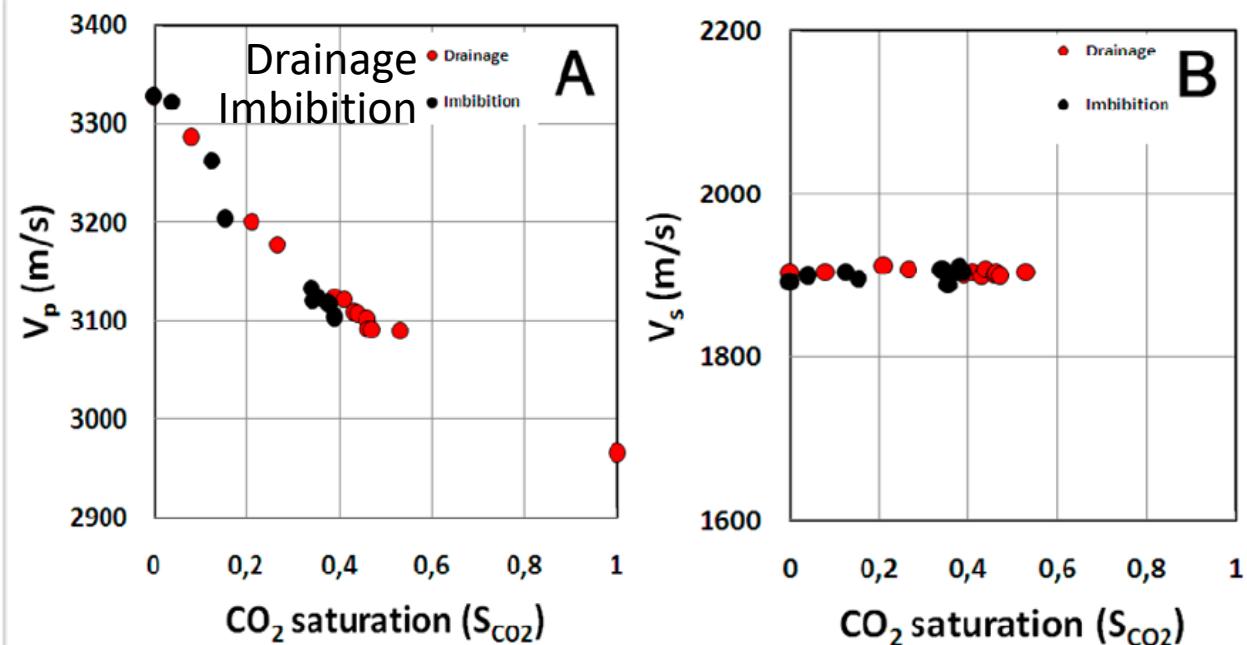
**Injection strategy:  
Five years injection  
Constant BHP=49.4 bar**



# Fluid substitution, CO<sub>2</sub> effect on the velocity

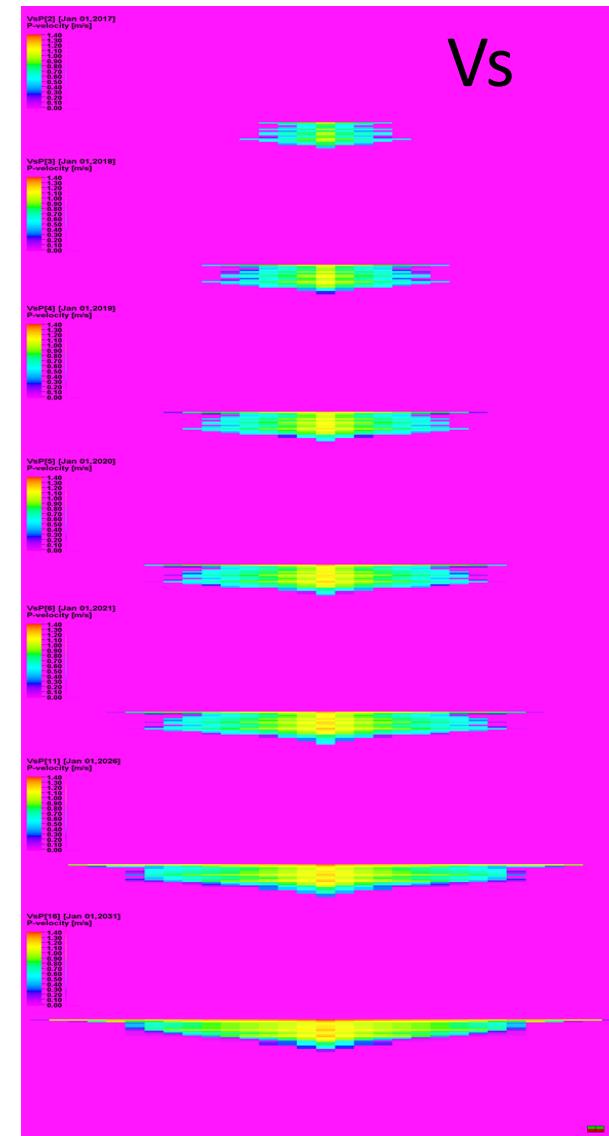
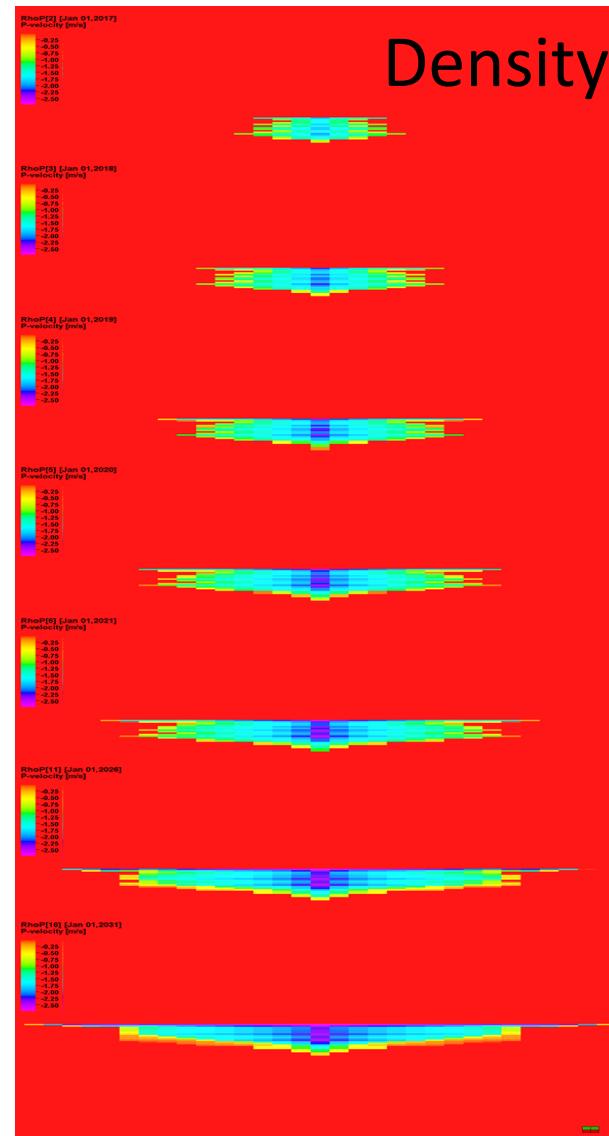
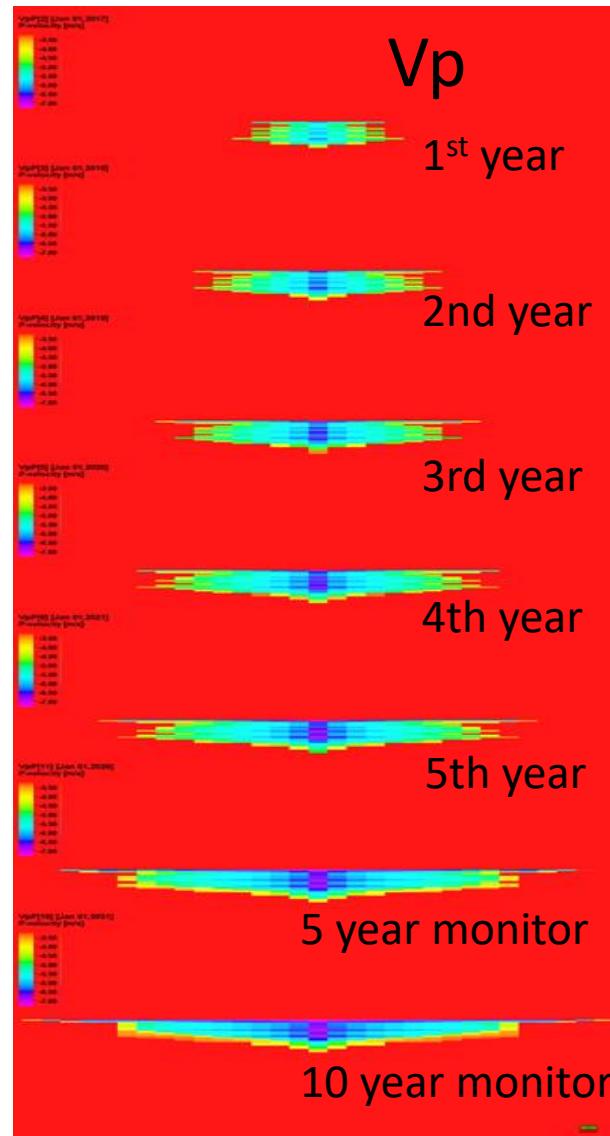


Fluid substitution effect

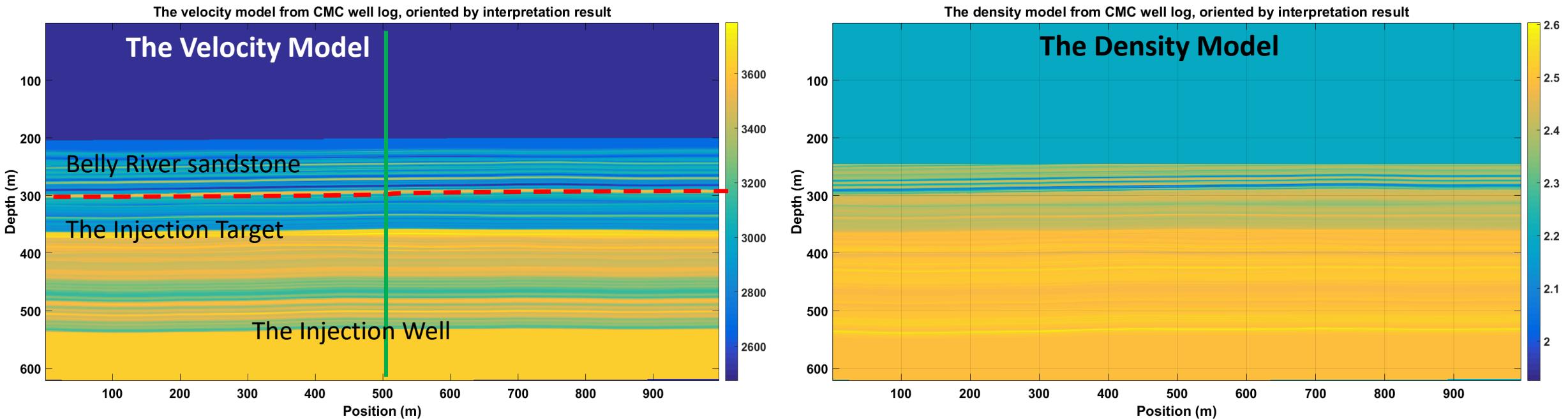


Lab test result for the CO<sub>2</sub> injection into the Sandstone (B.Alemo et al., 2011 )

# Vp, density and Vs in the reservoir during injection

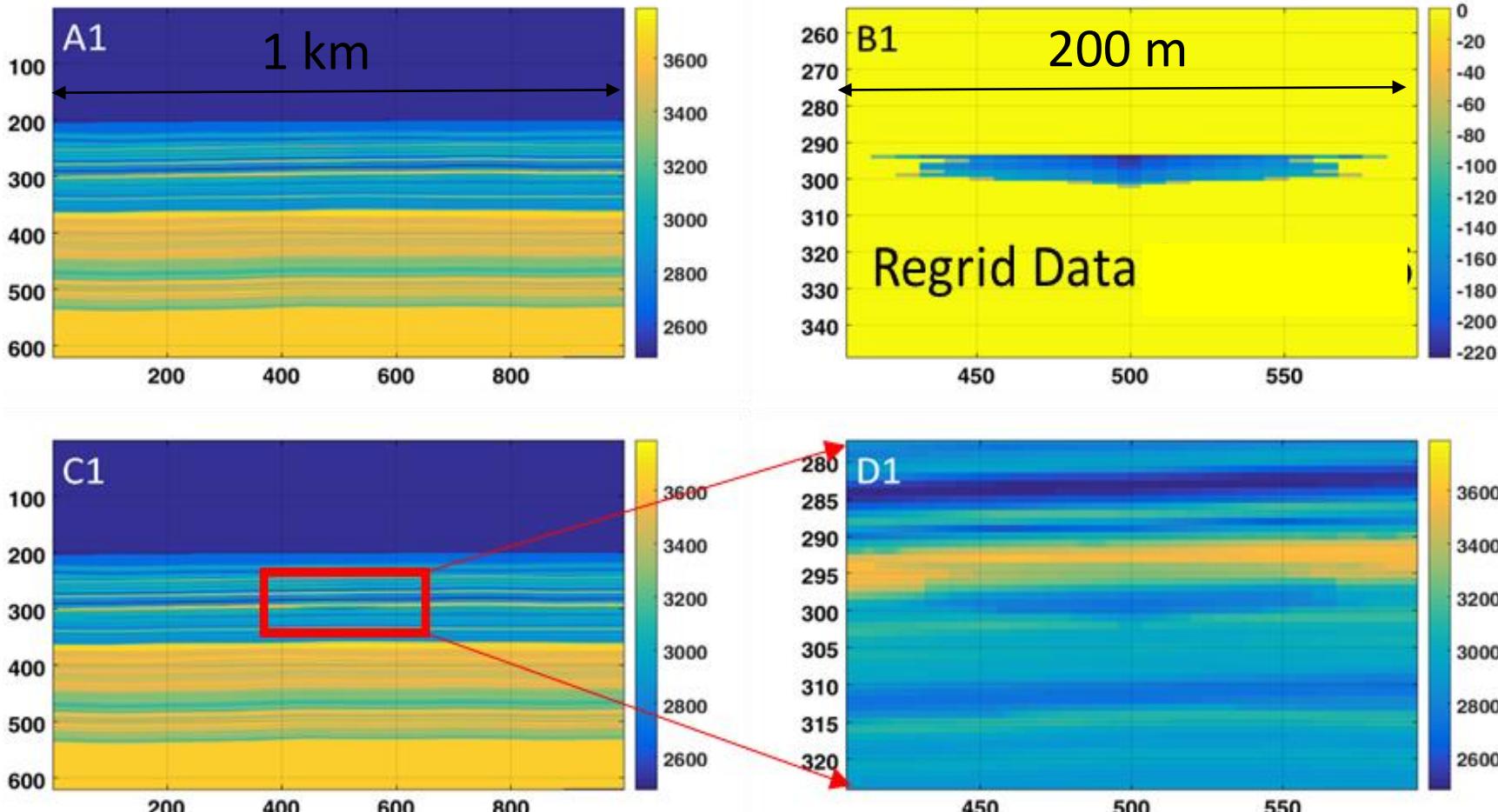


# The velocity and density models



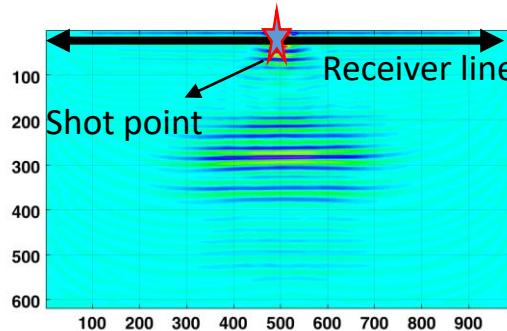
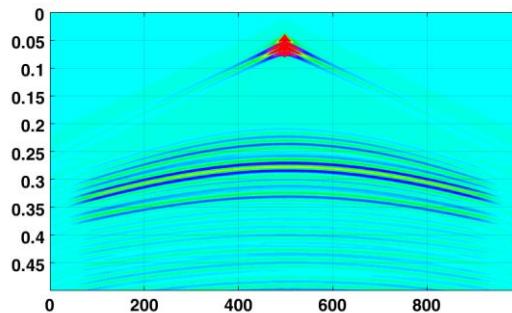
Layers geometry is based on seismic interpretation result  
The velocity and density are from CMC main well log data  
Model has 1\*1m cell size and geomodel made in Petrel

# The velocity perturbation due to the reservoir



# The seismic response of the reservoir

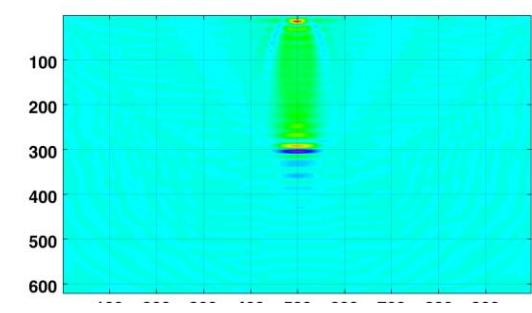
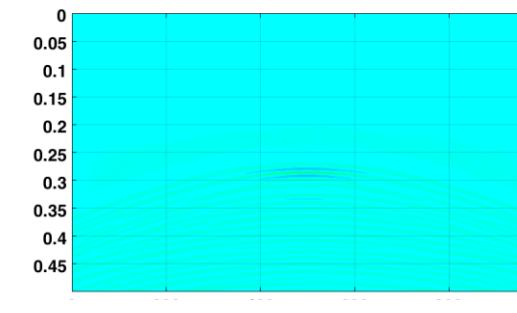
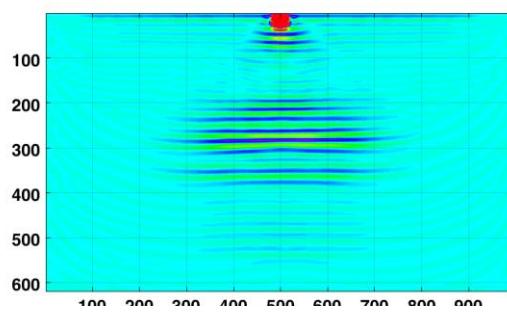
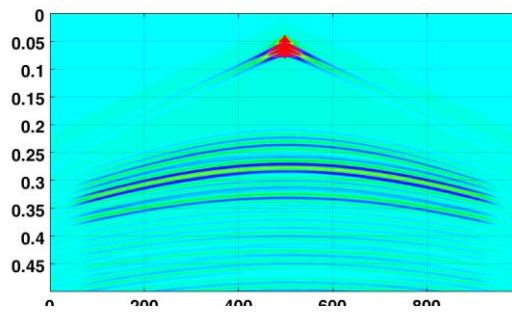
Baseline



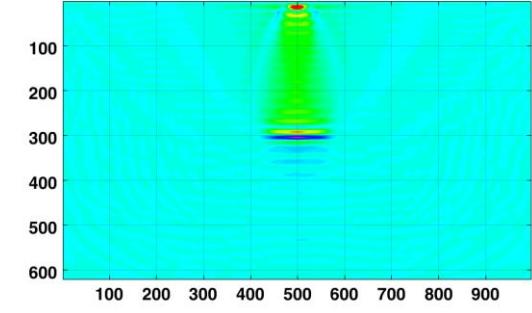
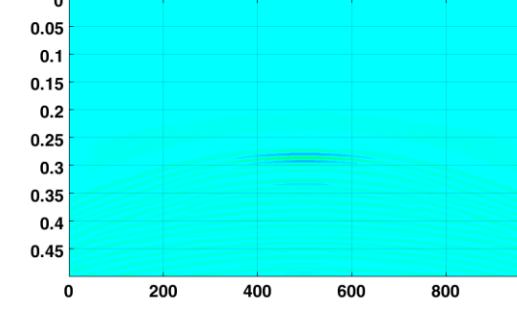
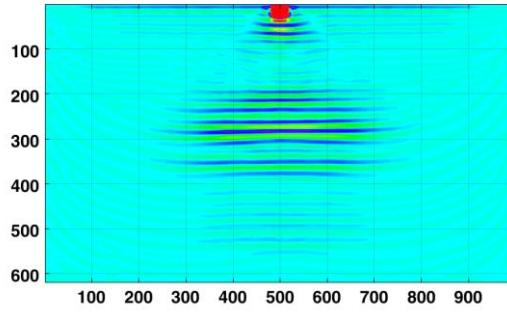
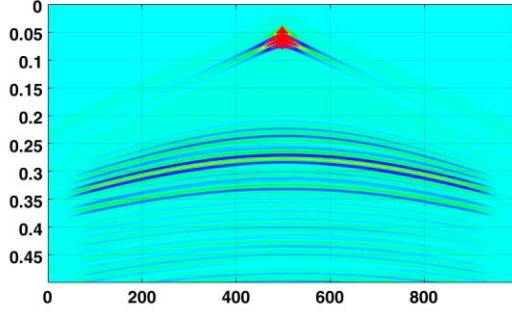
SM(20xx)-SM(Base)

RTM(SM(20xx)-RTM(SM(Base))

2018

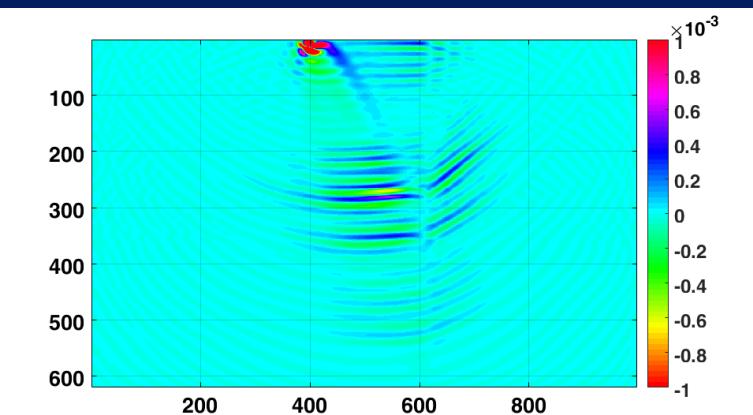
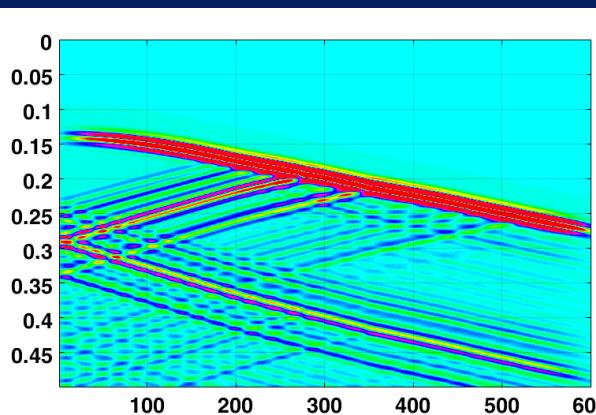


2021

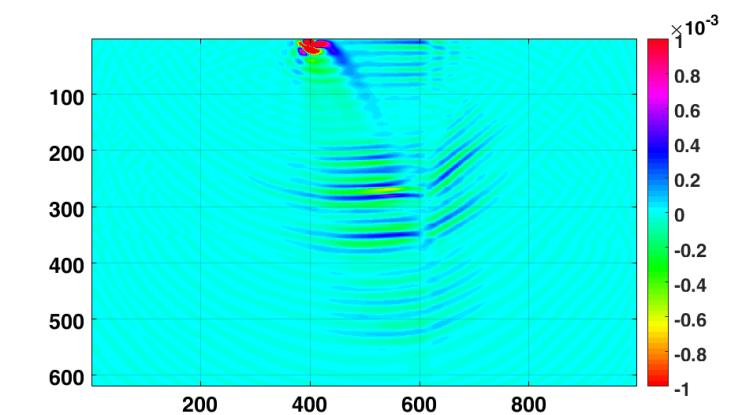
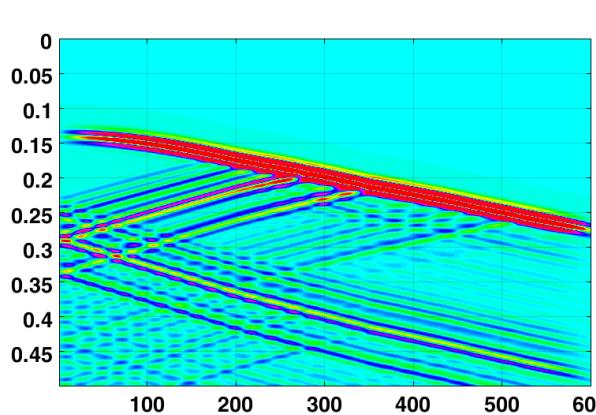


# VSP models

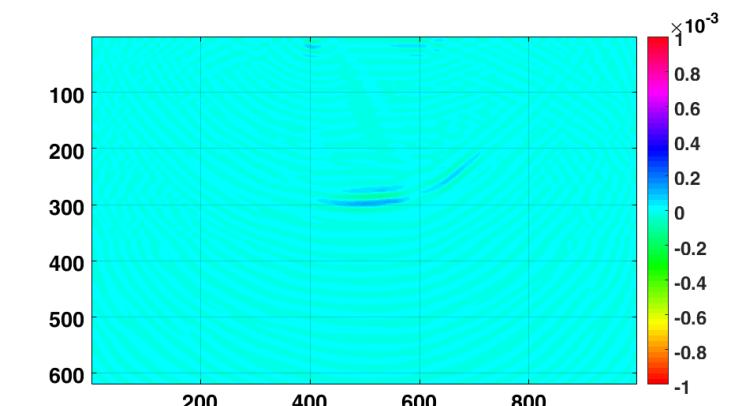
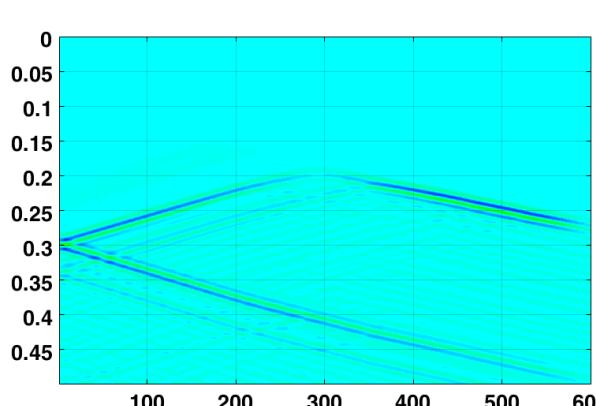
Baseline



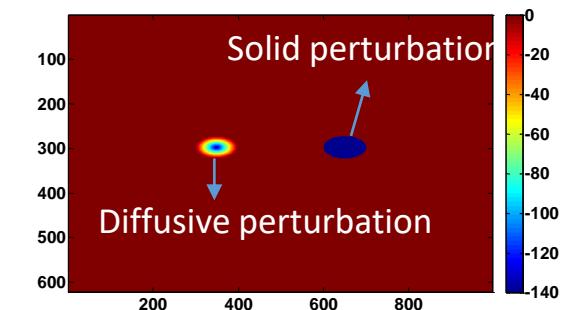
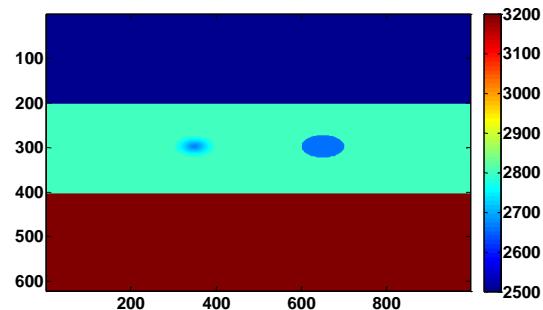
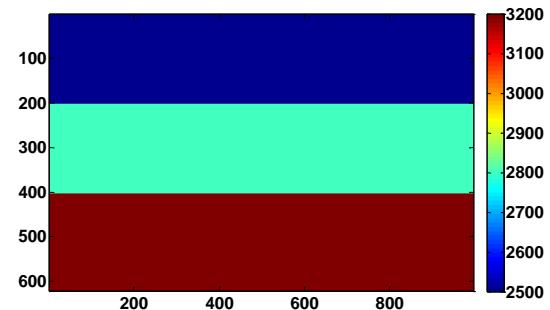
2021 (5-year injection)



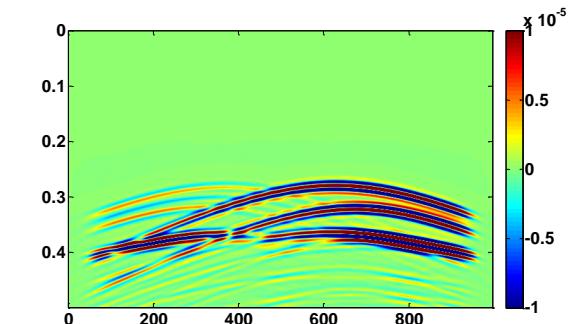
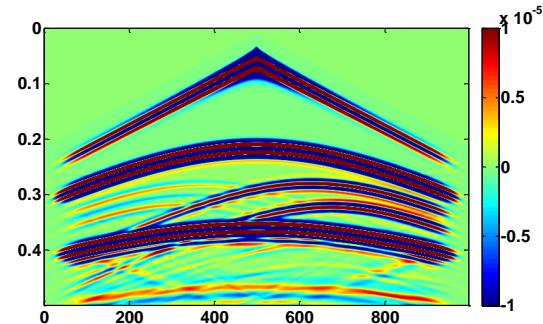
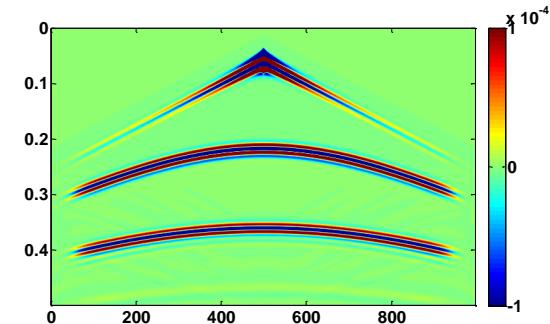
Difference



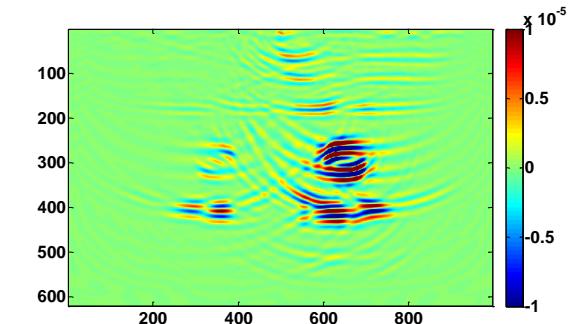
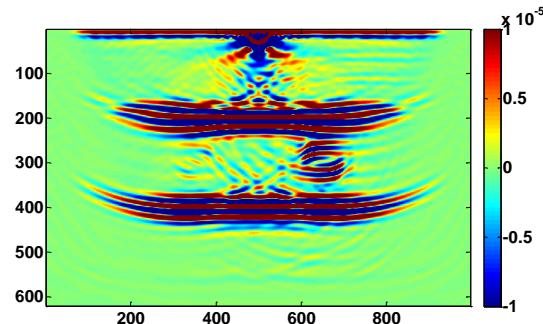
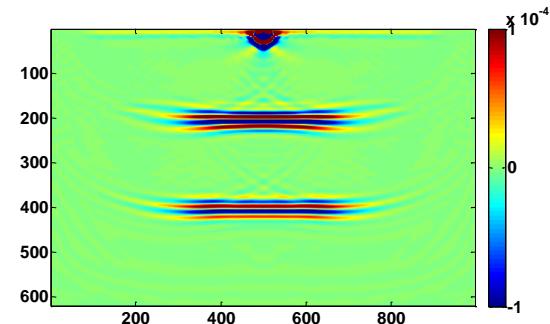
# Seismic response for solid and diffusive velocity



V Model

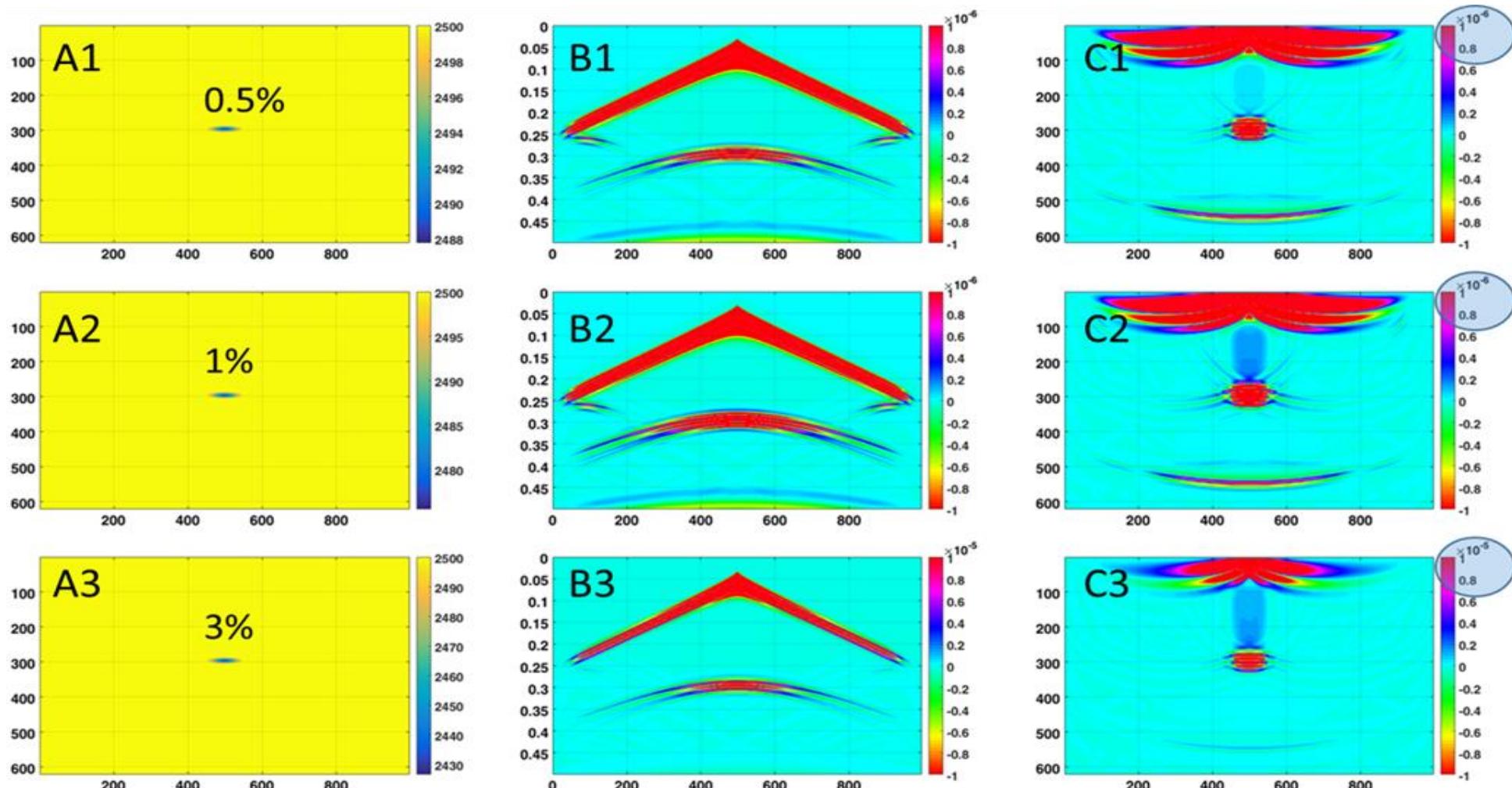


Pressure Component

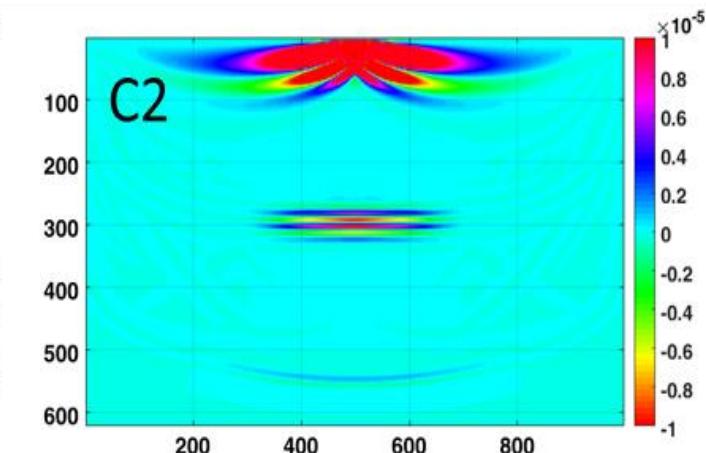
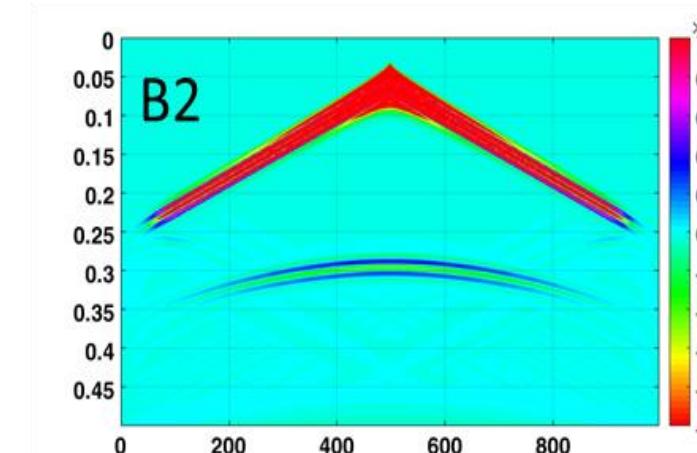
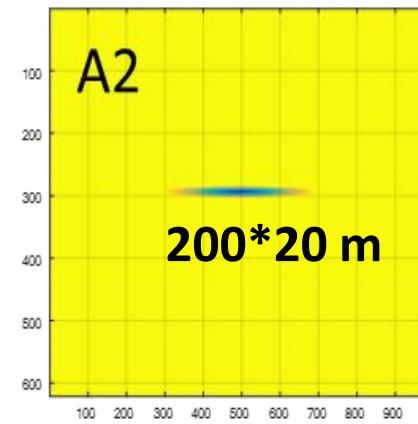
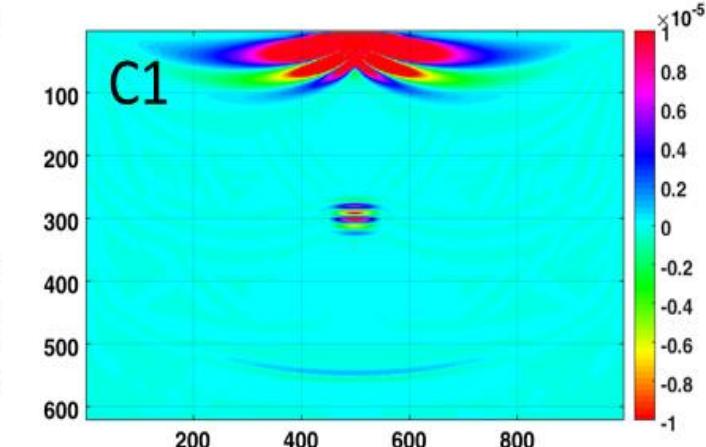
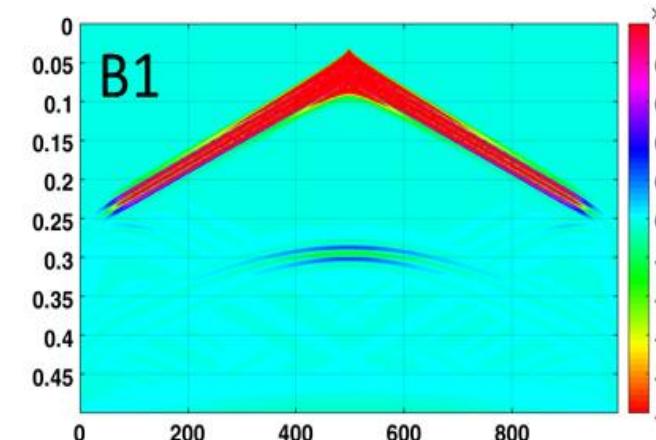
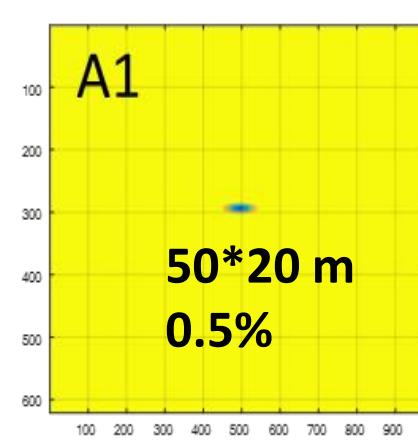


RTM

# Saturation and velocity change effect

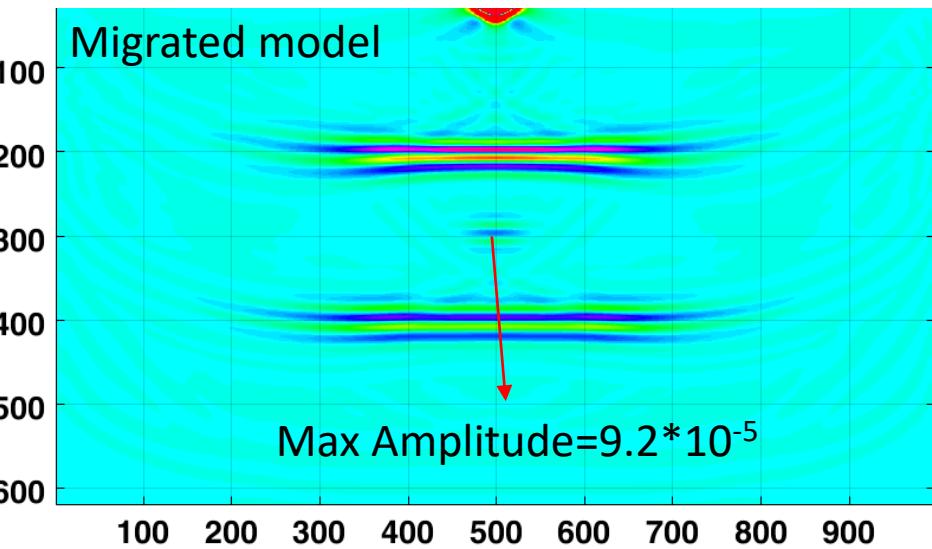
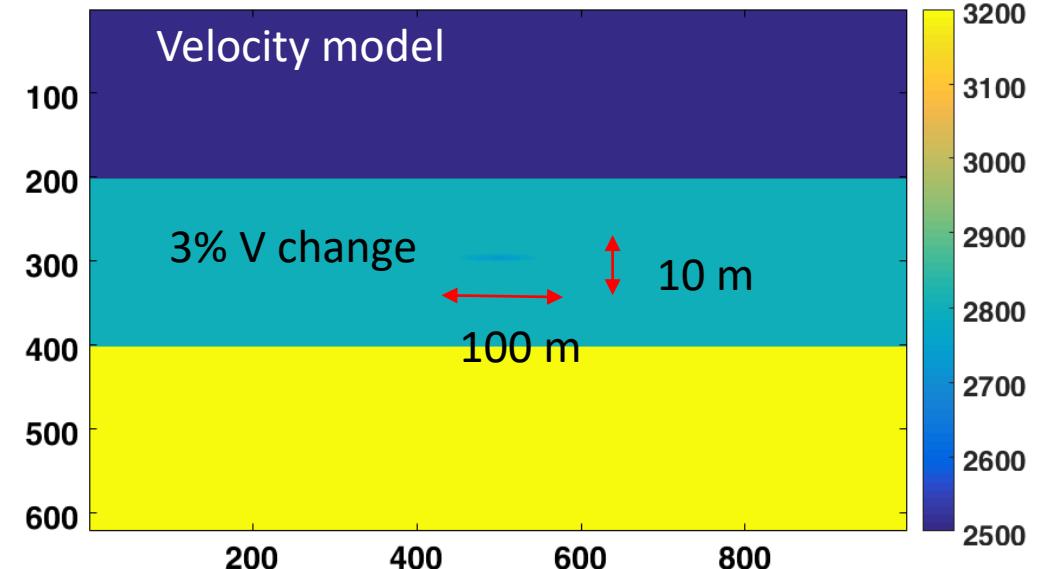
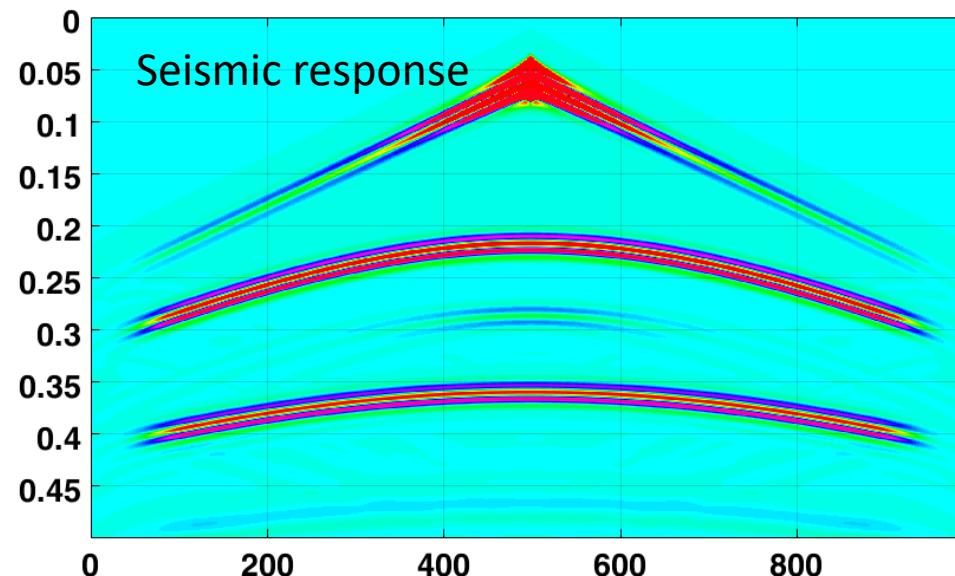


# The plume size effect



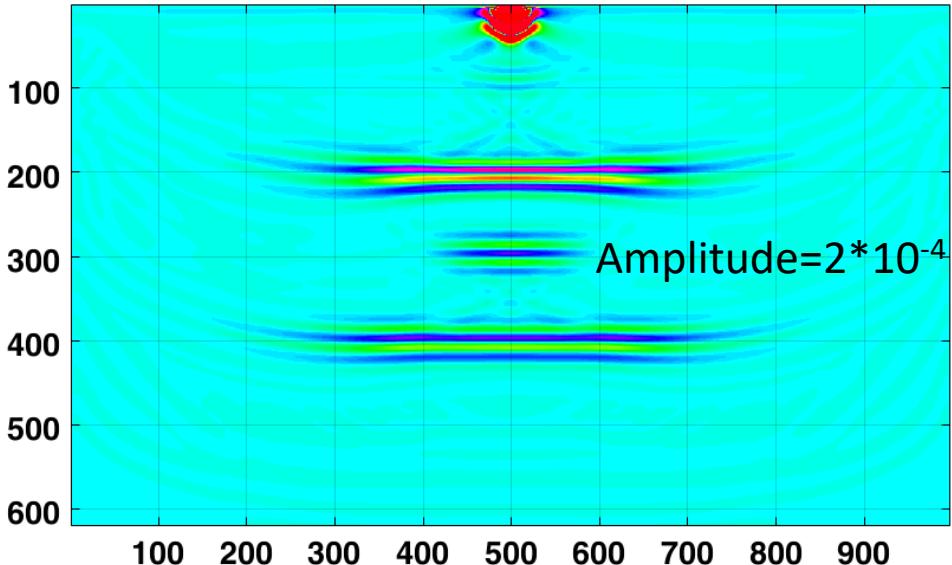
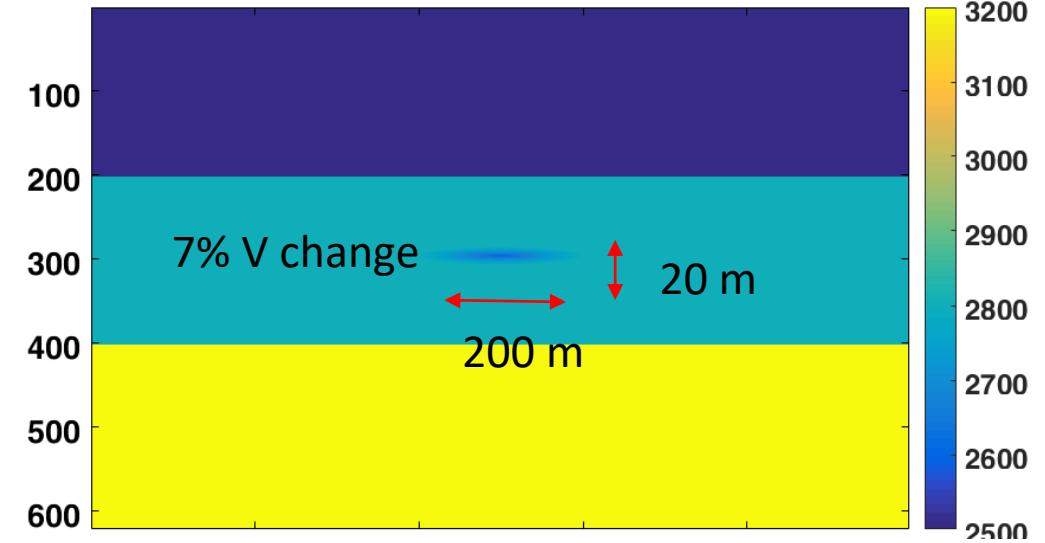
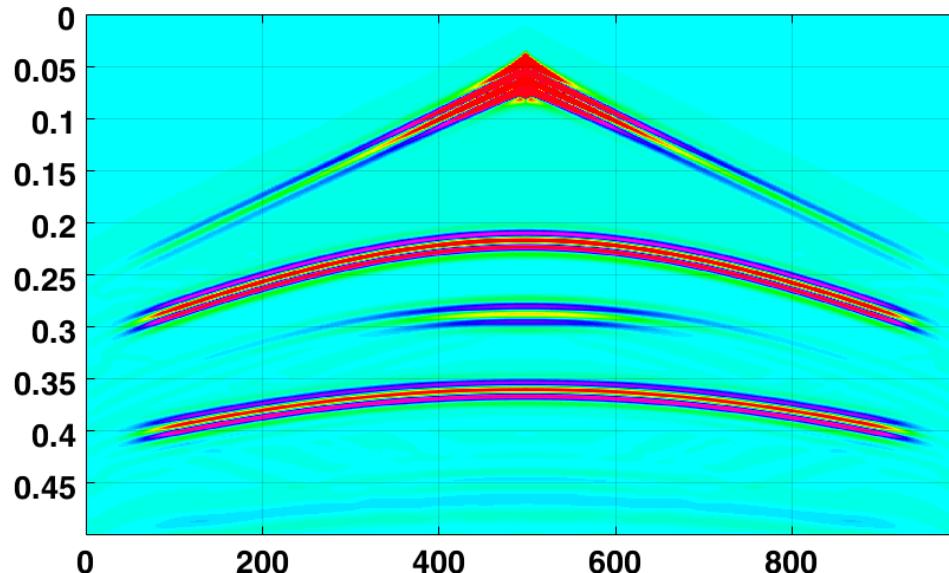
# 3-layer model with diffusive velocity

100\*10 m – 3%

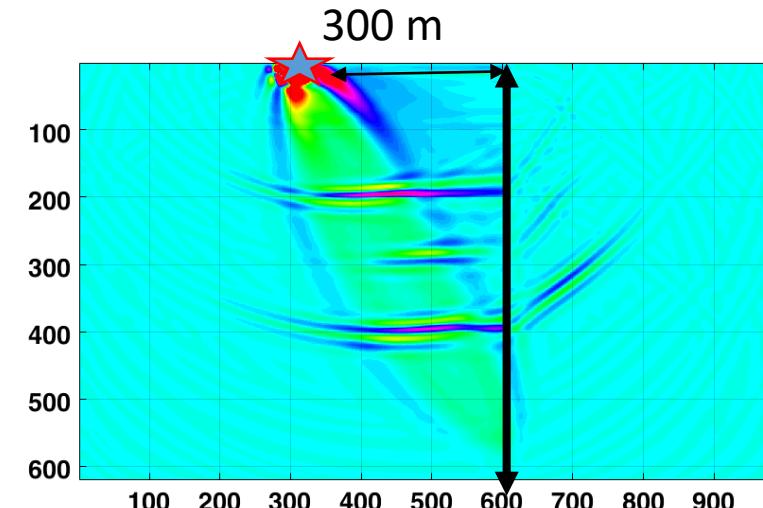
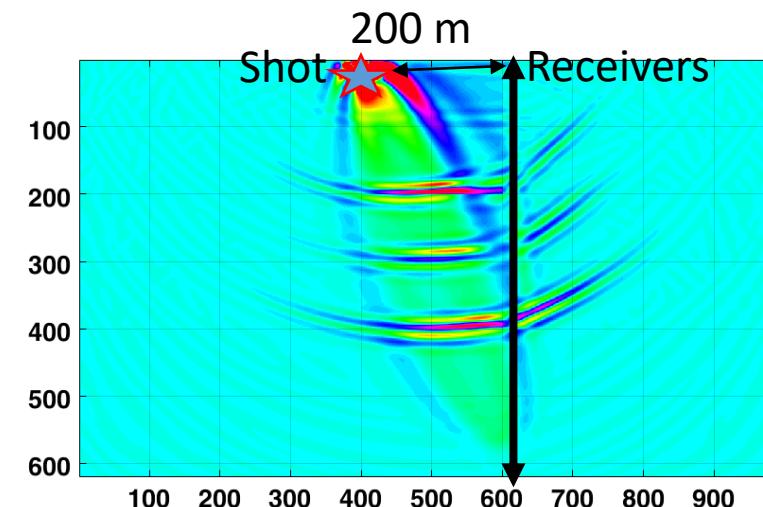
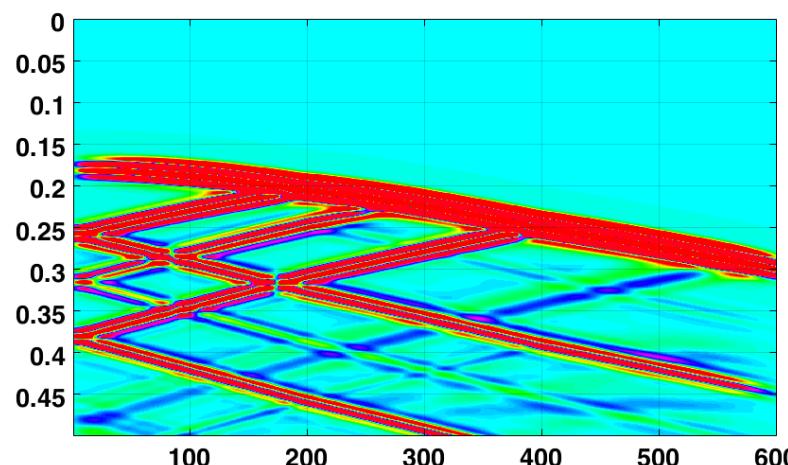
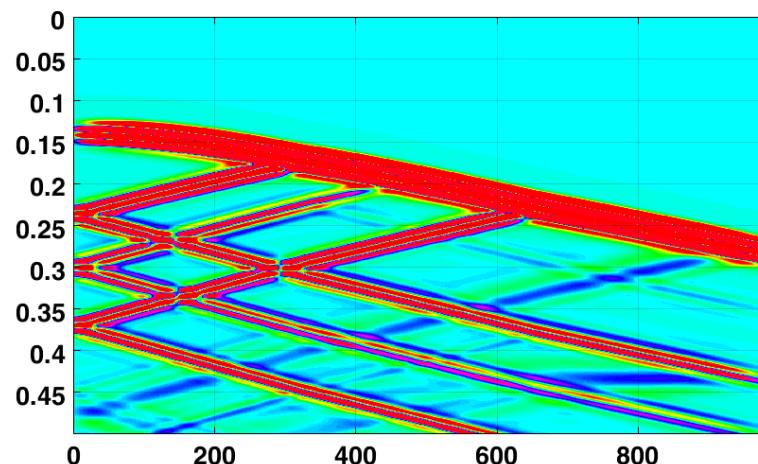


# 3-layer model with diffusive velocity

200\*20 m – 7%



# Narrow vs wide offset VSP models



# Conclusions

- The time-lapse seismic response of diffusive zone shows small changes in the amplitude compared to similar solid block changes.
- Because of velocity decrease in the reservoir , a time delay effect was detected in reflectors below the reservoir, so we should consider the changes in travel time of transmitted waveforms as an alternative framework for a full waveform study.
- Surface seismic acquisition is a suitable method for the shape estimation of the plume, but well seismic data has better amplitude and frequency content, so VSP are most useful for the small changes of fluid saturation.
- The Migrated data has a better amplitude condition , so interpretation is possible with the full migrated data.

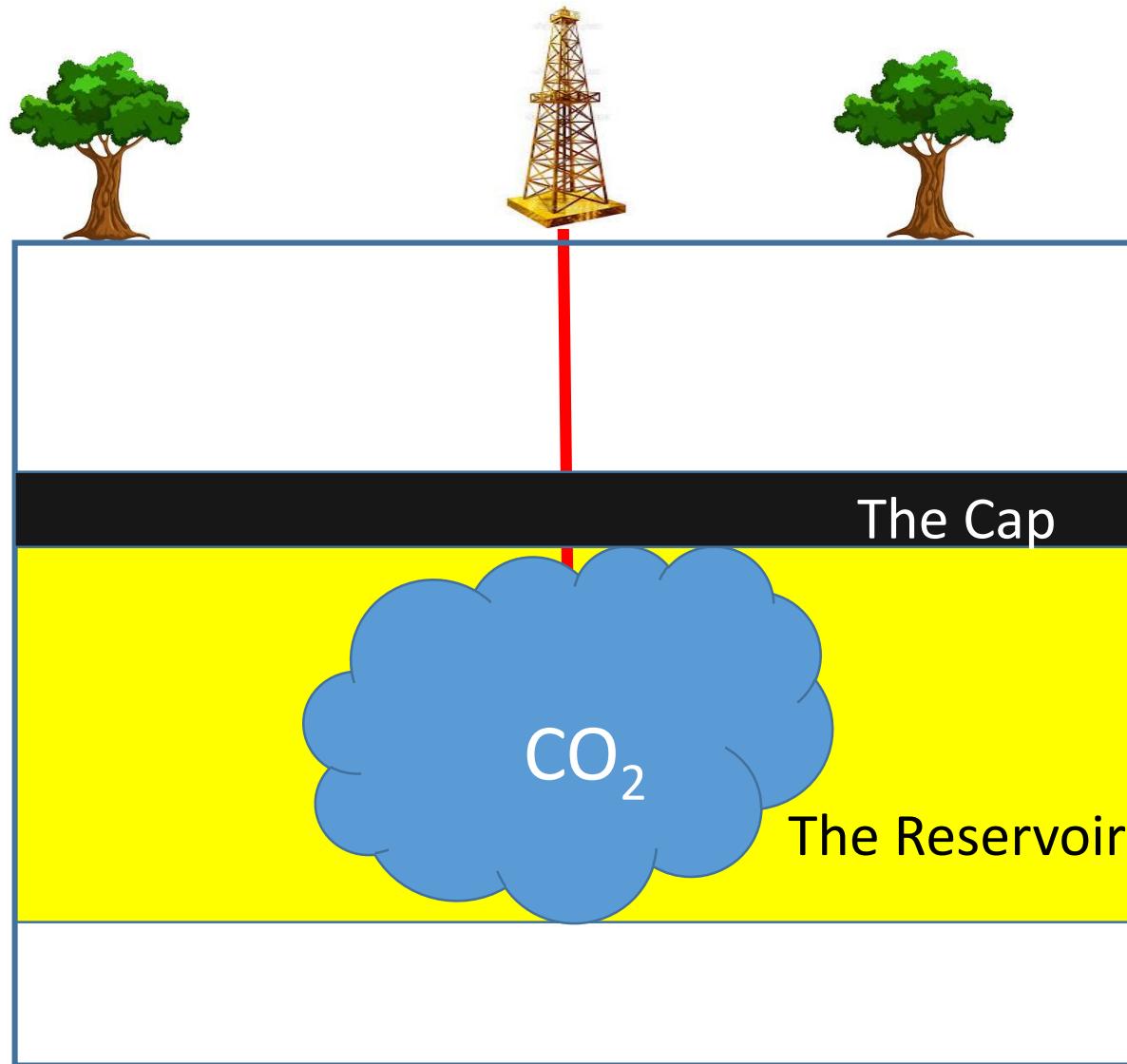
# Acknowledgments

- Industrial sponsors who support CREWES
- CMC Research Institutes, Inc.
- NSERC Grant
- CREWES team and students
- Helen Isaac for the seismic data processing

# Full Waveform Inversion and plume model

- The basic equations used in this study is the acoustic velocity-stress wave equation approach.
- Wave equation are solved by Finite Difference Time Domain in an explicit scheme. 2<sup>nd</sup> order in time and 4<sup>th</sup> order in space, staggered grid in a leap frog scheme

# Reservoir Geophysics

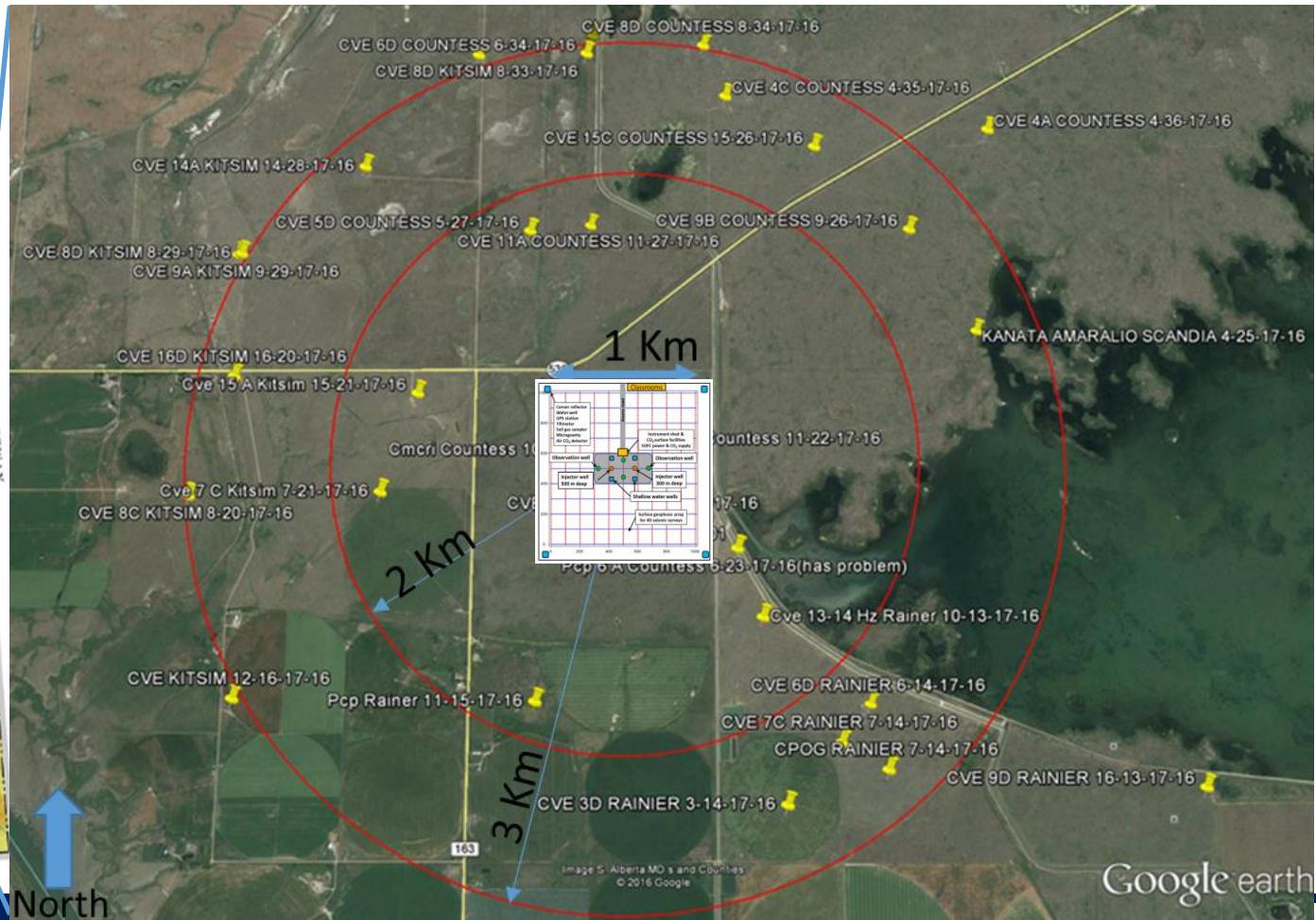
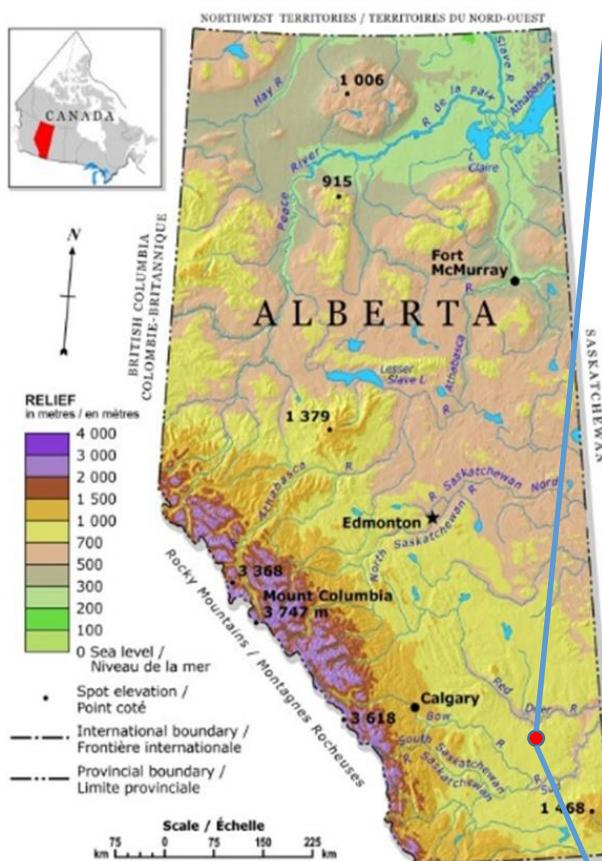


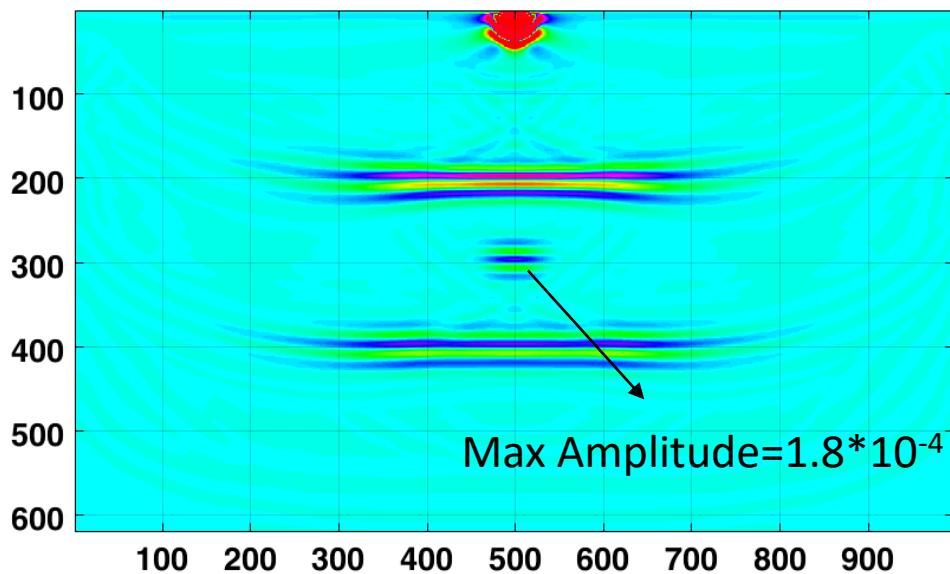
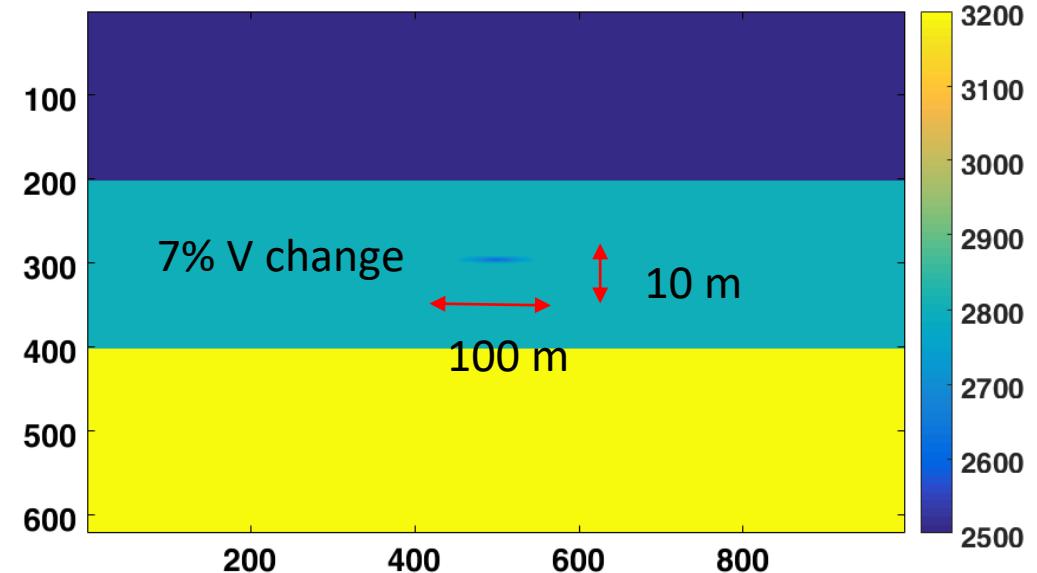
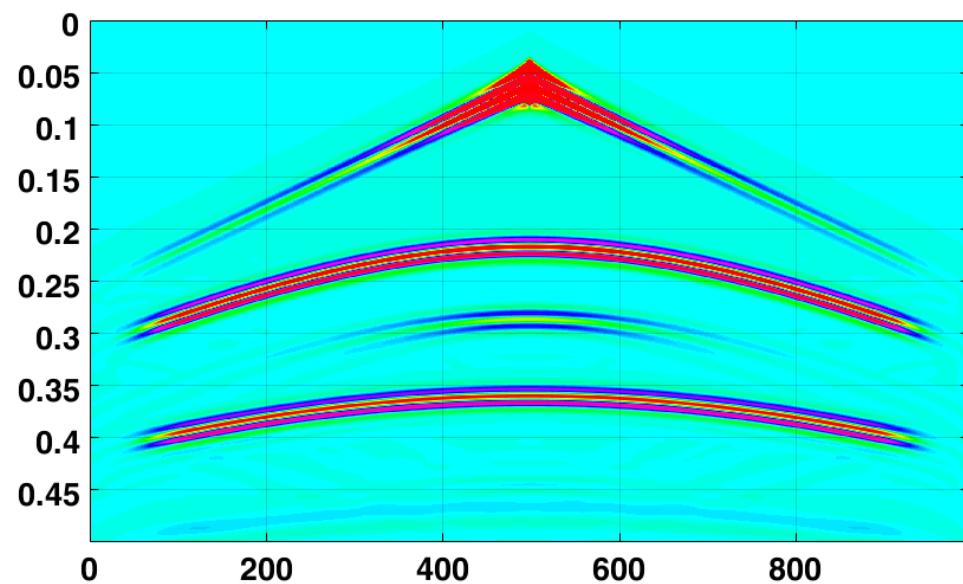
Plume Shape ~  $f(k, \phi, \text{Injection rate})$

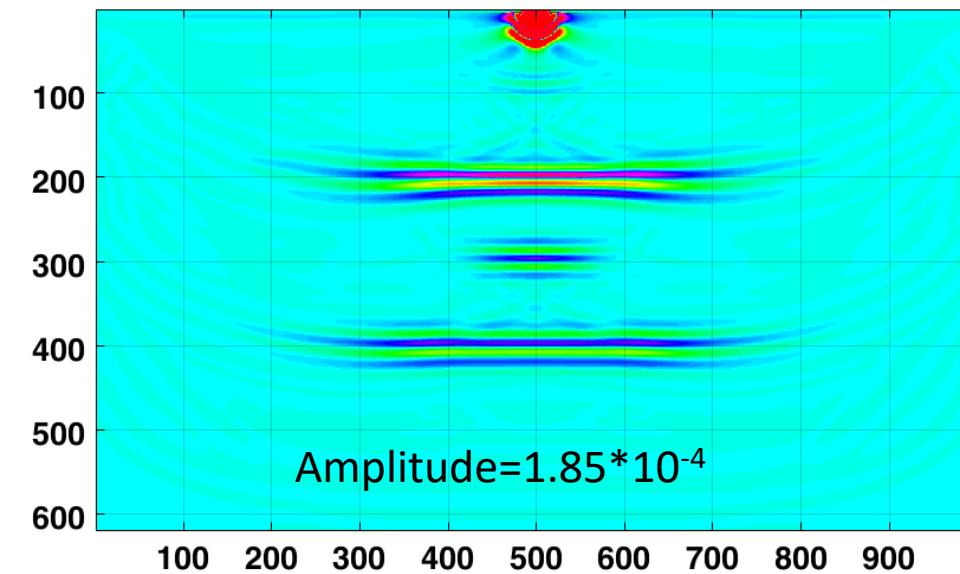
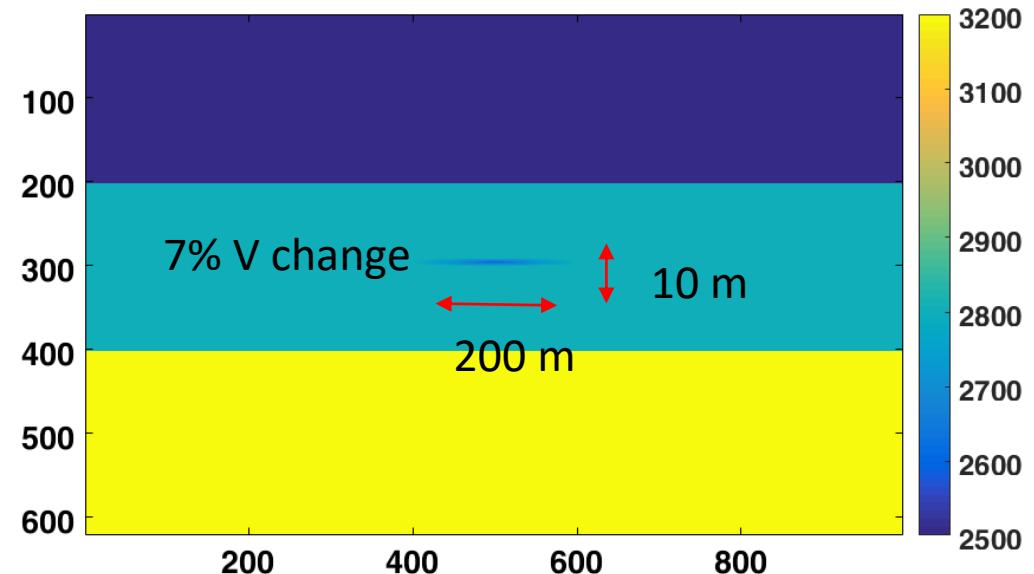
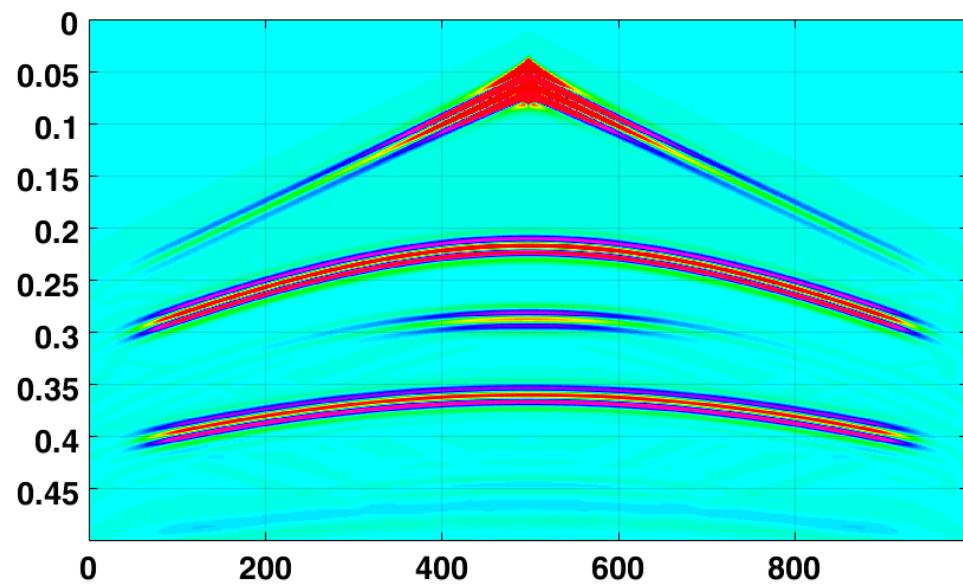
Velocity and density change

$$V \sim f(K_m, K_f1, K_f2, K_d, \phi, k)$$

$$\text{Density} \sim f(\rho_m, \rho_f1, \rho_f2, \phi)$$







# Theory of modeling and imaging

2D Acoustic approximation of wave propagation

$$\left. \begin{aligned} \frac{\partial u}{\partial t} &= -\frac{1}{\rho} \frac{\partial p}{\partial x}, \\ \frac{\partial v}{\partial t} &= -\frac{1}{\rho} \frac{\partial p}{\partial z}, \\ \frac{\partial p}{\partial t} &= -\rho v_p^2 \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial z} \right), \end{aligned} \right\}$$

*Euler*

*Continuity*

where,

$I(\vec{x})$  is the migrated image in subsurface coordinate

$\vec{x} = (x, z)$

$T_{max}$  is maximum recorded time,

$S(t, \vec{x})$  is forward propagated source and

$r(t, \vec{x})$  is the backward propagated receivers. The subscripts

$p$ ,  $u$  and  $v$

correspond to three images for pressure and displacements obtained by imaging conditions.

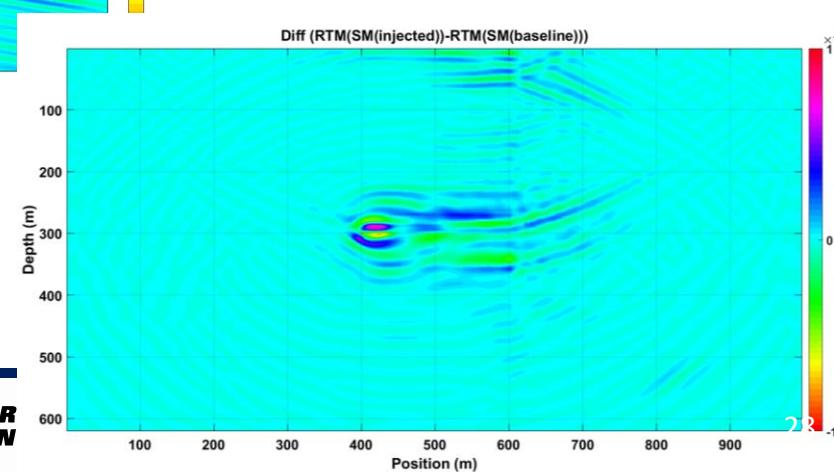
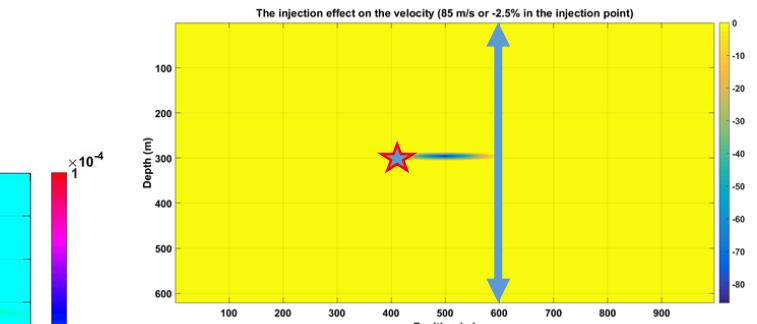
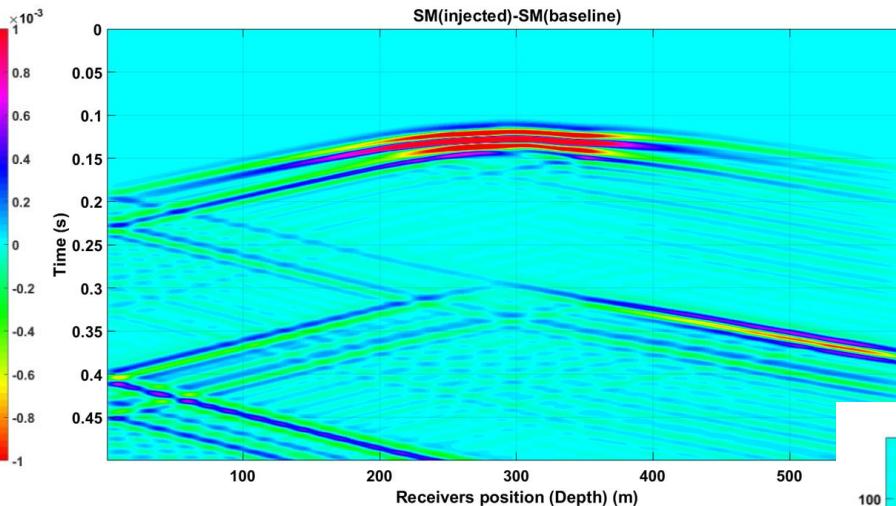
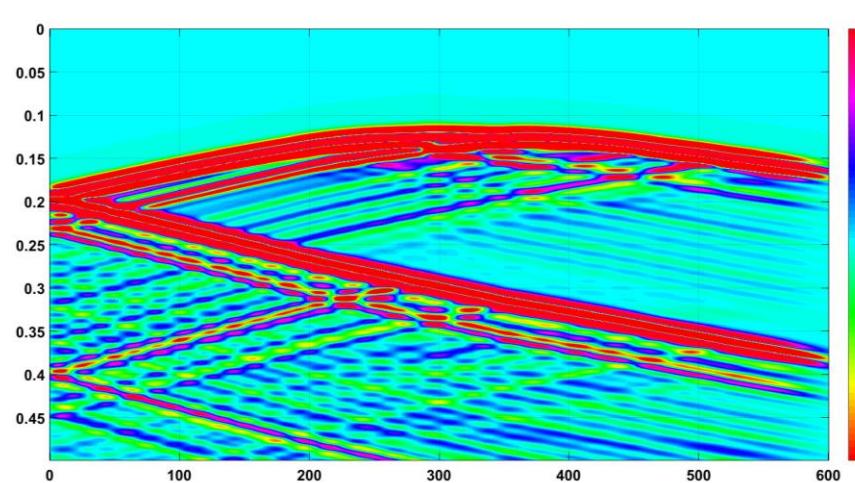
Migration and inversion framework

$$I_u(\vec{x}) = \int_0^{T_{max}} S_u(t, \vec{x}) r_u(t, \vec{x}) dt,$$

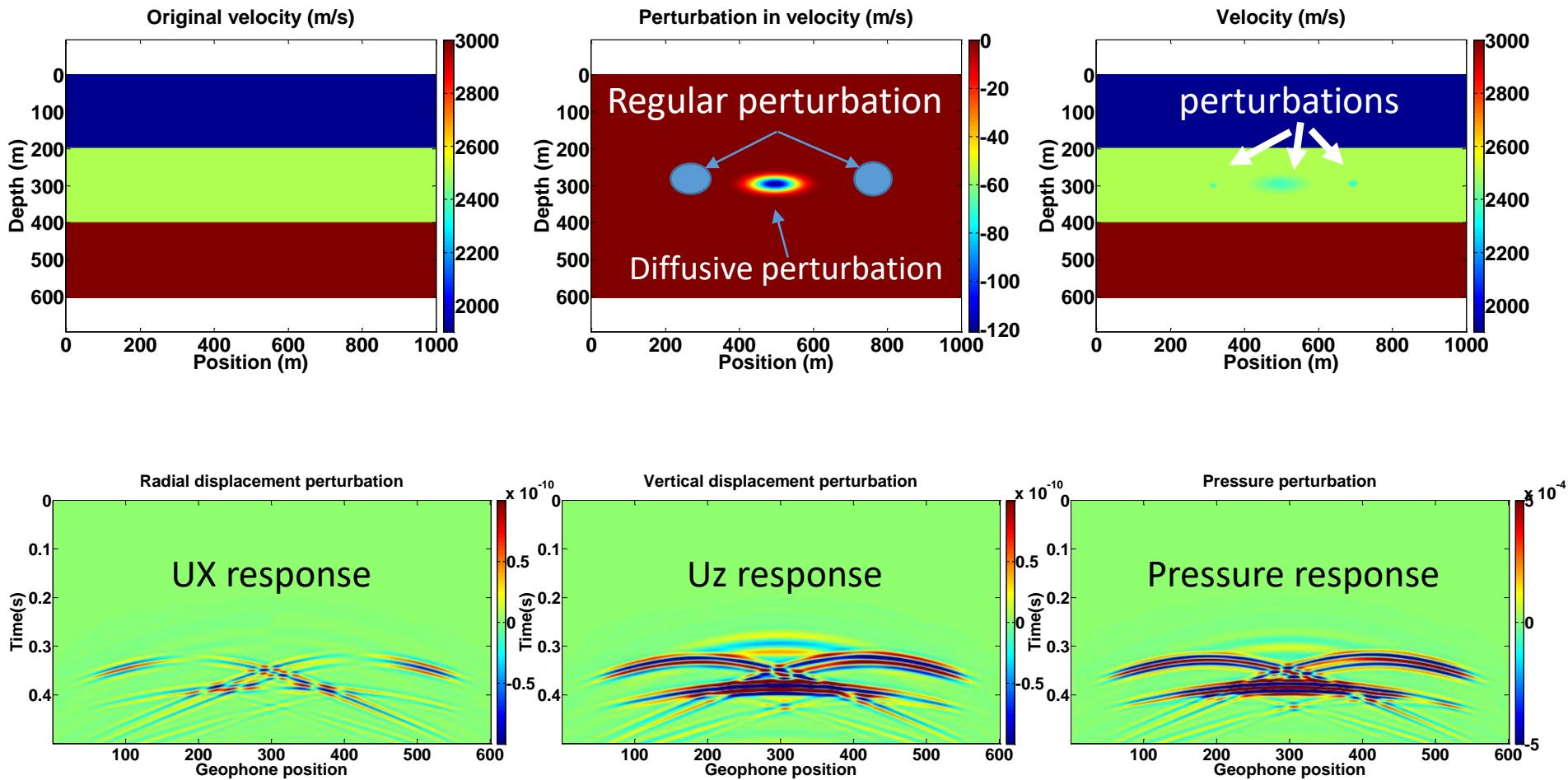
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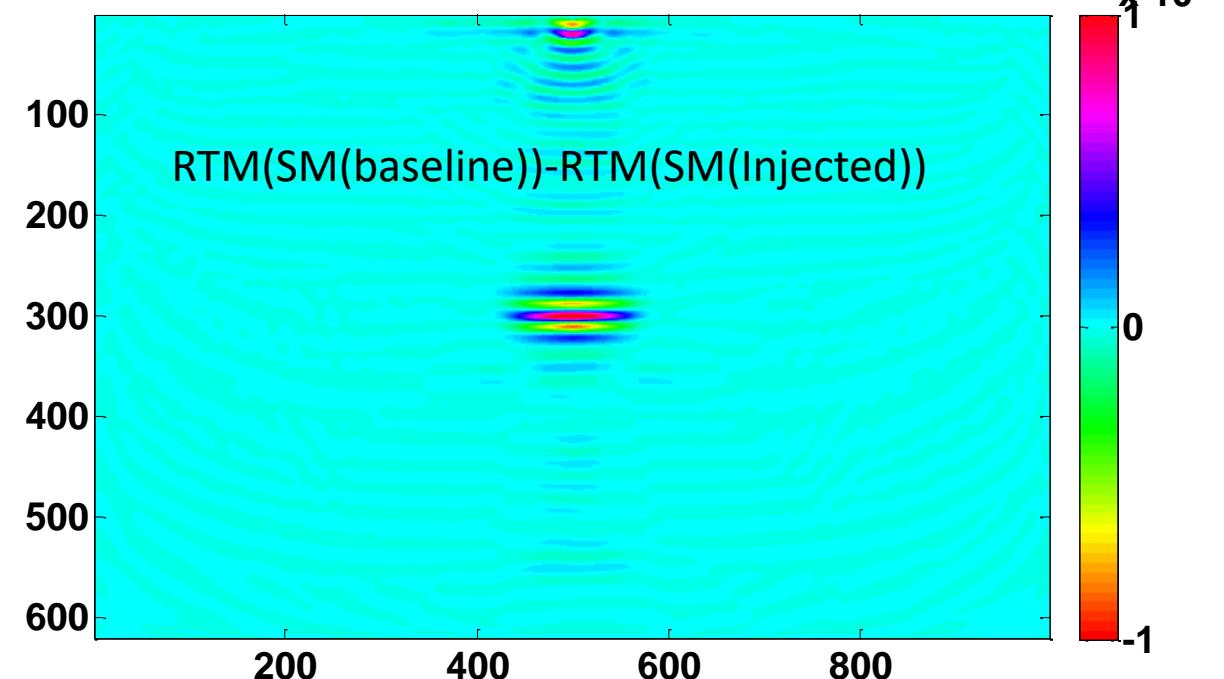
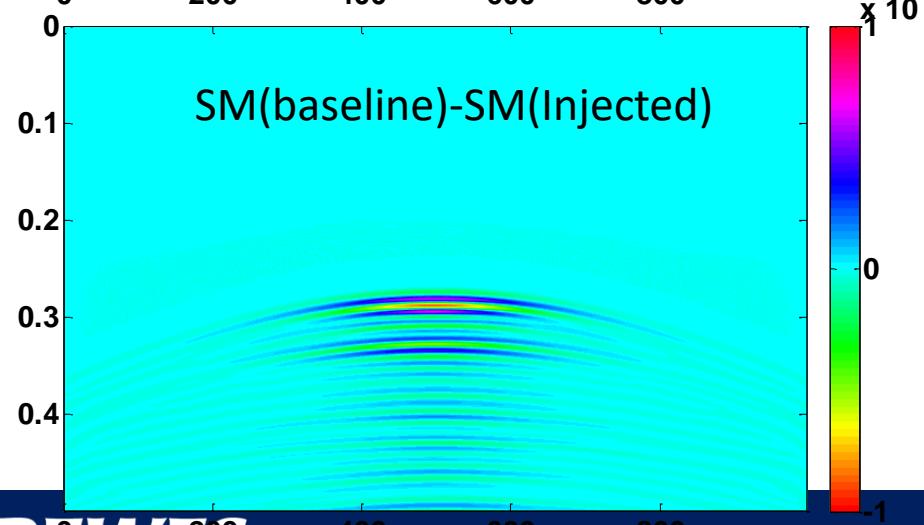
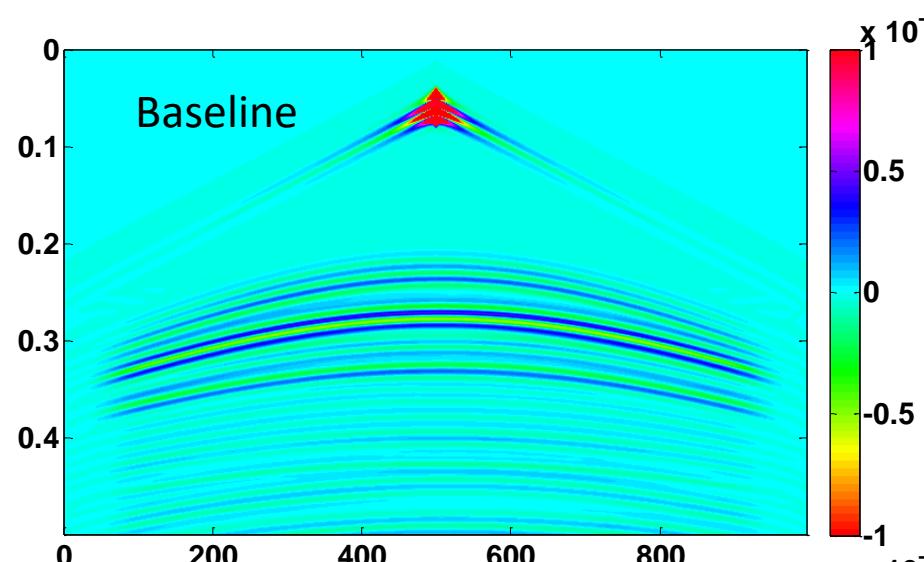
$$I_p(\vec{x}) = \int_0^{T_{max}} S_p(t, \vec{x}) r_p(t, \vec{x}) dt,$$

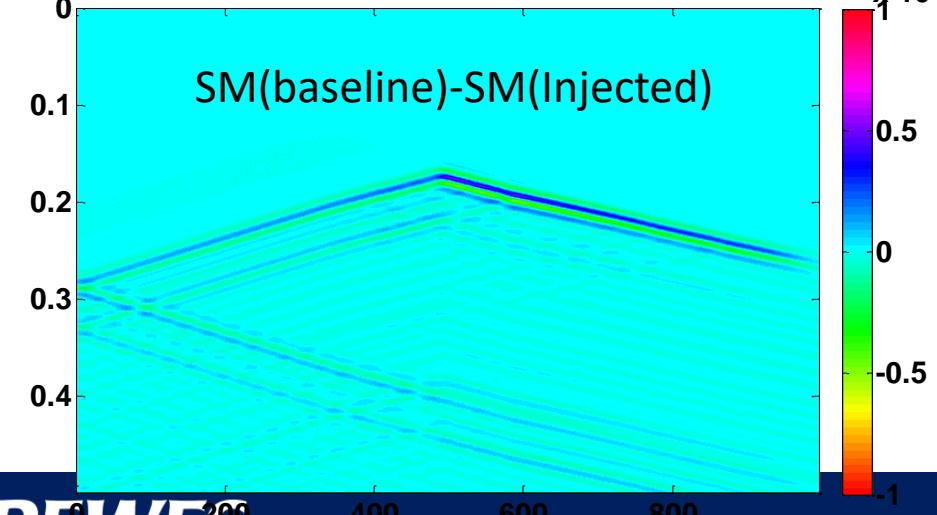
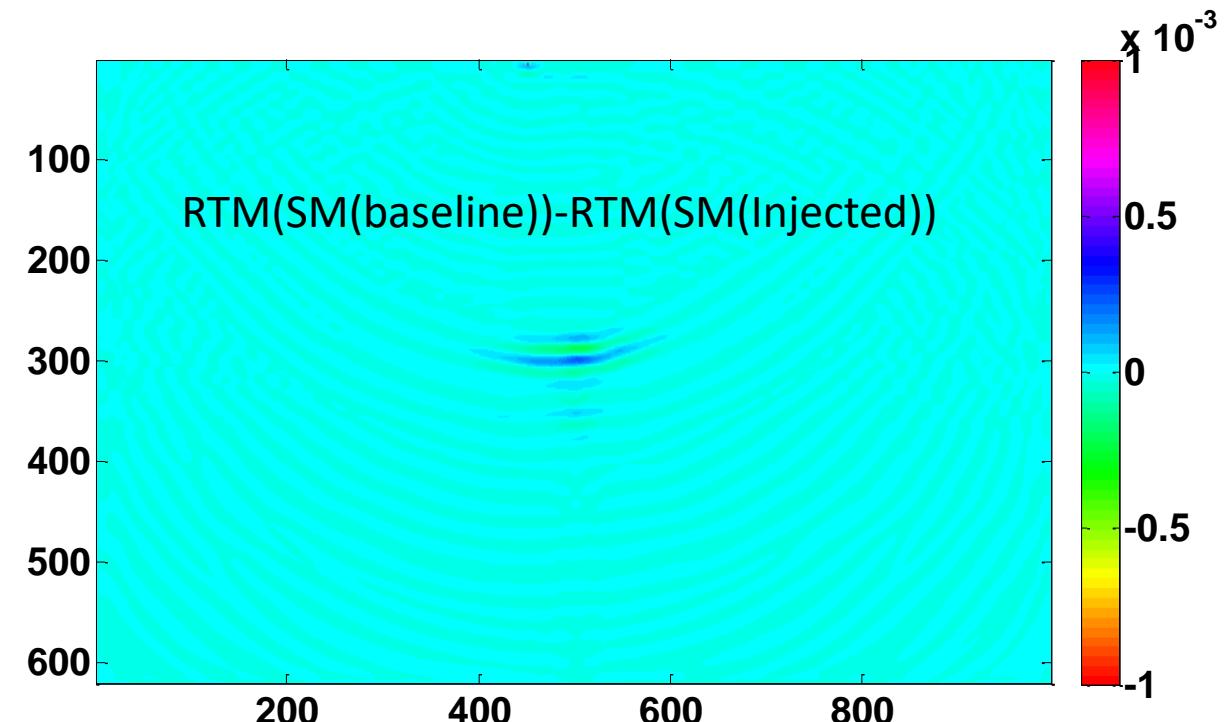
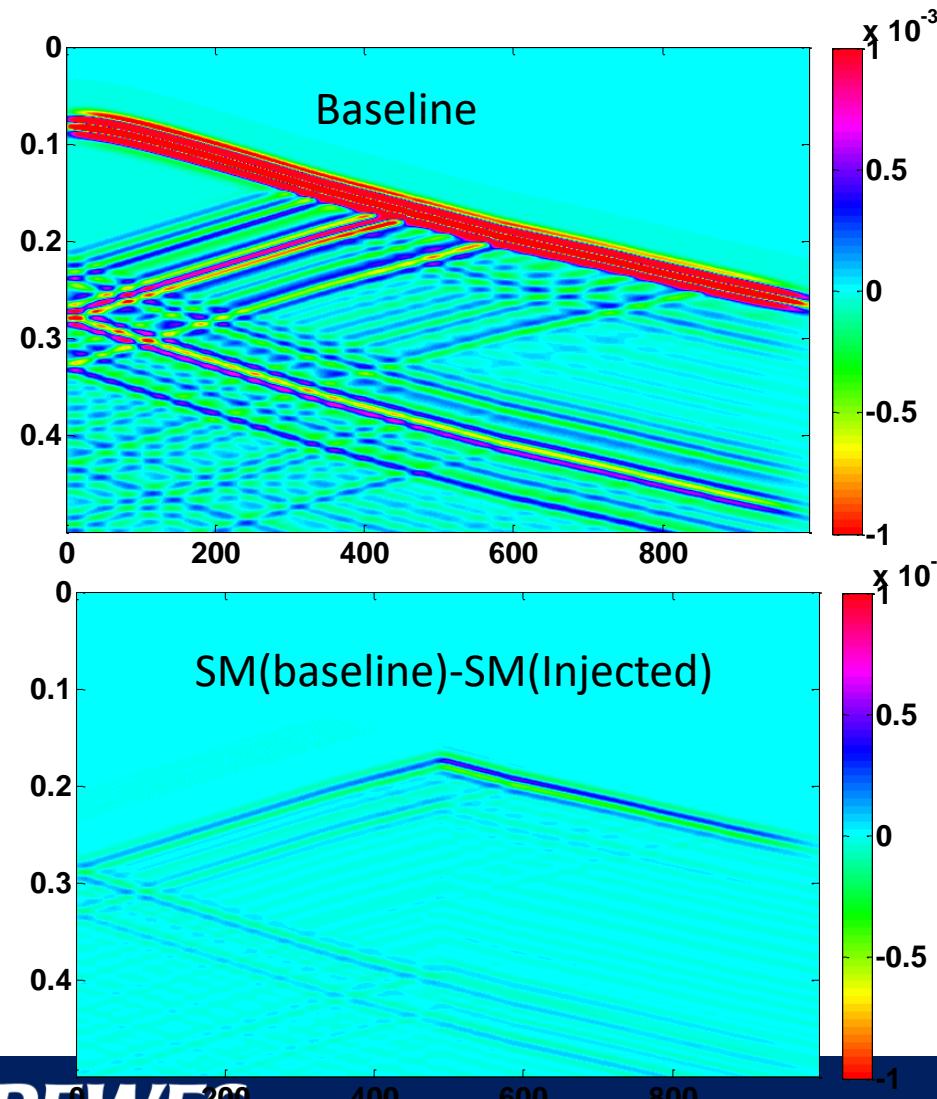
# The base seismic and difference after injection (XW)



# Model set up and seismic response



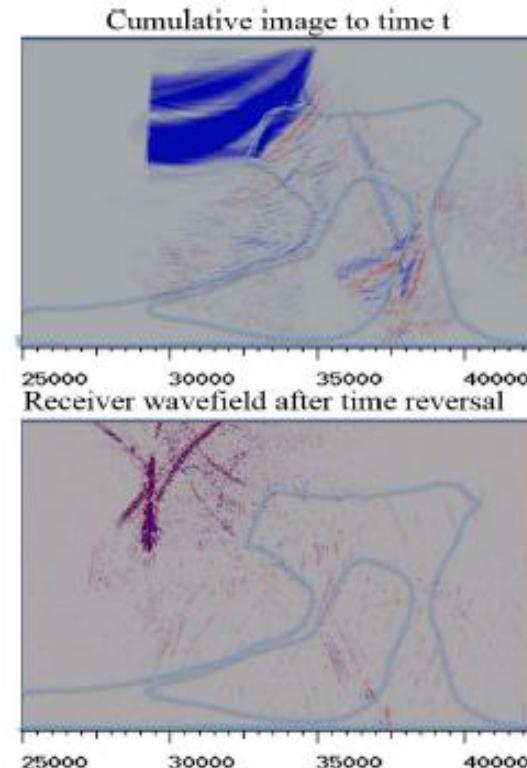
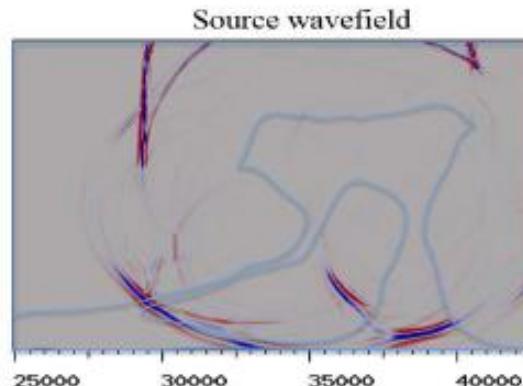




# Cross correlation: The simplest RTM imaging condition

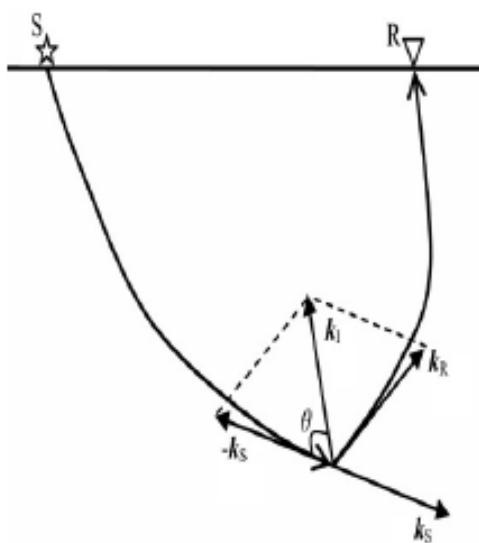
$$I(\mathbf{x}) = \frac{1}{A(\mathbf{x})} \int S(\mathbf{x}, t) R(\mathbf{x}, T-t) dt \quad \mathbf{x} = (x, y, z)$$

- After time reversal of the receiver wavefield, the artifacts of the rtm occur where the two wavefields are traveling **in the same direction**
- Note the accumulating low wavenumber noise through time



(After Whitmore et al., 2012)

# Laplacian filter for low wavenumber noise reduction



$$\nabla^2 \rightarrow -\left(k_x^2 + k_y^2 + k_z^2\right) = -|\vec{k}_I|^2;$$

$$\vec{k}_I = \vec{k}_R - \vec{k}_S$$

$$|\vec{k}_I|^2 = |\vec{k}_R|^2 + |\vec{k}_S|^2 - 2|\vec{k}_R|^2|\vec{k}_S|^2 \cos(\pi - 2\theta) = \frac{4\omega^2}{v^2} \cos^2 \theta$$

$\omega$  = angular frequency;

$v$  = velocity;

$k_R$  = Receiver wavenumber;

$k_S$  = Source wavenumber;

$k_I$  = Image wavenumber;

$k_x$  = spatial wavenumber in x;

$k_y$  = spatial wavenumber in y;

$k_z$  = spatial wavenumber in z;

$\theta$  = Incidence angle.

(After Liu et al., 2010)

## Full Waveform Inversion (FWI) - Concept

