



Migration with surface and internal multiples

Shang Huang and Daniel Trad

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modeling code with PML boundary condition



• Motivation and introduction

• Theory

• Numerical examples

• Conclusion and future work



Multiples can provide additional information for subsurface structures

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RTM (*Liu et al., 2011*) and LSRTM (*Zhang and Schuster, 2013; Liu et al., 2016*): Migrate controlled-order surface multiples FWM (Berkhout and Vershuur, 2016; Davydenko and Vershuur, 2017): Uses an inversion based method to migrate full wavefields Multiples can provide additional information for subsurface structures

RTM (*Liu et al., 2011*) and LSRTM (*Zhang and Schuster, 2013; Liu et al., 2016*): Migrate controlled-order surface multiples

FWM (Berkhout and Vershuur, 2016; Davydenko and Vershuur, 2017): Uses an inversion based method to migrate full wavefields

RTM and LSRTM for surface multiple; FWM with surface and internal multiples



Reverse time migration (RTM) of surface multiple





Reverse time migration (RTM) of surface multiple





Imaging condition in RTM with surface multiple

Artifact-free image: the downgoing (*N-1*)th-order multiple correlates \bullet with the back-propagated Nth-order multiple of the input data



Generation image and crosstalk

Least-squares reverse time migration (LSRTM) with surface multiple



Full-wavefield migration (FWM)



Full-wavefield migration (FWM)



- +: downgoing direction
- -: upward direction
- \vec{P} : wavefields approach a depth level
- \vec{Q} : wavefields leave a depth level
- Wavefield extrapolation operator: W
- Transmission coefficient: $\mathbf{T} = \mathbf{I} + \delta \mathbf{T}$
- Reflection coefficient: \mathbf{R}^{\cap} , \mathbf{R}^{\cup}



Fig 3. Forward modeling in FWM (adapted by Davydenko and Vershuur (2017))

$$\vec{Q}^{+}(z_m) = \vec{P}^{+}(z_m) + \delta \mathbf{T}^{+}(z_m)\vec{P}^{+}(z_m) + \mathbf{R}^{\cap}(z_m)\vec{P}^{-}(z_m)$$
(2)

$$\vec{Q}^{-}(z_m) = \vec{P}^{-}(z_m) + \delta \mathbf{T}^{-}(z_m)\vec{P}^{-}(z_m) + \mathbf{R}^{\cup}(z_m)\vec{P}^{+}(z_m)$$
(3)

$$\vec{P}^{+}(z_{m+1}) = \mathbf{W}(z_{m+1}, z_m)\vec{Q}^{+}(z_m)$$
 (4)

$$\vec{P}^{-}(z_{m-1}) = \mathbf{W}(z_{m-1}, z_m)\vec{Q}^{-}(z_m)$$
 (5)

• Acoustic media: $\delta \mathbf{T}^+ = \mathbf{R}^{\cup}, \ \delta \mathbf{T}^- = \mathbf{R}^{\cap}$

$$\vec{Q}^{+}(z_{m}) = \vec{P}^{+}(z_{m}) + \mathbf{R}^{\cup}(z_{m})\vec{P}^{+}(z_{m}) + \mathbf{R}^{\cap}(z_{m})\vec{P}^{-}(z_{m})$$
(6)
$$\vec{Q}^{-}(z_{m}) = \vec{P}^{-}(z_{m}) + \mathbf{R}^{\cap}(z_{m})\vec{P}^{-}(z_{m}) + \mathbf{R}^{\cup}(z_{m})\vec{P}^{+}(z_{m})$$
(7)

• Acoustic media: $\delta \mathbf{T}^+ = \mathbf{R}^{\cup}, \ \delta \mathbf{T}^- = \mathbf{R}^{\cap}$

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(7)

Scattering term (secondary virtual source) $\delta \vec{S}$

• Acoustic media: $\delta \mathbf{T}^+ = \mathbf{R}^{\cup}, \ \delta \mathbf{T}^- = \mathbf{R}^{\cap}$

$$\vec{Q}^{+}(z_{m}) = \vec{P}^{+}(z_{m}) + \mathbf{R}^{\cup}(z_{m})\vec{P}^{+}(z_{m}) + \mathbf{R}^{\cap}(z_{m})\vec{P}^{-}(z_{m})$$
(6)
$$\vec{Q}^{-}(z_{m}) = \vec{P}^{-}(z_{m}) + \mathbf{R}^{\cap}(z_{m})\vec{P}^{-}(z_{m}) + \mathbf{R}^{\cup}(z_{m})\vec{P}^{+}(z_{m})$$
(7)

Scattering term (secondary virtual source) $\delta \vec{S}$

• Downward and upward propagation wavefields

$$\vec{P}^{+}(z_{m}) = \sum_{n < m} \mathbf{W}(z_{m}, z_{n})[\vec{S}^{+}(z_{n}) + \delta \vec{S}(z_{n})]$$

$$\vec{P}^{-}(z_{m}) = \sum_{n > m} \mathbf{W}(z_{m}, z_{n})\delta \vec{S}(z_{n})$$
(9)

Full-wavefield migration (FWM)



Imaging in full-wavefield migration (FWM)

• Objective function for FWM (Davydenko and Vershuur, 2017)

$$J = \sum_{\omega} ||\Delta \mathbf{P}||_2^2 + f(\mathbf{R}) = \sum_{\omega} ||\mathbf{P}_{obs} - \mathbf{P}_{mod}||_2^2 + f(\mathbf{R})$$
(10)

(11)

The gradient of objective function

$$\mathbf{C}^{\cup}(z_m) = [\Delta \mathbf{P}^{-}(z_m)][\mathbf{P}^{+}(z_m)]^H$$

• Update reflectivity matrix

$$\Delta \mathbf{R}^{\cup}(z_m) = \left(\sum_{\omega} \mathbf{C}^{\cup}(z_m)\right) + f'(\mathbf{R}^{\cup}(z_m)) \quad (12)$$

$$\Delta \vec{P}^{-}(z_{0}) \qquad \vdots \qquad [W(z_{0}, z_{m})]^{H} \\ \Delta \vec{P}^{-}(z_{m}) \qquad \vec{P}^{+}(z_{m}) \\ \Delta R^{\cup}(z_{m}) \qquad Z_{m}$$

Fig 4. Reflectivity updates of both sides can be projected by crosscorrelation between forward-modelled wavefield (green lines) and backward residuals (red lines).

Example 1 – RTM of the first-order surface multiple 1 - RTM



Example 1 – RTM of the first-order surface multiple 1 - RTM



Example 1 – RTM of the first-order surface multiple 1 - RTM













Example 3 – Compare FWM with primary wavefield migration (PWM)

(b) Observed data

(a) True velocity model



Shot record 0.3 0.4 0.5 0.6 0.7 0.8 0.9 0 200 400 600 800 1000 1200 ×10⁴

(c) Forward modeling in FWM



(d) Smoothed velocity model



(e) Forward modeling in PWM



(f) Difference between (c) and (e)



Example 3 – Trace comparison



Example 3 – Reflectivity coefficient comparison



Reflectivity coefficient (trace=128)

Example 3 – Reflectivity coefficient comparison





- RTM and LSRTM with the first-order surface multiple can enhance the illumination and signal-to-noise ratio in the image compared with primary wave
- Accurate separation for primary and multiple energy
- FWM can predict and use surface and internal multiples, recover reflectivity coefficient amplitude
- Background velocity should be close to the true velocity model



- Use surface-related multiple elimination (SRME) to separate and obtain good estimates of primary and multiples
- Work on the iterative approach and generate f-x extrapolation operator to deal with lateral velocity variation
- Update velocity model



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Thank you!